Molecular Dynamics and Accelerated Molecular Dynamics

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Lecture 1

Tutorial Lecture Series
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Overall Outline

Day 1:   Molecular dynamics methods

Day 2:   Molecular dynamics methods

Day 3:   Infrequent events, transition state theory, saddle finding, etc.

Day 4:   Accelerated molecular dynamics methods

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Molecular Dynamics (MD)

Evolve a system of atoms according to the classical equations of motion (F=ma)

N atoms ---> 6N coordinates {**x,p**}

x_i = position of atom i

p_i = momentum of atom i

v_i = p_i/m_i = velocity of atom i

Equations of motion:

$$\frac{\partial x_i}{\partial t} = \frac{p_i}{m}$$

$$\frac{\partial p_i}{\partial t} = -\frac{\partial V}{\partial x_i}$$

Typically, potential V is solely due to interactions among the atoms (but need not be).

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Brief History of MD

First MD simulation

      B.J. Alder and T.E. Wainwright, 1956 - hard sphere liquid, phase transition

First MD simulations with a continuous potential

      G.H. Vineyard et al, 1959 -- radiation damage simulation with a pair potential

   A. Rahman, 1964 - Lennard-Jones liquid

Some points

In nature, V comes from the electronic interactions -- the electronic wavefunction. In MD, this is typically swept under the rug, leaving just a relatively simple functional form for V. (Although sometimes we do better than this.)

The system is evolved on the Born-Oppenheimer surface -- i.e., V is for the ground state of the system, and the electronic wavefunction is assumed to instantaneously adapt to the current configuration of atoms ($m_{electron} << m_{nucleus}$).

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Why do we do MD?

MD is the highest level (i.e., the largest scale) model that gives dynamics in full atomistic detail in an unbiased fashion.

There is no approximation beyond the choice of interatomic potential and the assumption of (nonrelativistic) classical mechanics.

Interatomic potential + boundary conditions

↓

Integrate equations of motion

↓

Observations, predictions
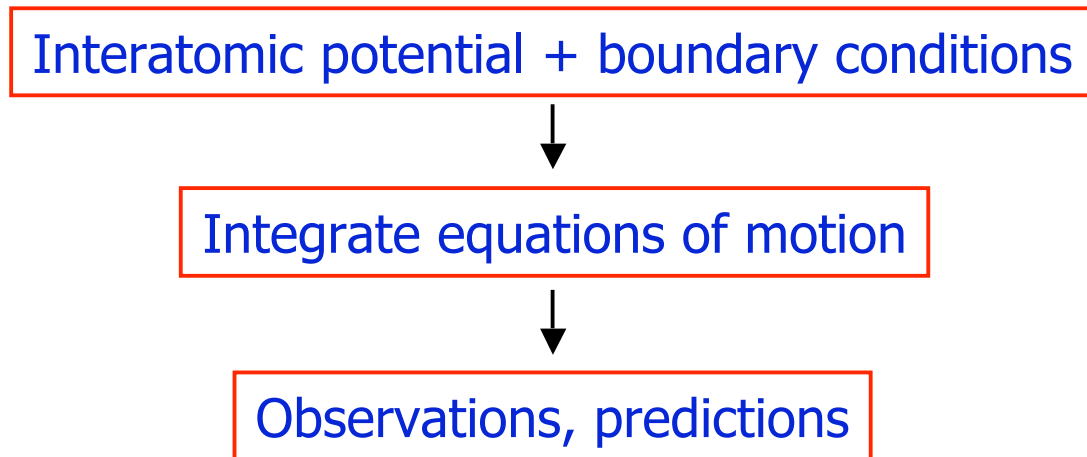
Gives the "truth" for the chosen interatomic potential -- very appealing.

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Why do we do MD? (cont)

With a good-quality potential, we can use MD to interpret
experiment, make experimentally testable predictions, and gain
a physical understanding of real systems at the atomic level.

Also, MD simulations can themselves be considered to be
"experiments."
- test higher-level models
- parameterize higher-level models
- to simply see what happens*

*Often, MD simulations show unexpected, surprising results,
forcing the development of better theory, better
understanding, and new experiments.

Properties we can calculate/study

Pair distribution function in a liquid
Diffusion constant in a a liquid
Structure factor in a liquid
Pressure vs. volume
Thermal expansion
Melting point
Surface melting
Free energy differences between phases
Defect dynamics and diffusion in solid (*)
Surface diffusion (*)
Surface sputtering
Surface scattering
Thermal conductivity

Shock waves
Detonation
Radiation damage events
Grain boundary structure
Vapor deposition (*)
Fast fracture
Nanoindentation
Fast plastic flow
Grain boundary sliding (*)
Protein structure (*)
Protein function (*)
Protein dynamics (*)

(* = may be limited by MD time scale)

Limited primarily by imagination.

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Interatomic Potentials - first pass

Simplest: pair potential

$$V = \frac{1}{2} \sum_{\substack{i \neq j}}^{N} \phi(r_{ij})$$

$\phi(r)$
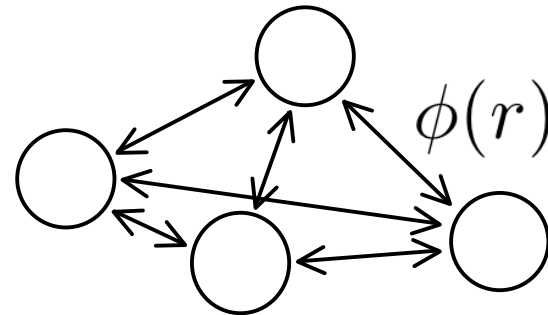
e.g., Lennard-Jones 6-12:

$$\phi(r_{ij}) = 4\epsilon \left[\left(\frac{\sigma}{r_{ij}} \right)^{12} - \left(\frac{\sigma}{r_{ij}} \right)^{6} \right]$$

short-range repulsion

dispersion interactions

σ = length scale
ε = energy scale
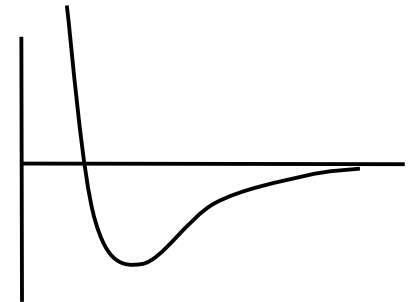
LJ is appropriate for argon, for example.

A.F. Voter, September, 2005 LAUR-05-8125

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Interatomic potentials

Potential cutoff (typical for non-ionic materials)

good   bad

With cutoff, forces depend only on nearby atoms, and overall computational work scales as N.

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Interatomic potentials

Potential cutoff (typical for non-ionic materials)

good

still bad
(perhaps even worse!)

With cutoff, forces depend only on nearby atoms, and overall computational work scales as N.

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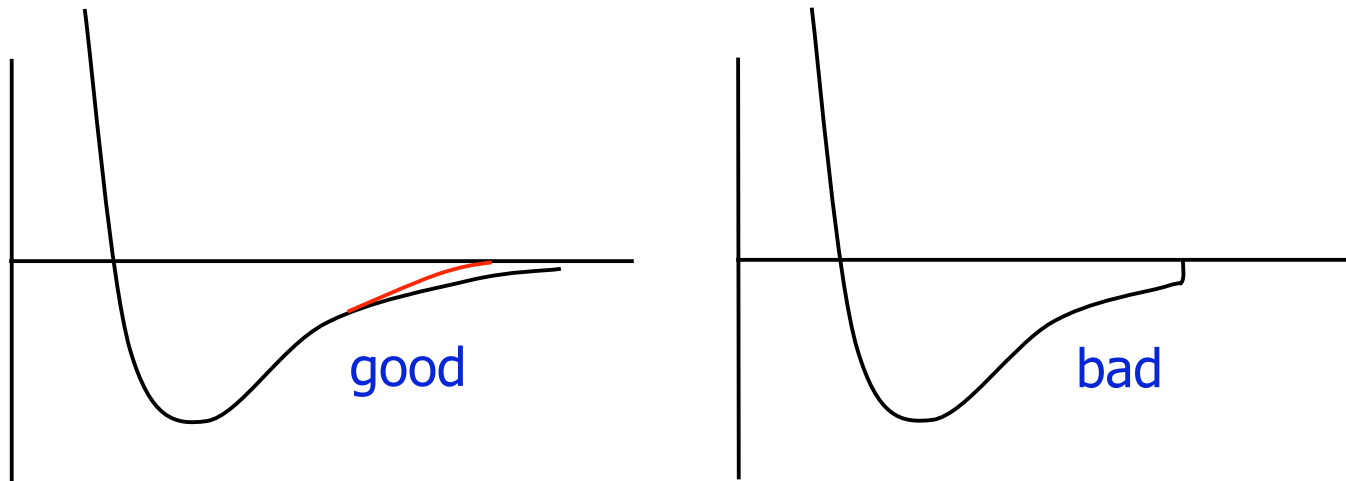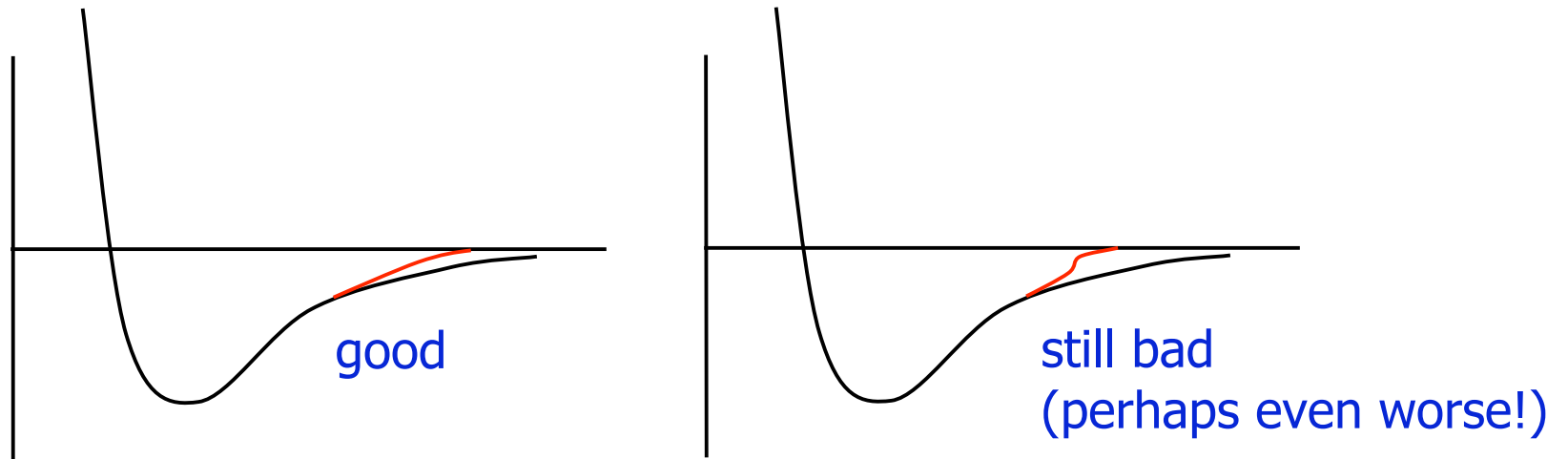
Integrating the equations of motion

For each atom i:

$$\frac{\partial x_i}{\partial t} = \frac{p_i}{m}$$

$$\frac{\partial p_i}{\partial t} = -\frac{\partial V}{\partial x_i}$$

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Verlet Algorithm

Most commonly used method for MD these days.

Given **x**(t), **p**(t-Δt/2),

First advance p:

$$p_i(t + \Delta t/2) = p_i(t - \Delta t/2) - \frac{\partial V(\mathbf{x}(t))}{\partial x_i} \Delta t$$

Then advance x:

$$x_i(t + \Delta t) = x_i(t) + \frac{1}{m} p_i(t + \Delta t/2) \Delta t$$

x and p jump over each other, staying out of phase by Δt/2.

This is "leapfrog Verlet." There are other types of Verlet (e.g., velocity Verlet), but they all give the same integration.

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Verlet Algorithm

Simple.

Error term is 4th order.

Symplectic (conserves volume in phase space, as real Hamiltonian dynamics should).

Time reversible.

Within stability limit (Δt <= ~period/20), conserves energy for an extremely long time.

Typical time step: metals 2-6 fs, proteins 0.5-1 fs

Typically the best choice for most any MD simulation.

Verlet energy conservation

Too-large Δt

Large delta Δt

Total energy
(V + Σp²/2m)

Moderate delta Δt

Small delta Δt
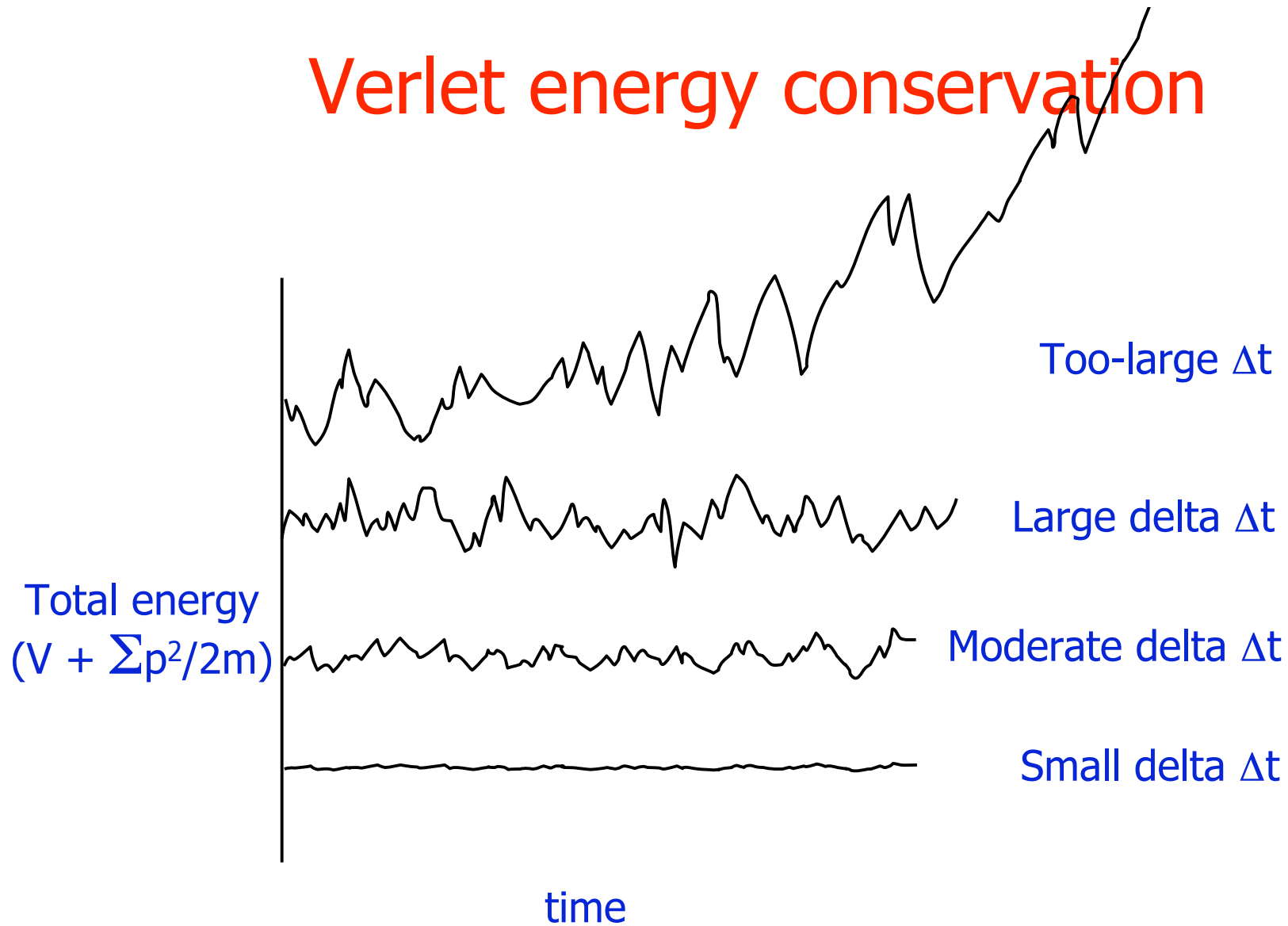
time

Energy fluctuates, but mean is very stable over long times.

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Verlet vs. Runge Kutta

Total energy $(V + \Sigma p^2/2m)$

Verlet

4th order Runge Kutta

time

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Verlet vs. Runge Kutta

Total energy
$(V + \Sigma p^2/2m)$

Verlet

4th order Runge Kutta
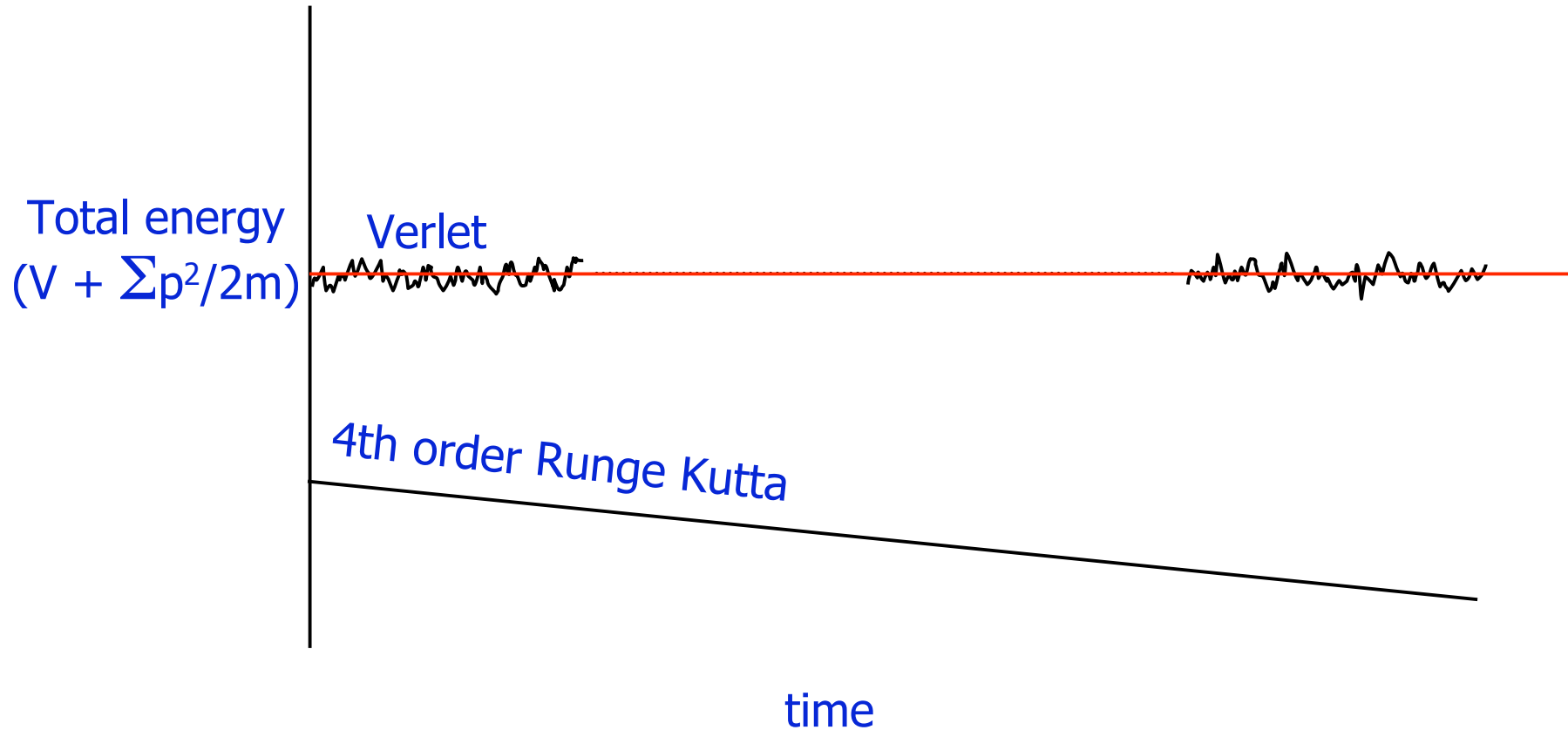
time

10-atom Lennard-Jones cluster
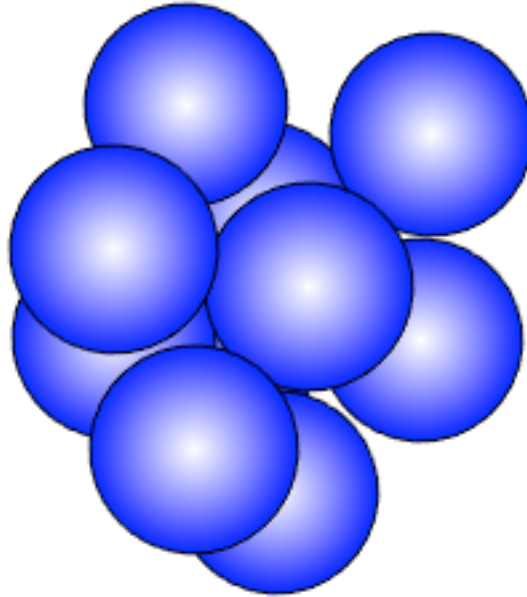
Parameterized to be sort of like silver
Verlet time step = 5 fs
Kinetic temperature ~500K
10 ps movie
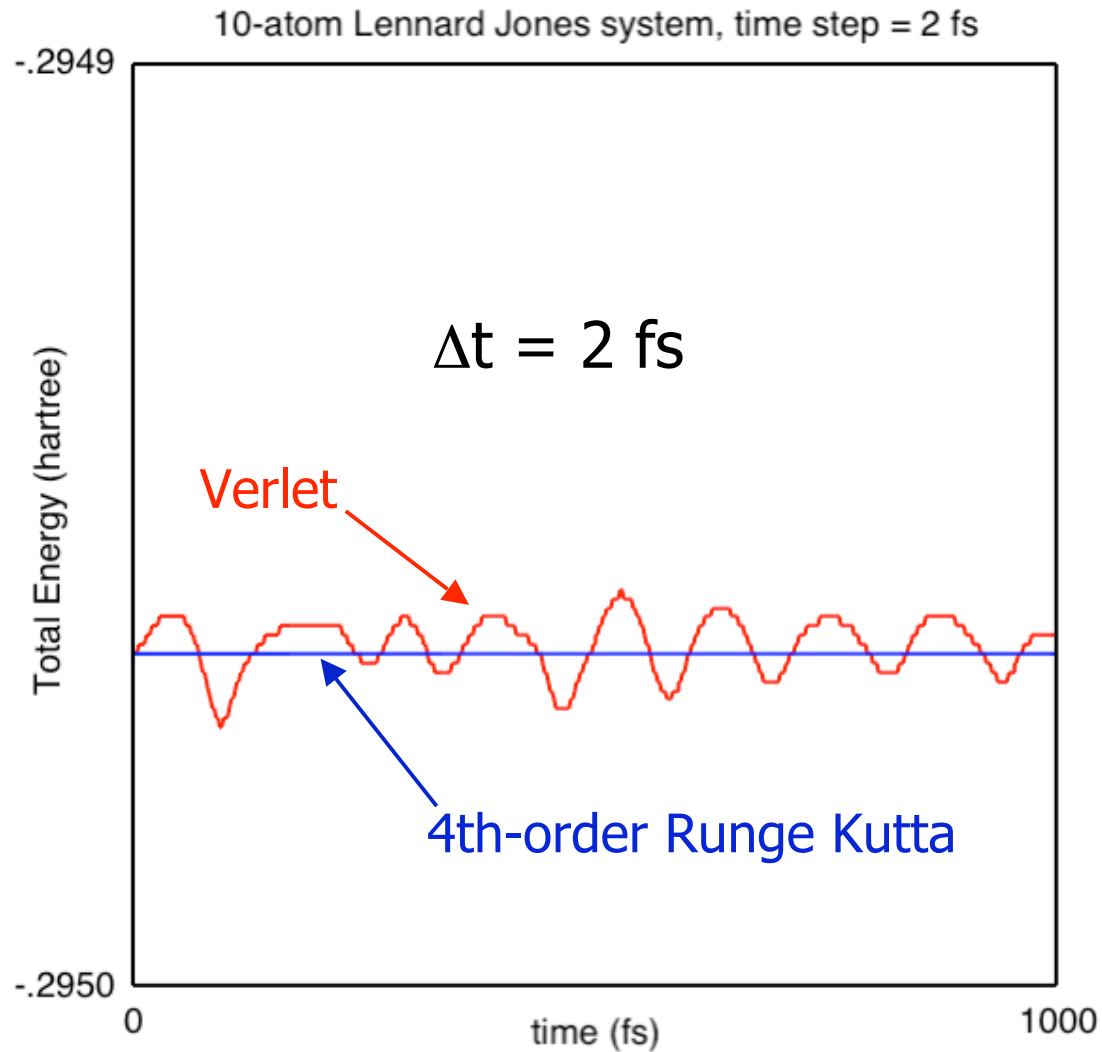
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Verlet versus Runge Kutta

10-atom Lennard Jones system, time step = 2 fs

$\Delta t = 2$ fs

short time

Verlet

4th-order Runge Kutta

Total Energy (hartree)

-.2949

-.2950

time (fs)

0   1000

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Verlet versus Runge Kutta

10-atom LJ system, time step = 1,10 fs (RK), 10 fs (Verlet)

Total Energy (hartree)

-.29

-.30

Verlet, Δt = 10 fs

long time

1 fs

10 fs   Runge Kutta

0   time (ns)   1

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Verlet versus Runge Kutta

10-atom LJ system, time step = 1,10 fs (RK), 10 fs (Verlet)

Verlet, Δt = 10 fs

even longer time

Runge Kutta, Δt=1 fs

Total Energy (hartree)

-.2946

-.2956

0   time (ns)   100
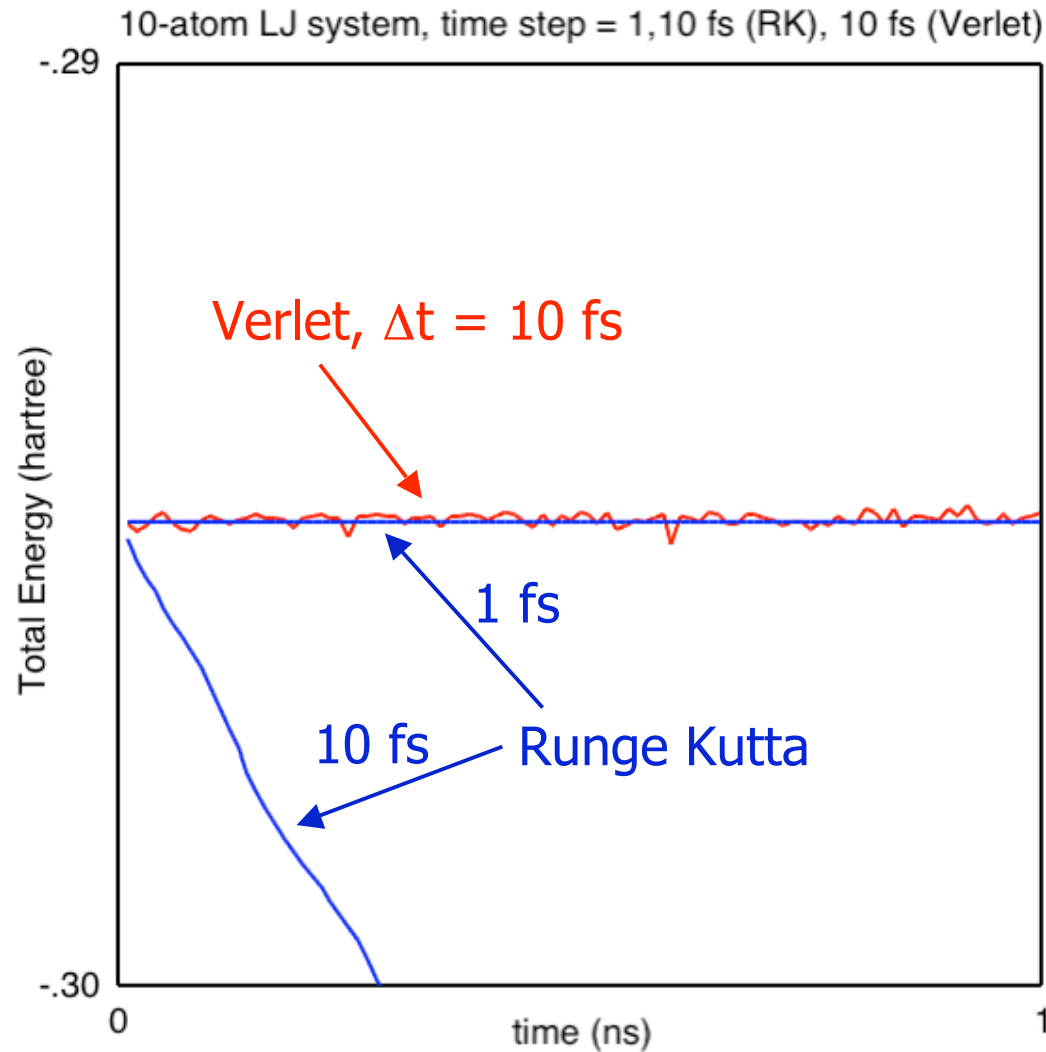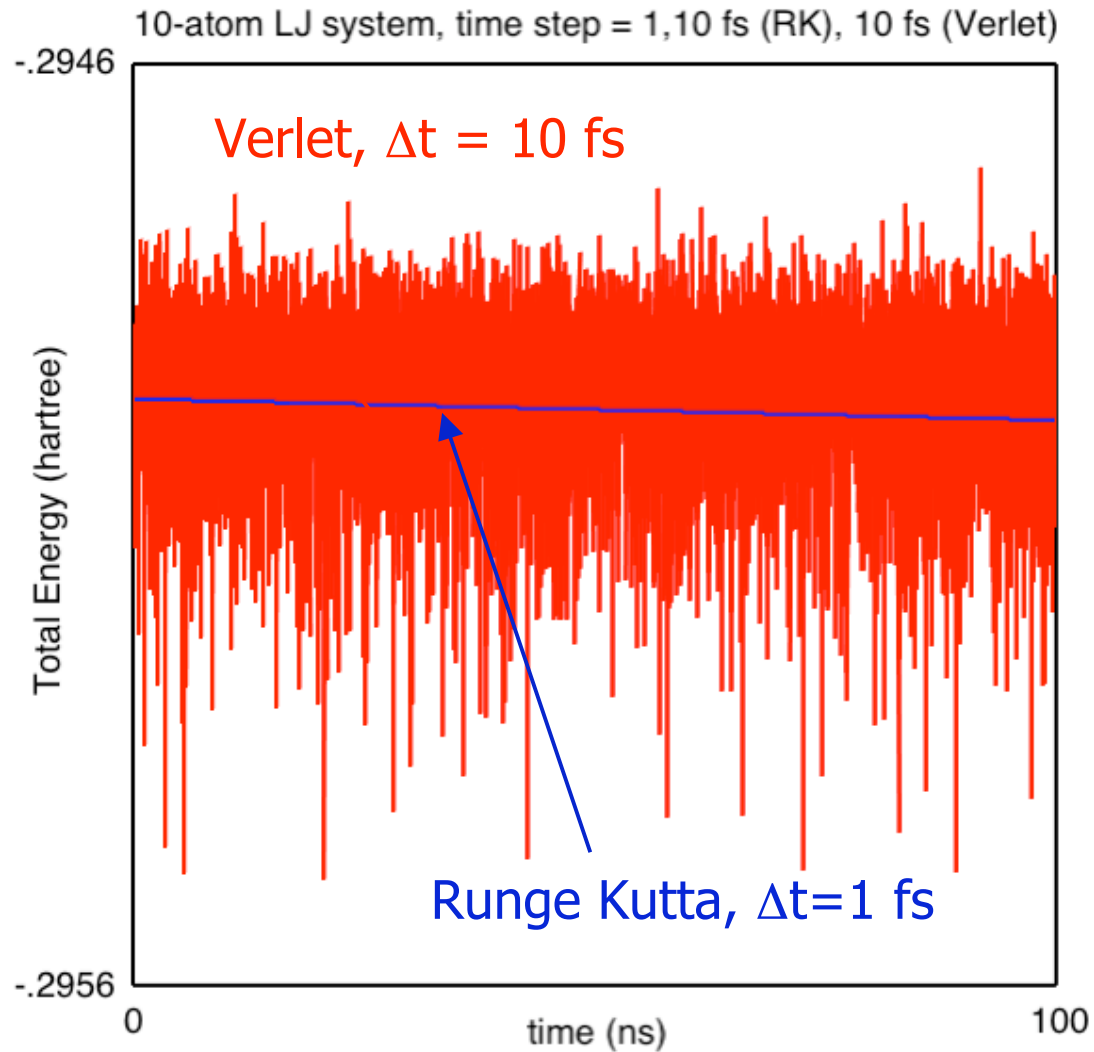
Integrators - other point(s)

Computational cost is almost always dominated by the cost of the force call (evaluating dV/dx), not by the integrator itself.

Periodic boundary conditions

We often use periodic boundary conditions to mimic infinite bulk system -- liquid, solid, surface, …

Periodic boundary conditions

Primary period
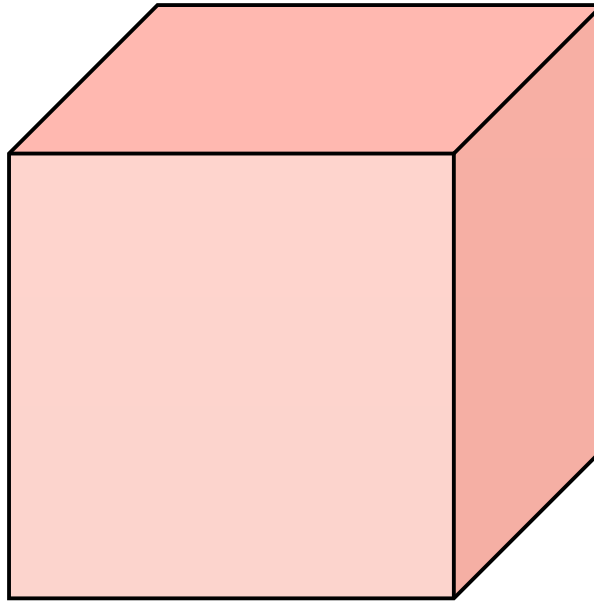
period length

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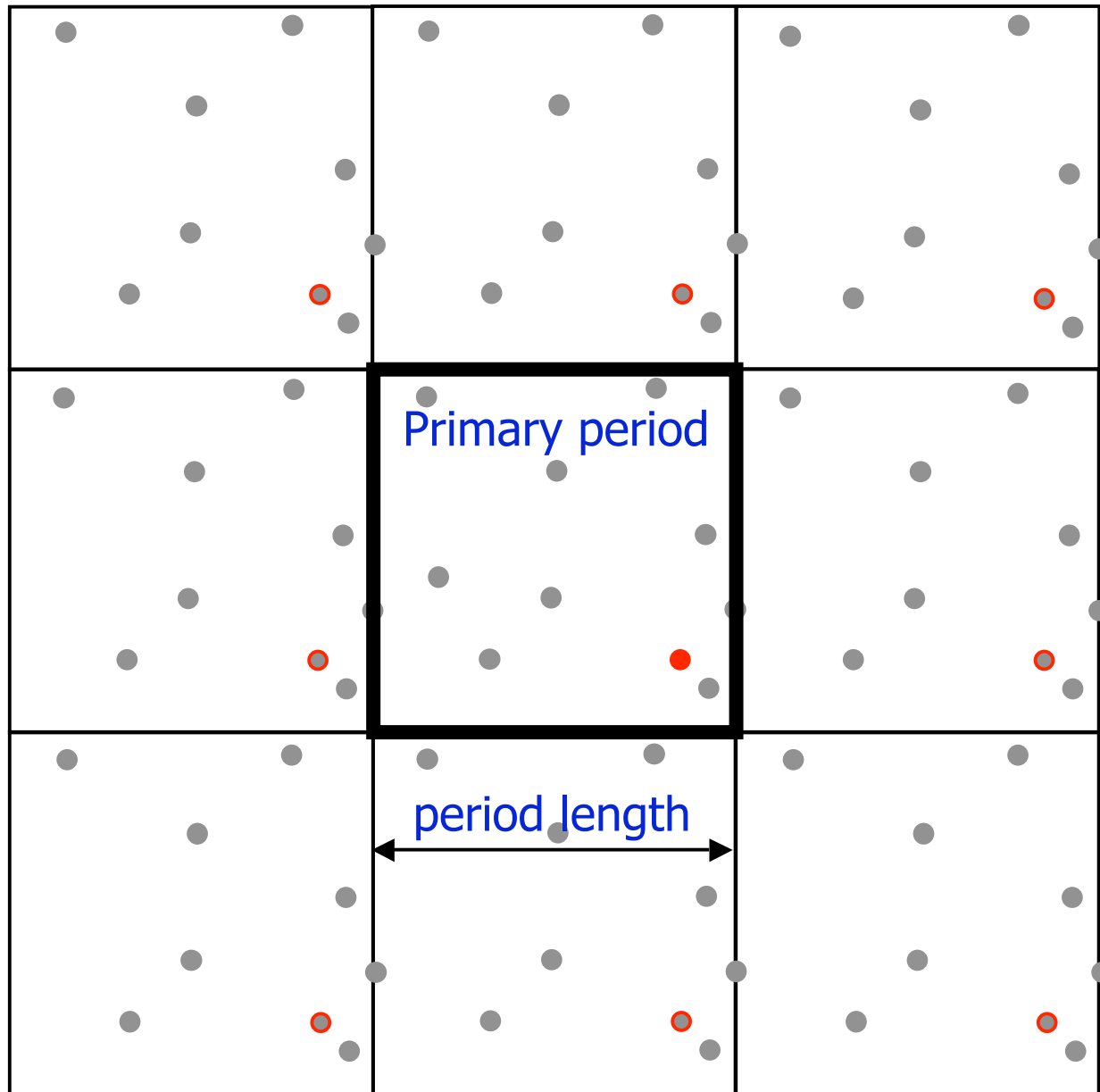
Minimum-image condition
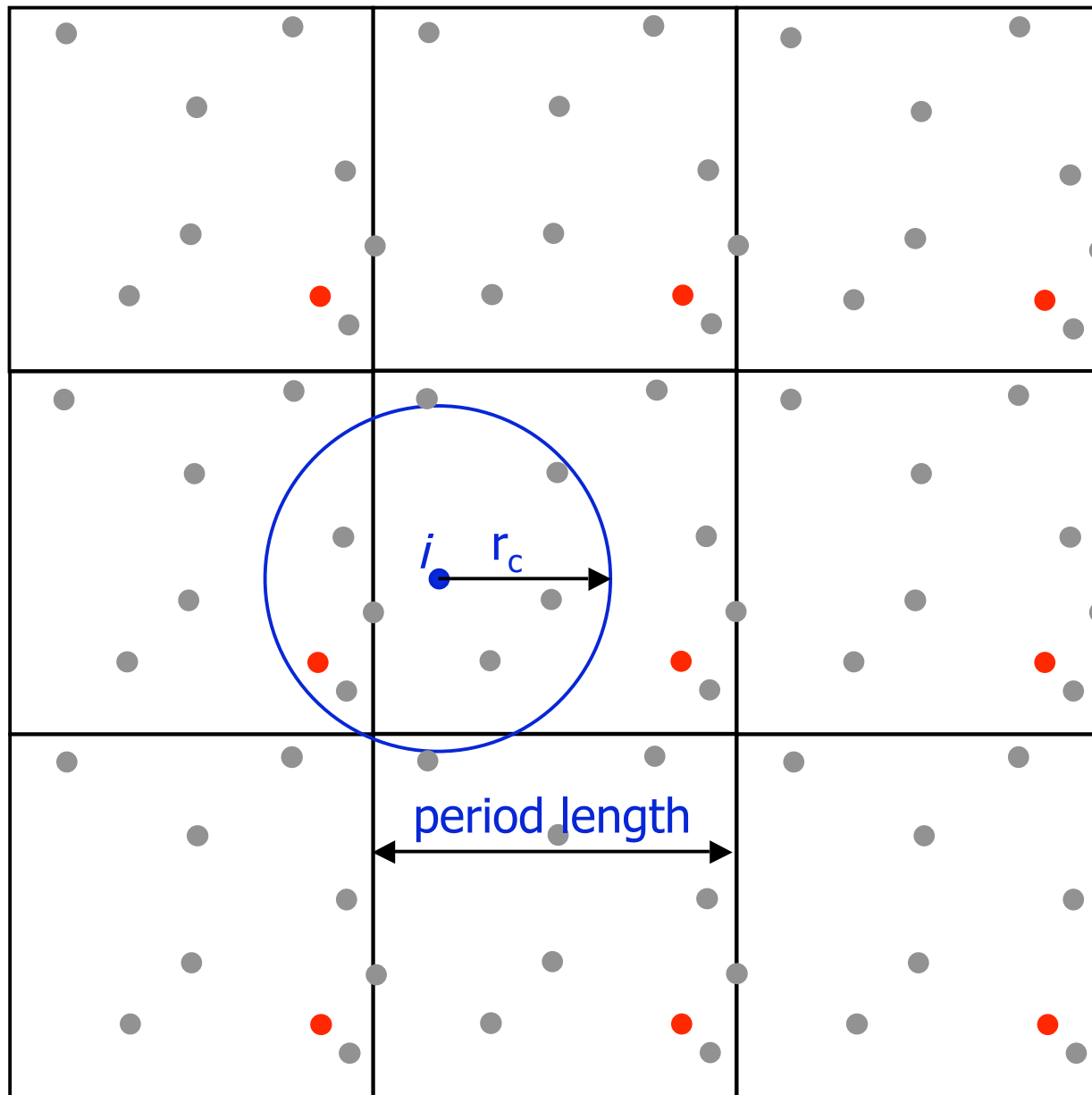
If r_c < period length/2, then only one image of each neighbor will be within cutoff distance of atom i.

This simplifies construction of the neighbor lists, and reduces artificial behavior.

i r_c

period length

Verlet list
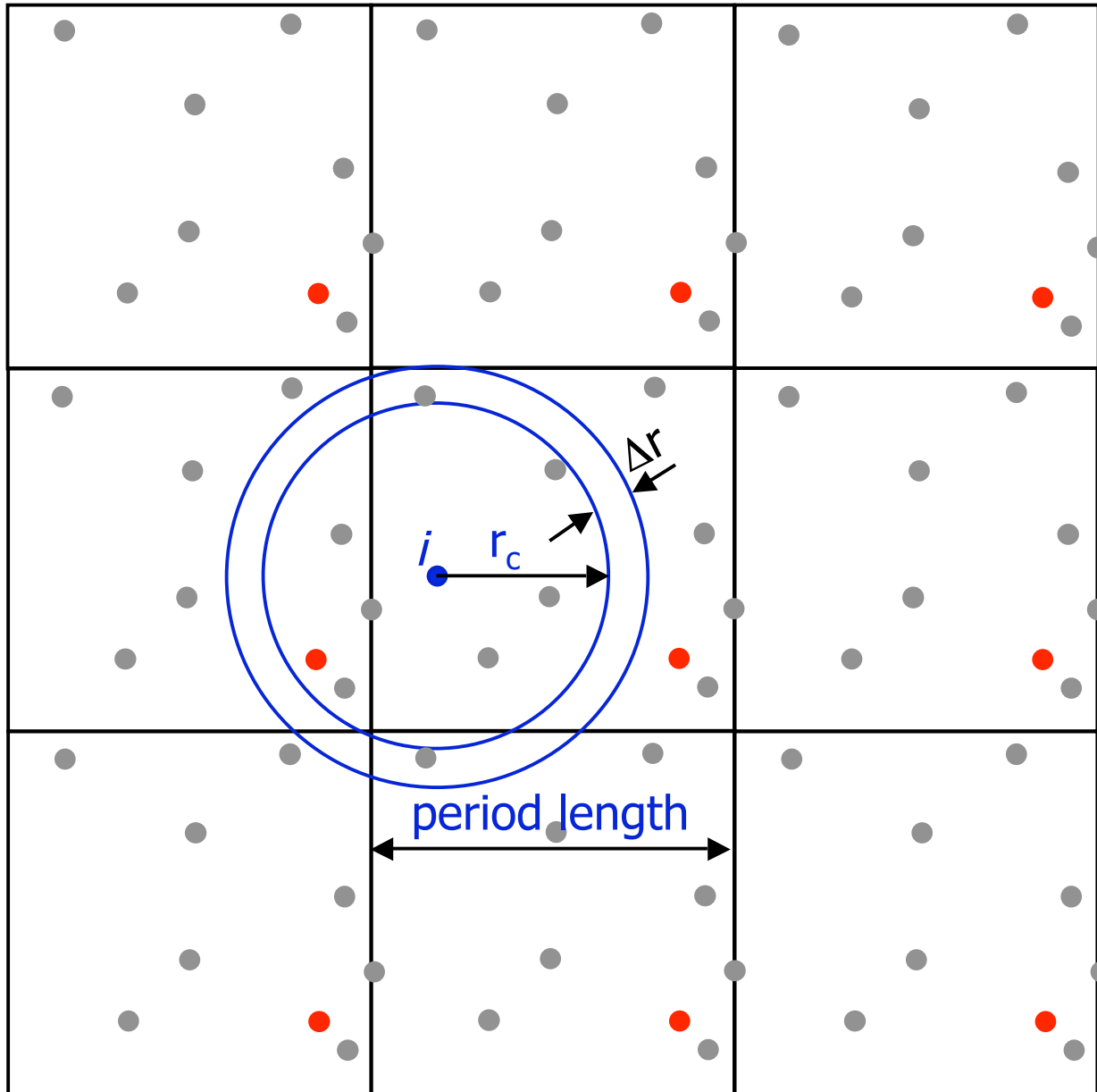
Make list of neighbors within a larger cutoff range.

Compute neighbor distances from this list.

Only update the list after some atom has moved more than Δr - typically many MD steps.

Cell list (for large N)
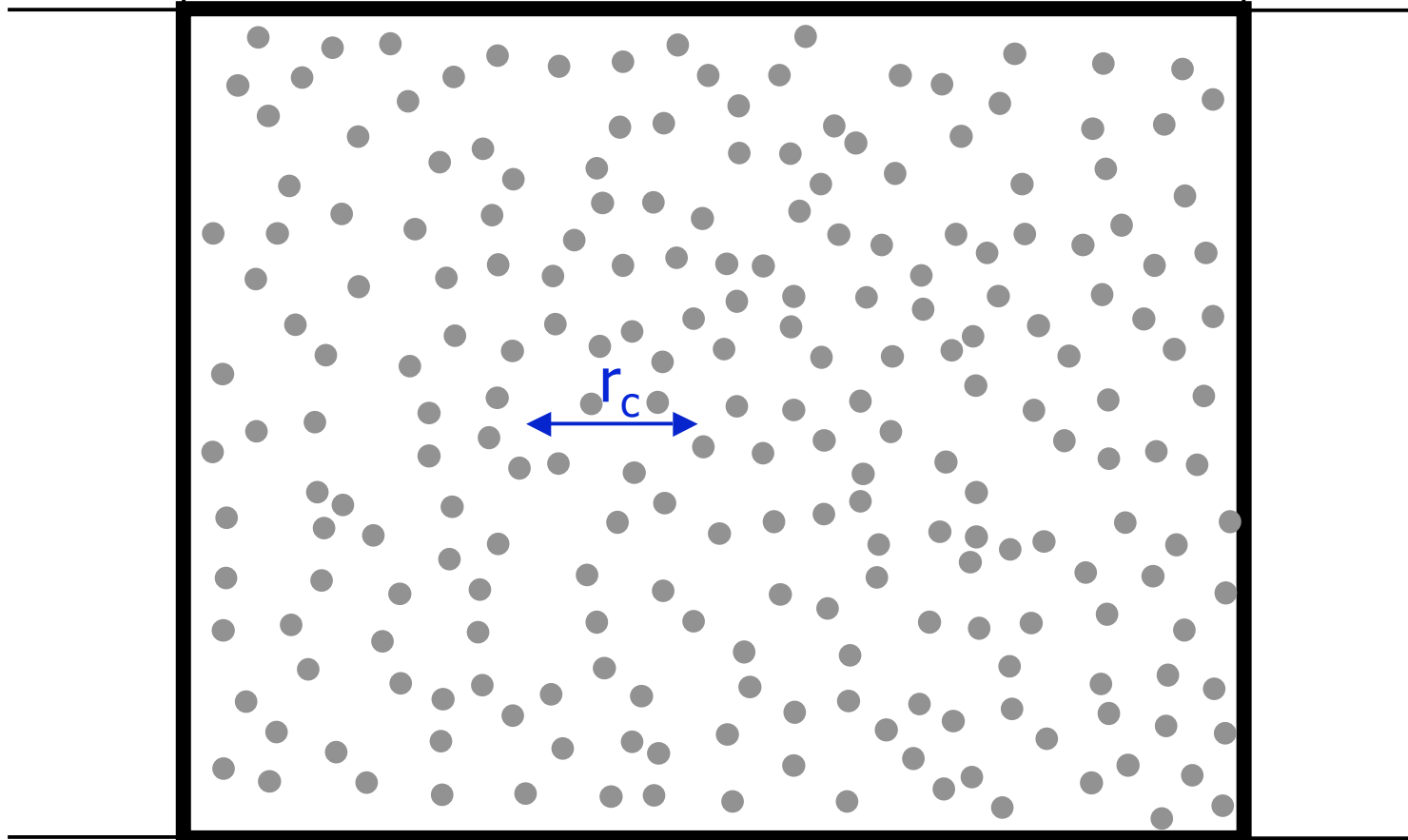
r_c

Make cells with edge length $>r_c$.
Assign each atom to its cell.
Only search adjacent cells when making neighbor list.
Overall work scales as N.

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Cell list (for large N)

r_c

Make cells with edge length $>r_c$.
Assign each atom to its cell.
Only search adjacent cells when making neighbor list.
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Cell list (for large N)

Make cells with edge length >r_c.
Assign each atom to its cell.
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Cell list (for large N)
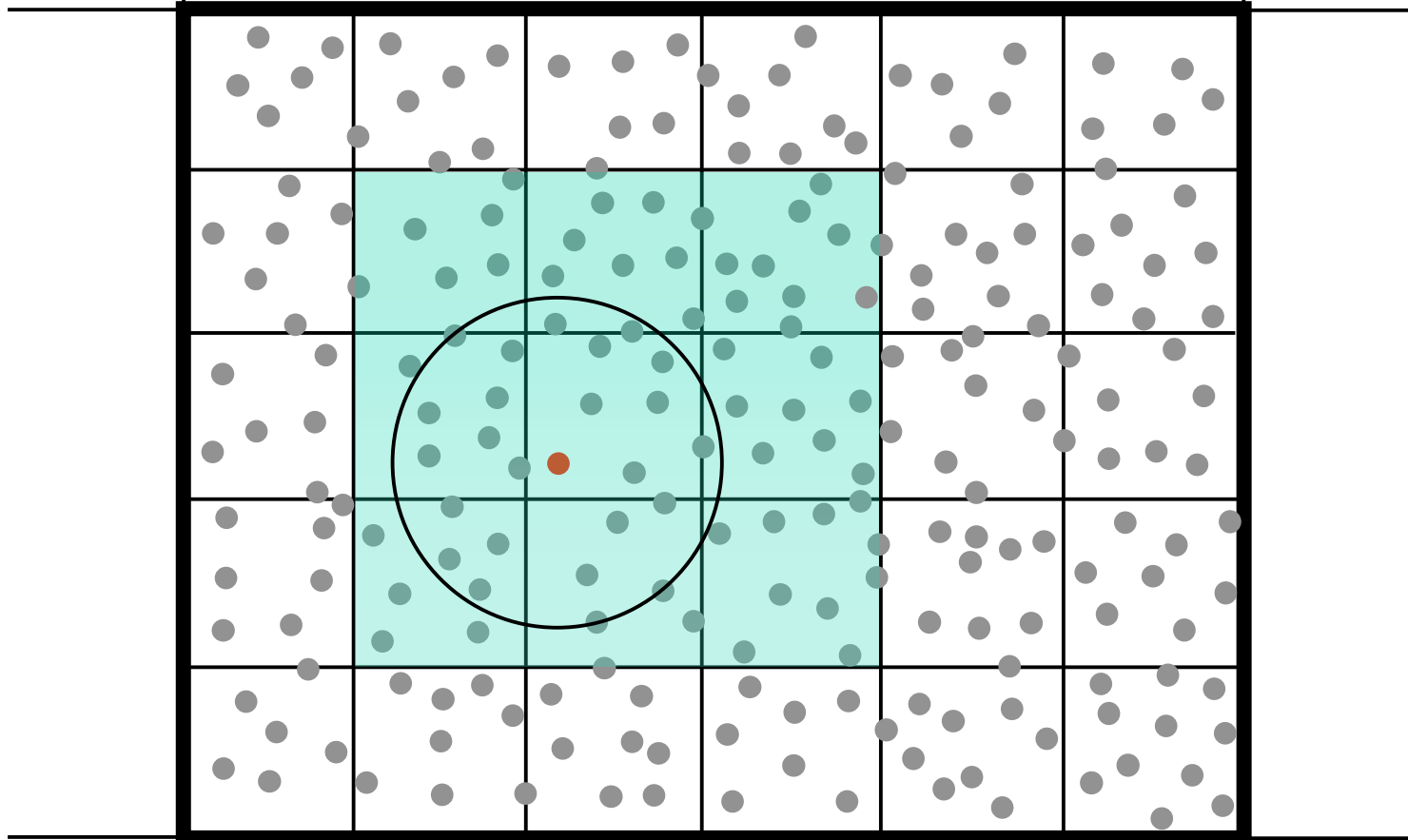
Make cells with edge length $> r_c$.
Assign each atom to its cell.
Only search adjacent cells when making neighbor list.
Overall work scales as N.

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Limitations of MD

- Accuracy of potential

- Length scale - not macroscopic

- Time scale - limited to ns

- Quantum dynamical effects

- Non adiabatic dynamics

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Accuracy of potentials

Good systems:
    Noble gases (Ne, Ar, …)
    Certain fcc metals (Cu, Ag, Ni)

OK systems:
  - many metal systems (Pt, Fe, V …)
  - ionic systems (NaCl, MgO,…)
  - proteins, polymers (but not perfect, and bonds can't break)
  - silicon (record number of fits)

Problem systems:
  - mixed ionic-covalent systems (e.g., Pt/MgO)
  - mixed metallic-covalent systems (e.g., C in Fe)

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MD - achievable length scales

10^3 - 10^4 atoms easy on single processor

Much larger systems possible via parallelization

Each processor responsible for atoms in a physical cell
Communication required between adjacent cells
$>\sim10^3$-10^4 atoms per processor to maintain good efficiency

Million atoms -- now fairly routine

Billion atoms -- possible

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Cu Cascade simulation
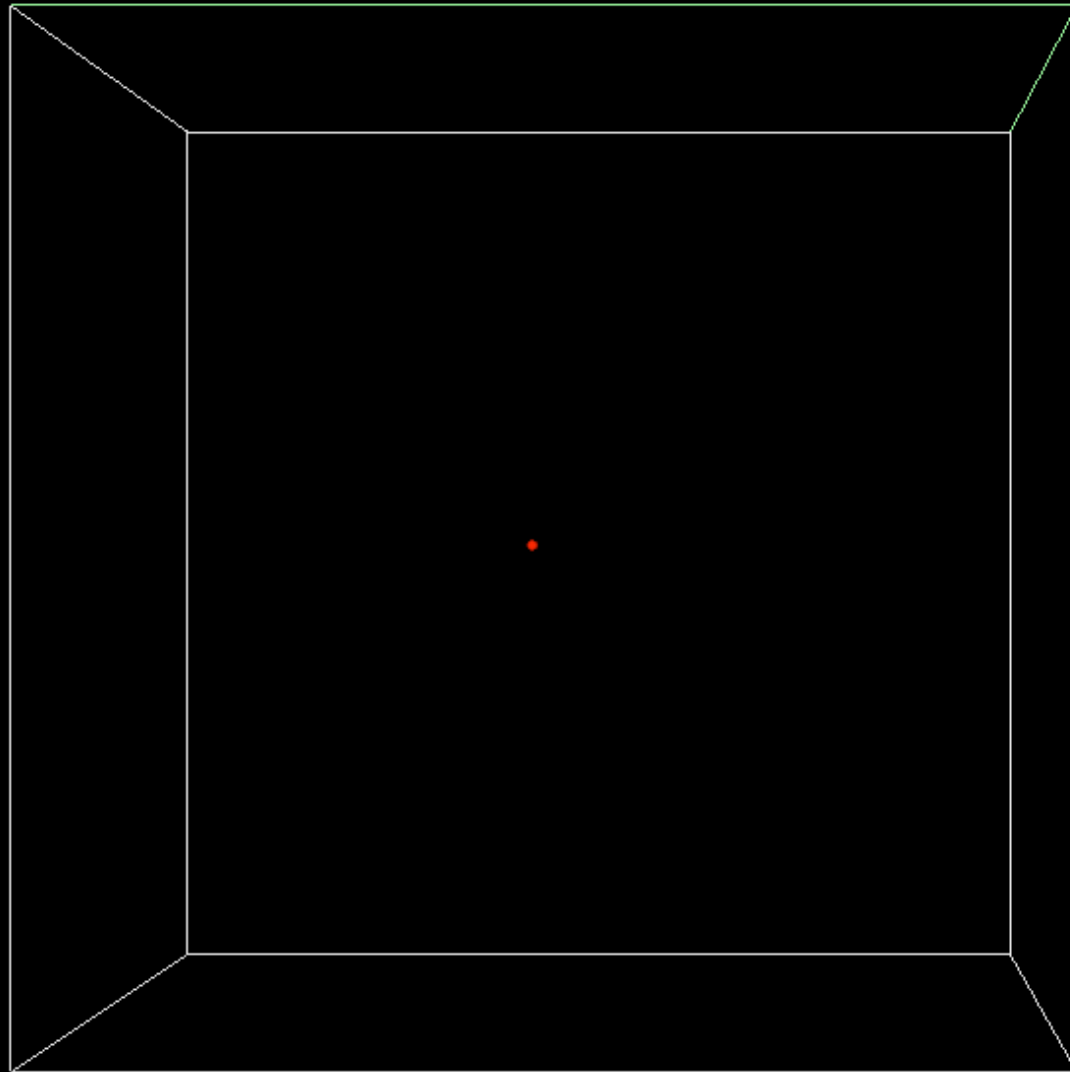
Copper 25keV:

Cube faces (100)
Cube size = 25nm
2.048.000 atoms
Temperature=100K

time = 0.006ps

NFP = 1

Legend :

Displaced atoms

Vacant sites

D.J. Bacon
et al
(Liverpool)

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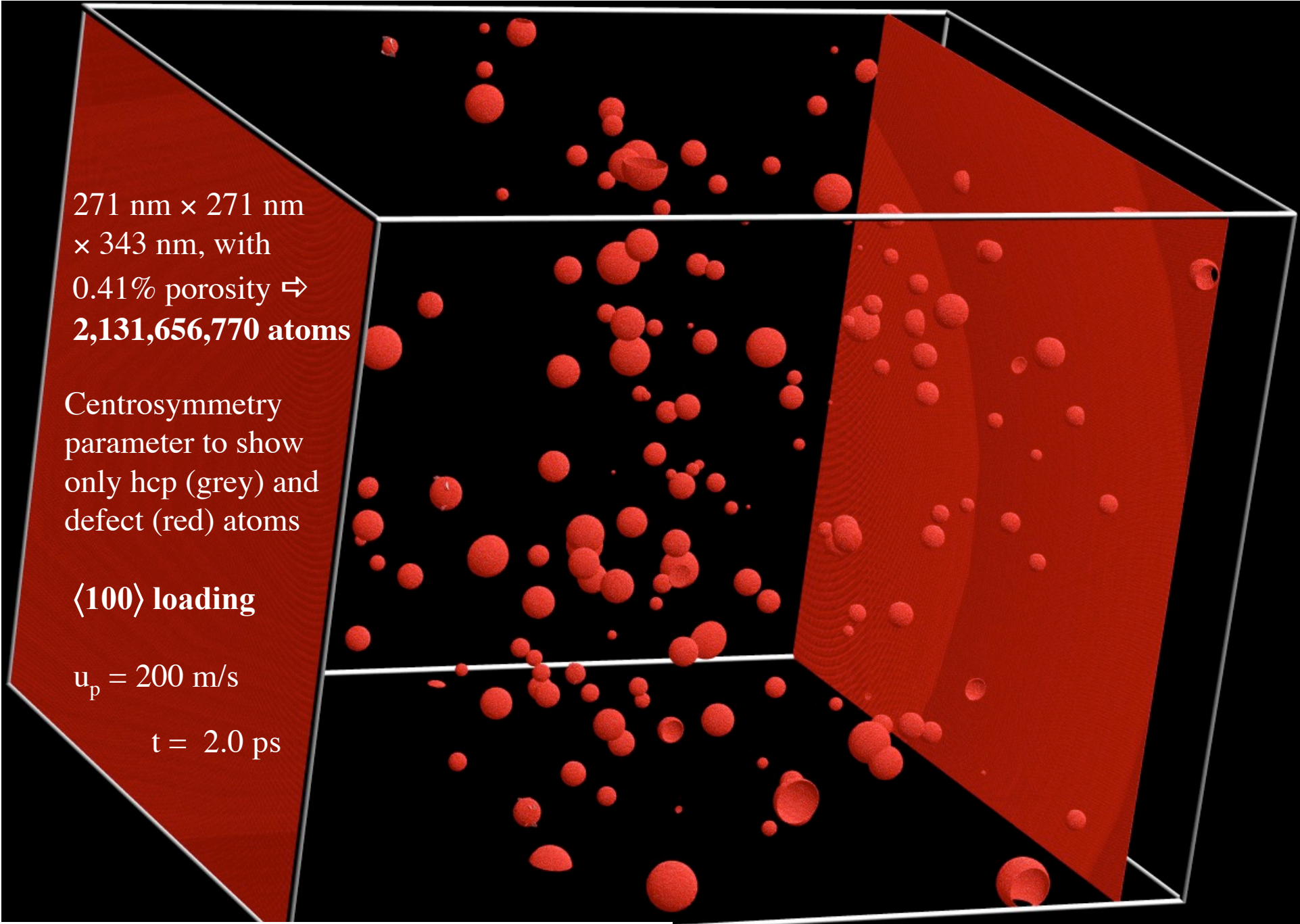
Cu Cascade simulation
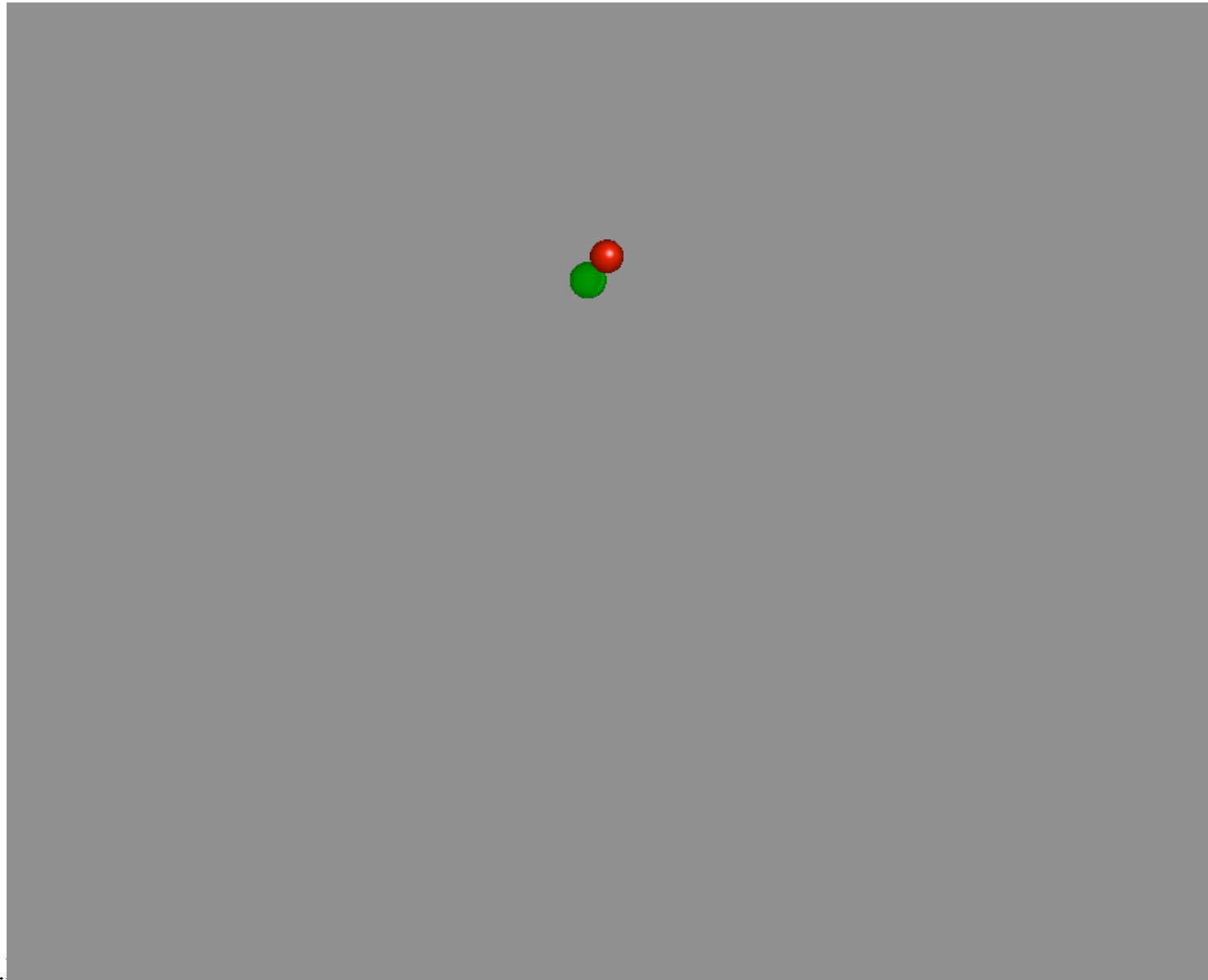
25 keV, copper

green=interstitial
red=vacancy

D.J. Bacon et al

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A.

271 nm × 271 nm × 343 nm, with 0.41% porosity ⇨ **2,131,656,770 atoms**

Centrosymmetry parameter to show only hcp (grey) and defect (red) atoms

⟨100⟩ loading

u_p = 200 m/s

t = 2.0 ps

Germann, Holian, Kadau, and Lomdahl, 2005

t = 8.0 ps

Germann, Holian, Kadau, and Lomdahl, 2005

t = 11.0 ps

t = 13.0 ps

t = 17.0 ps

t = 19.0 ps

t = 19.0 ps
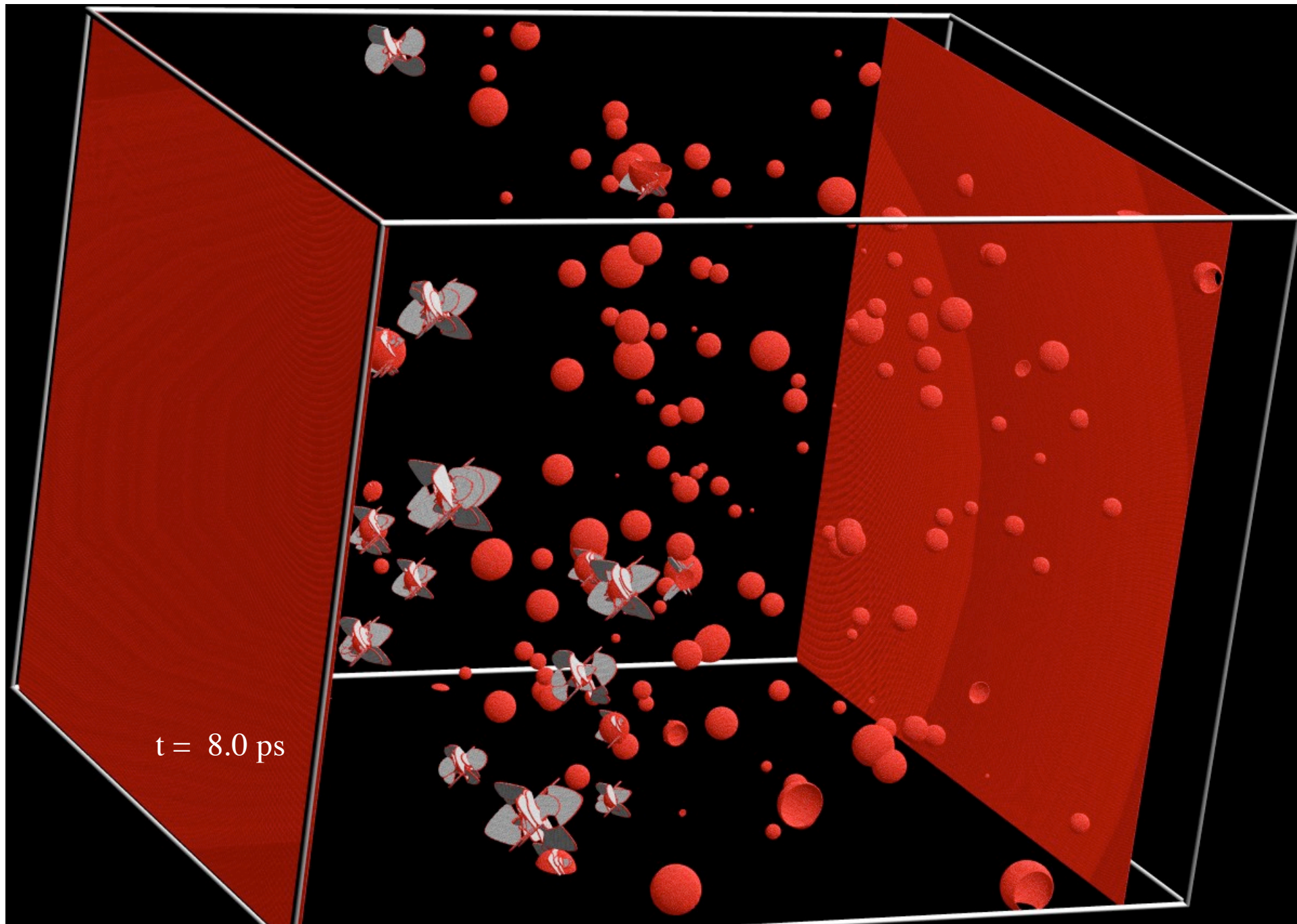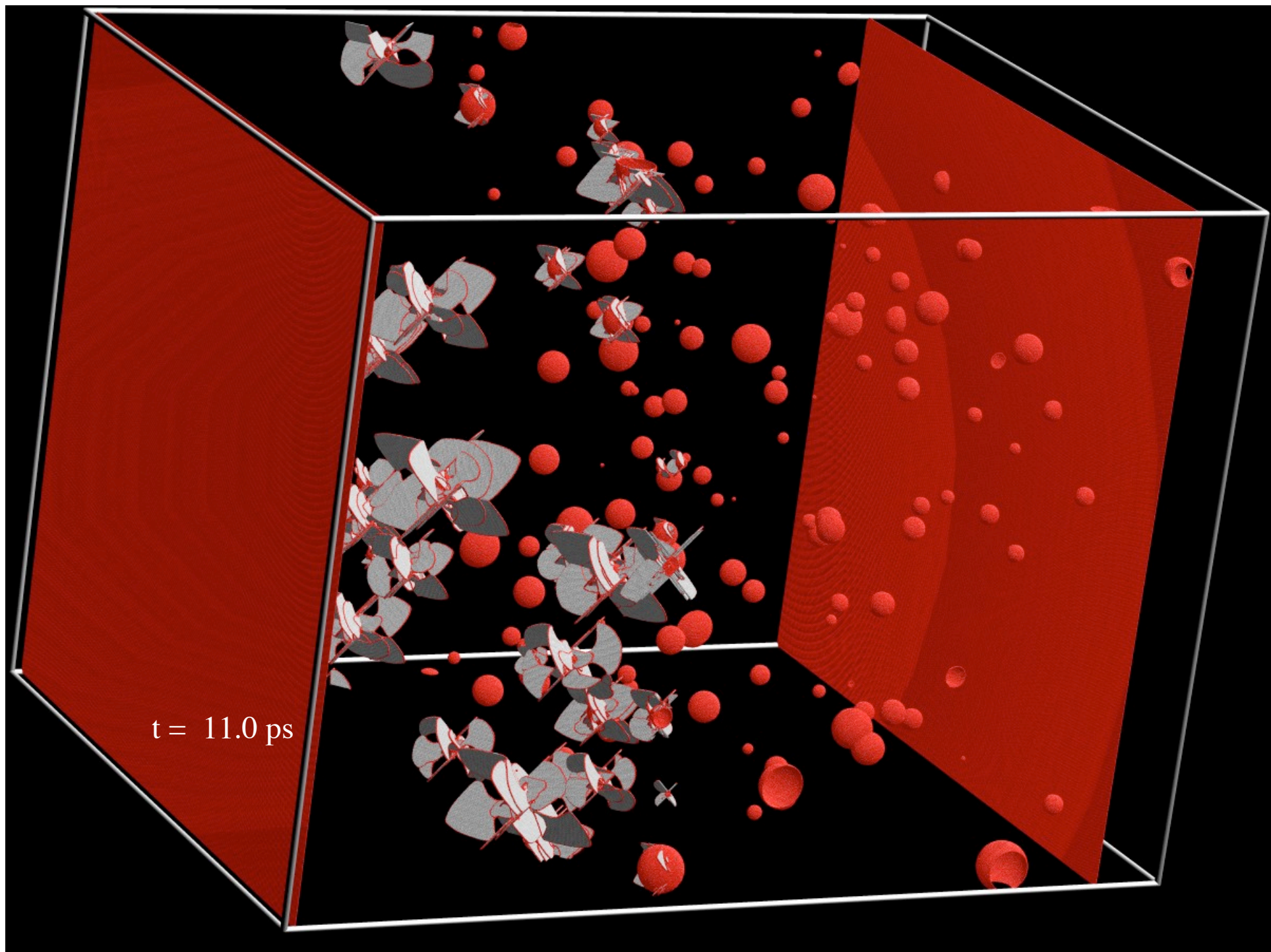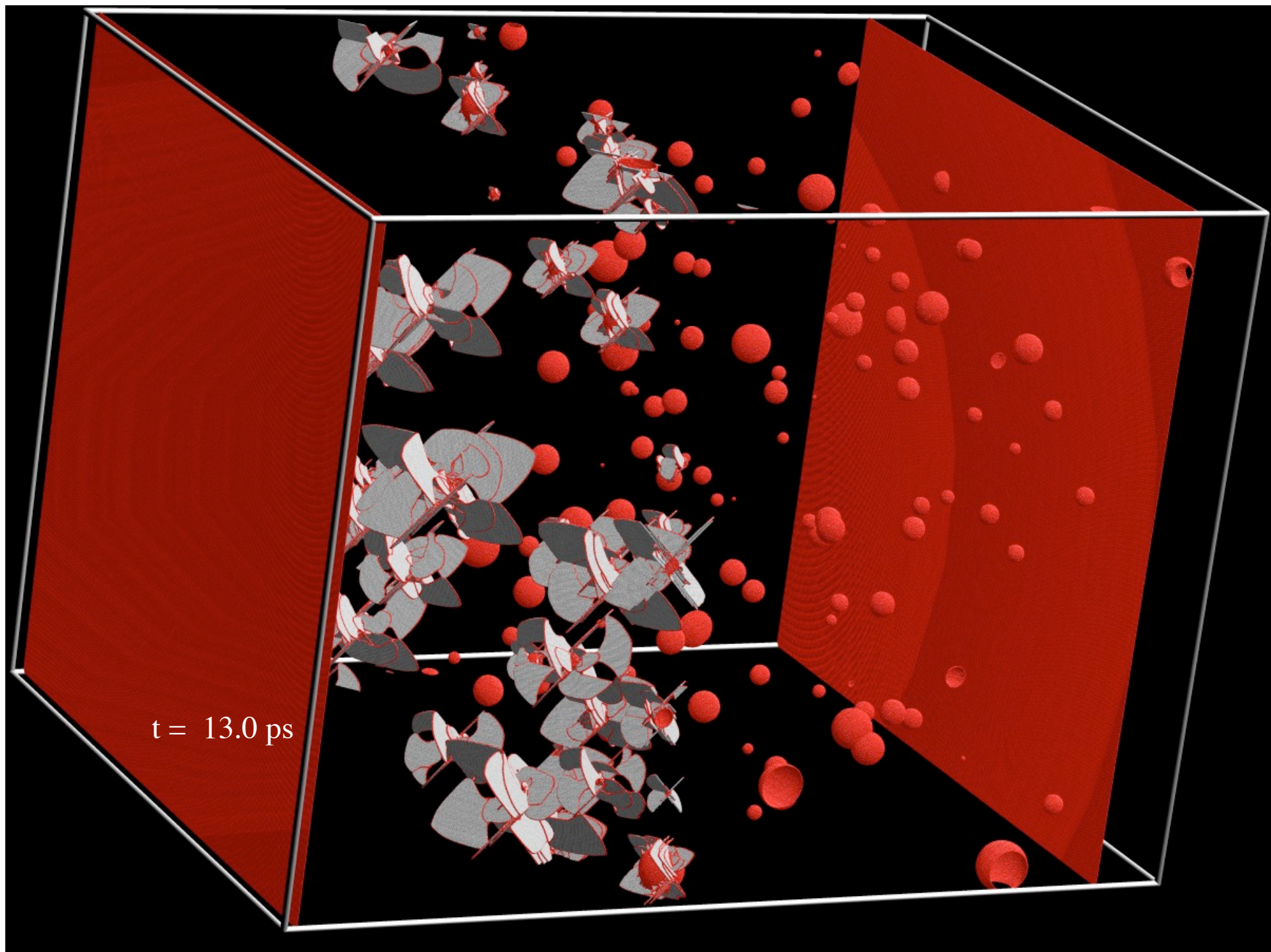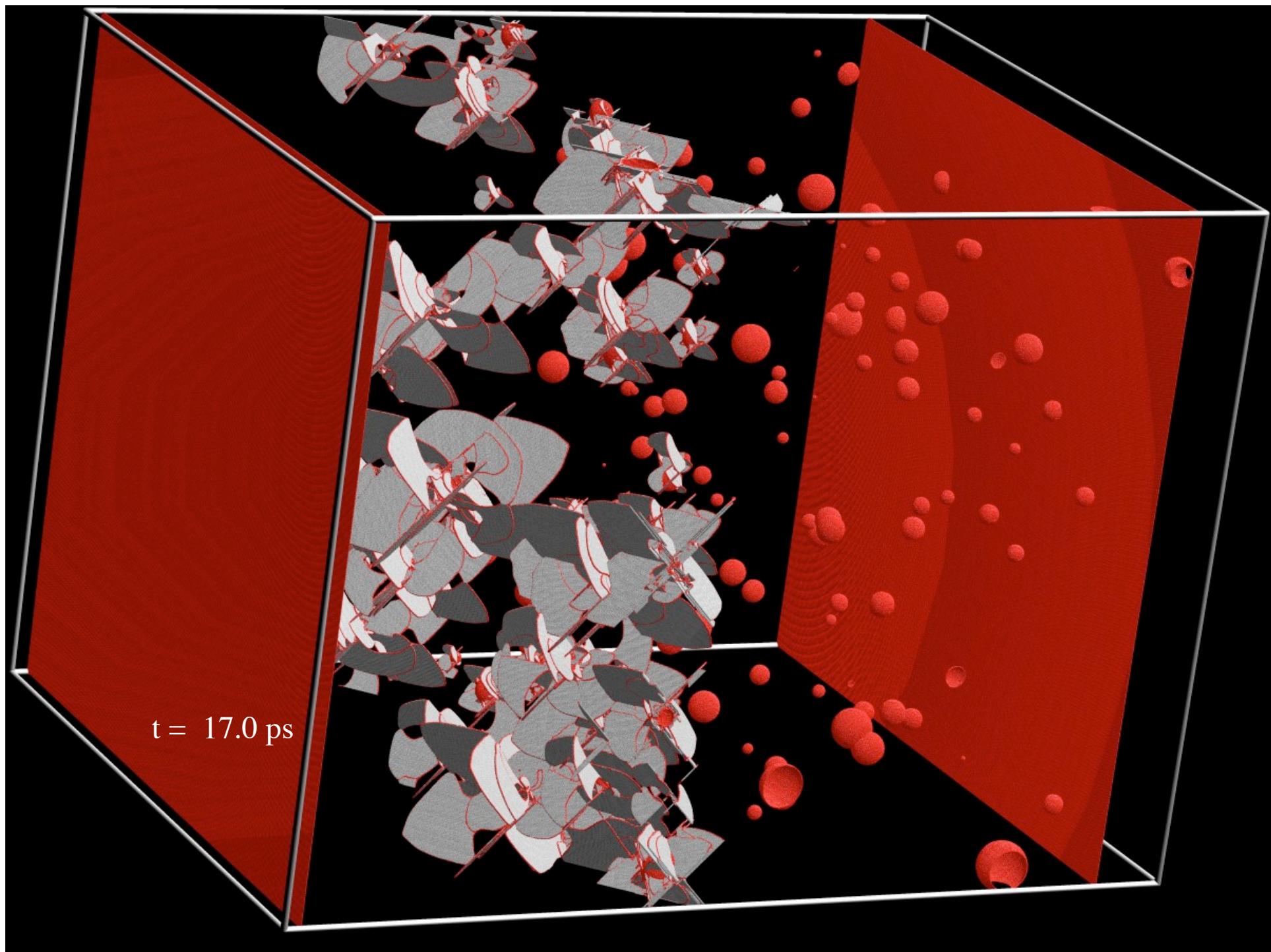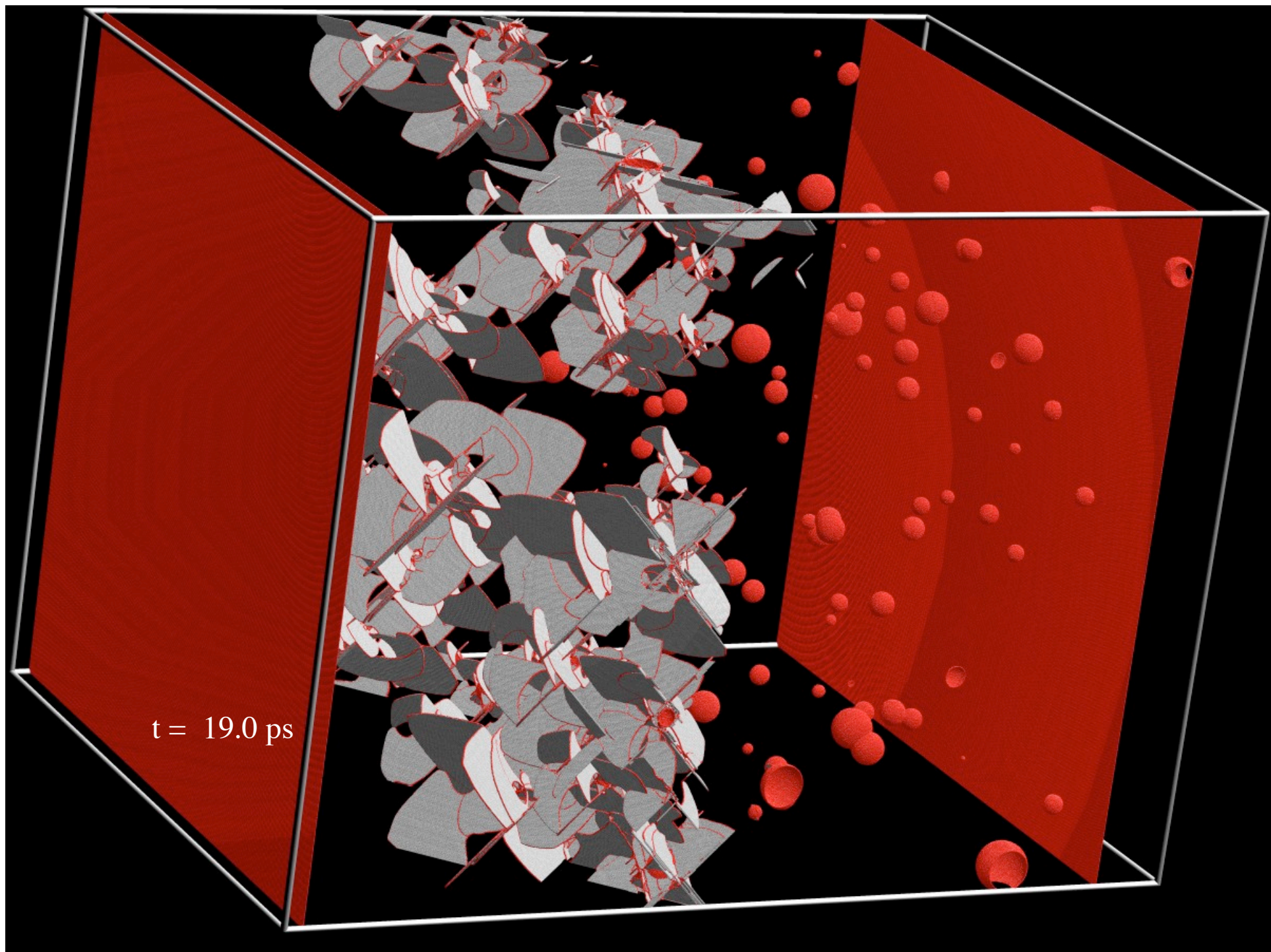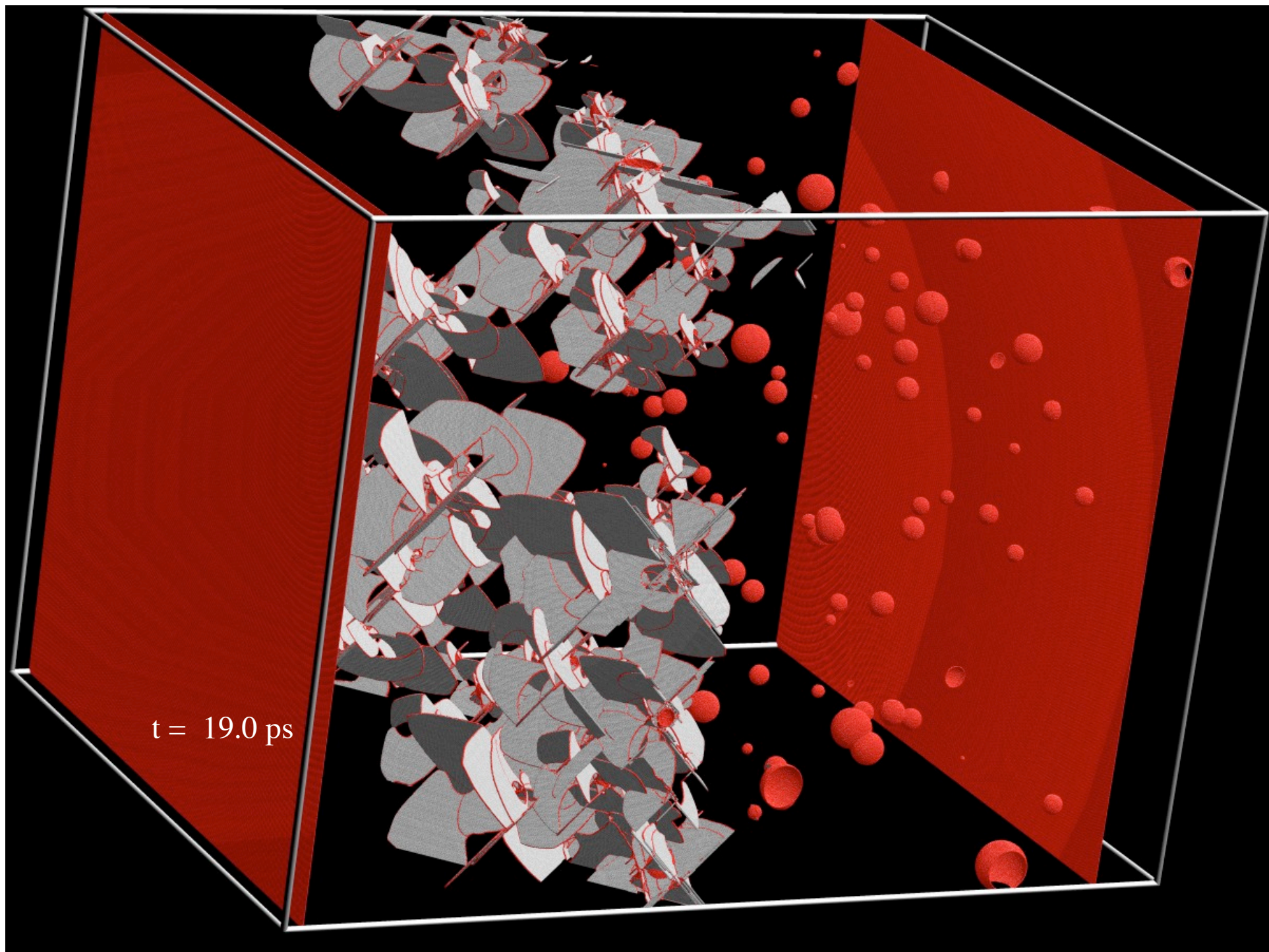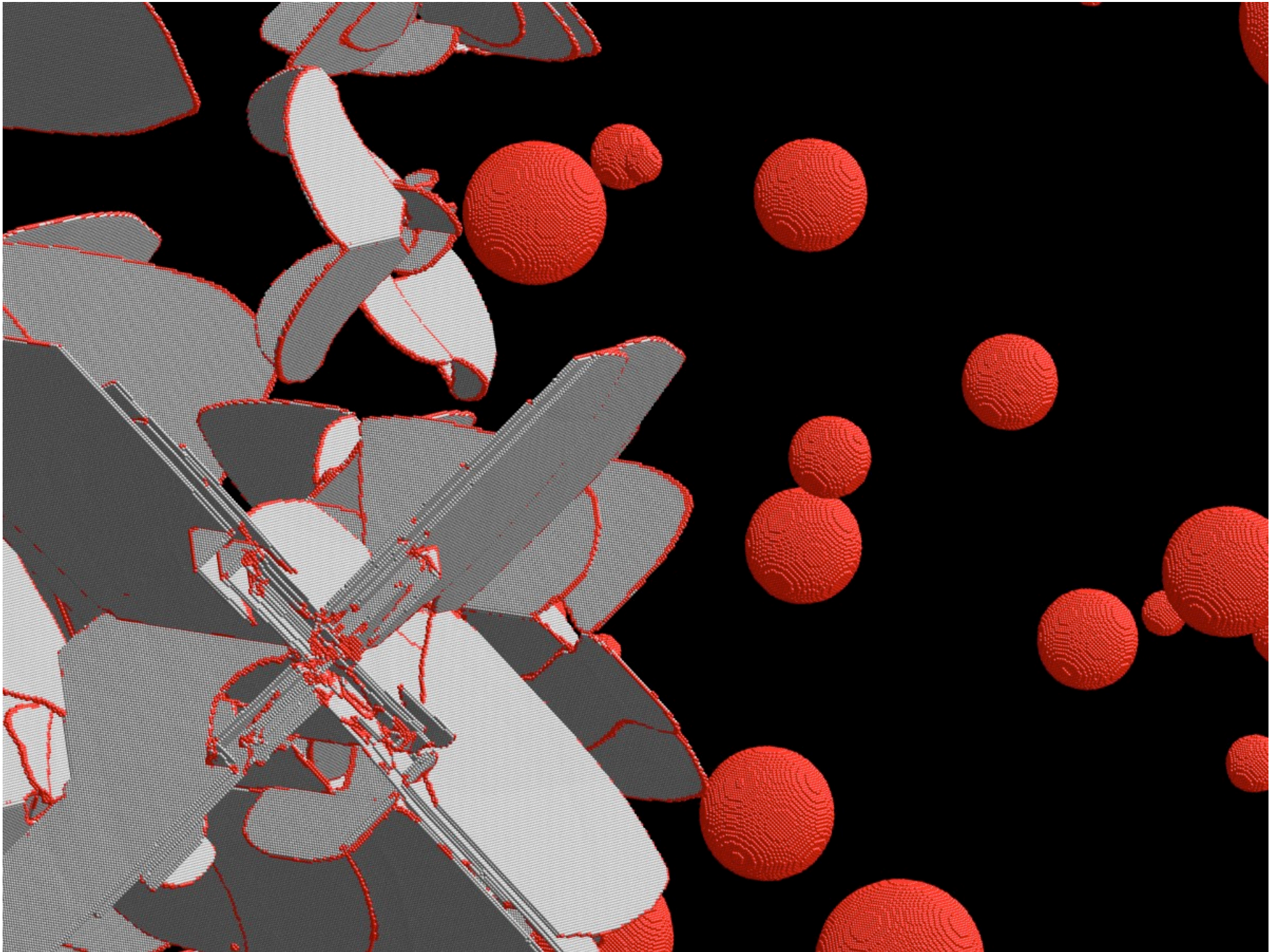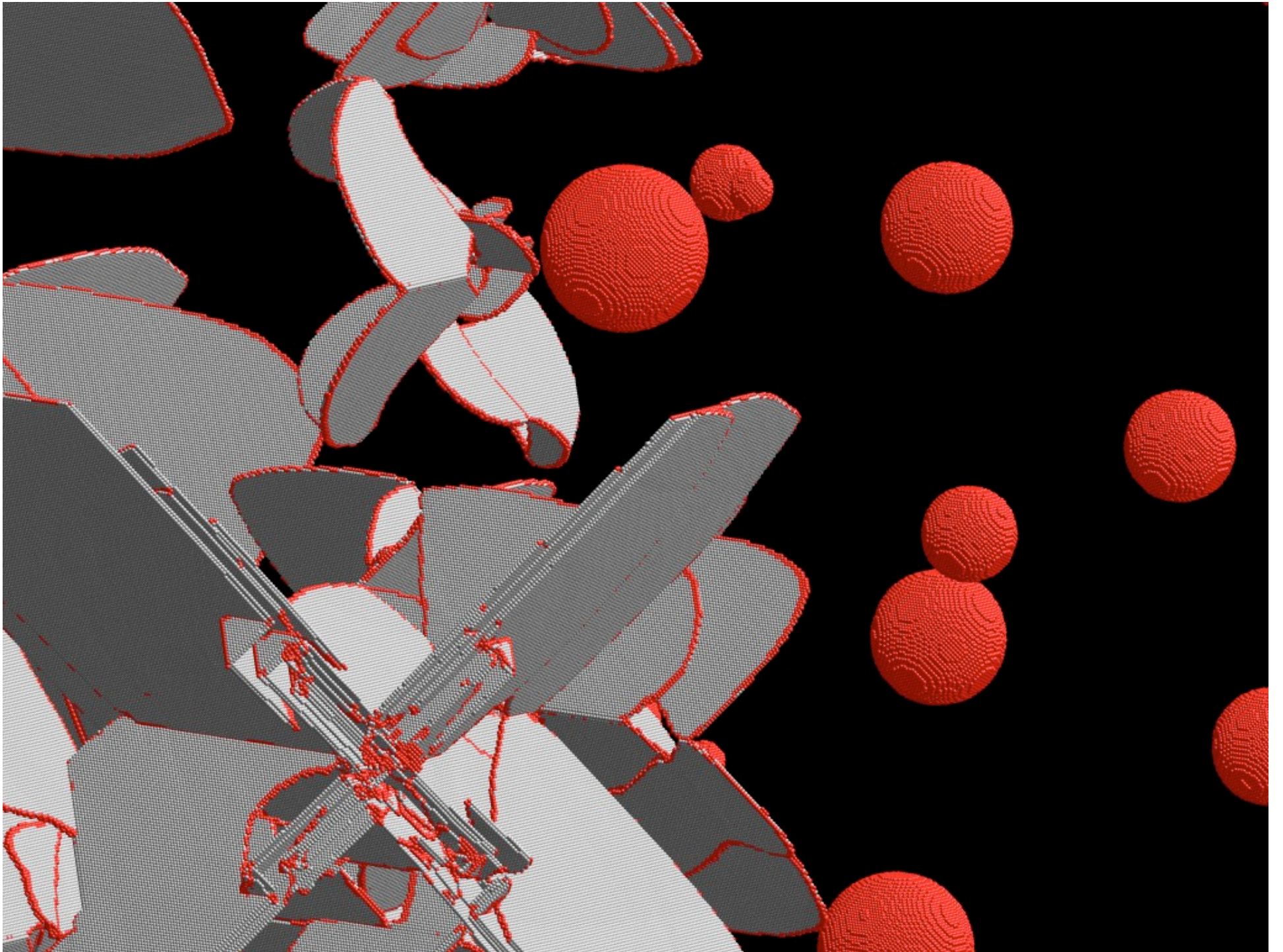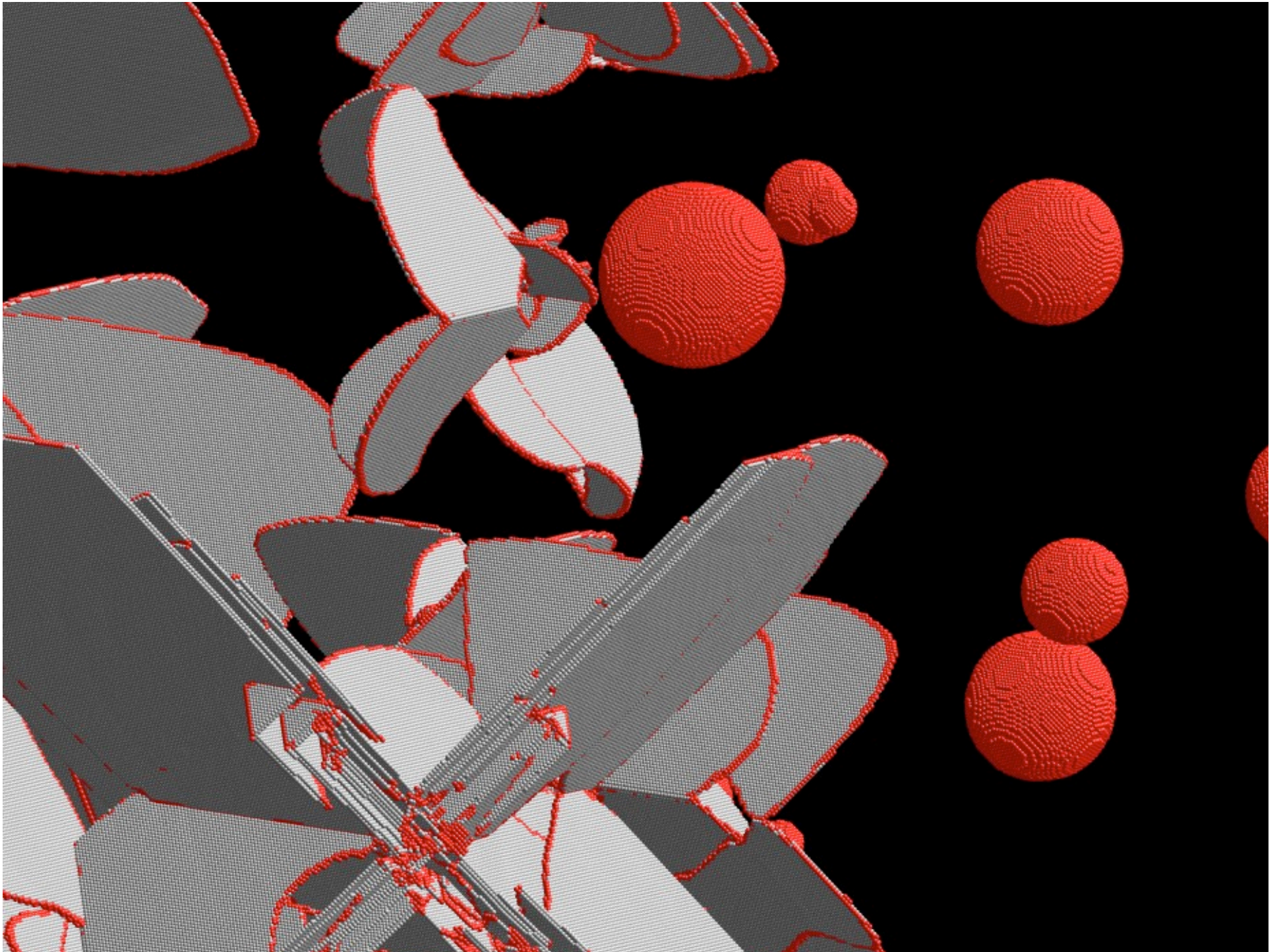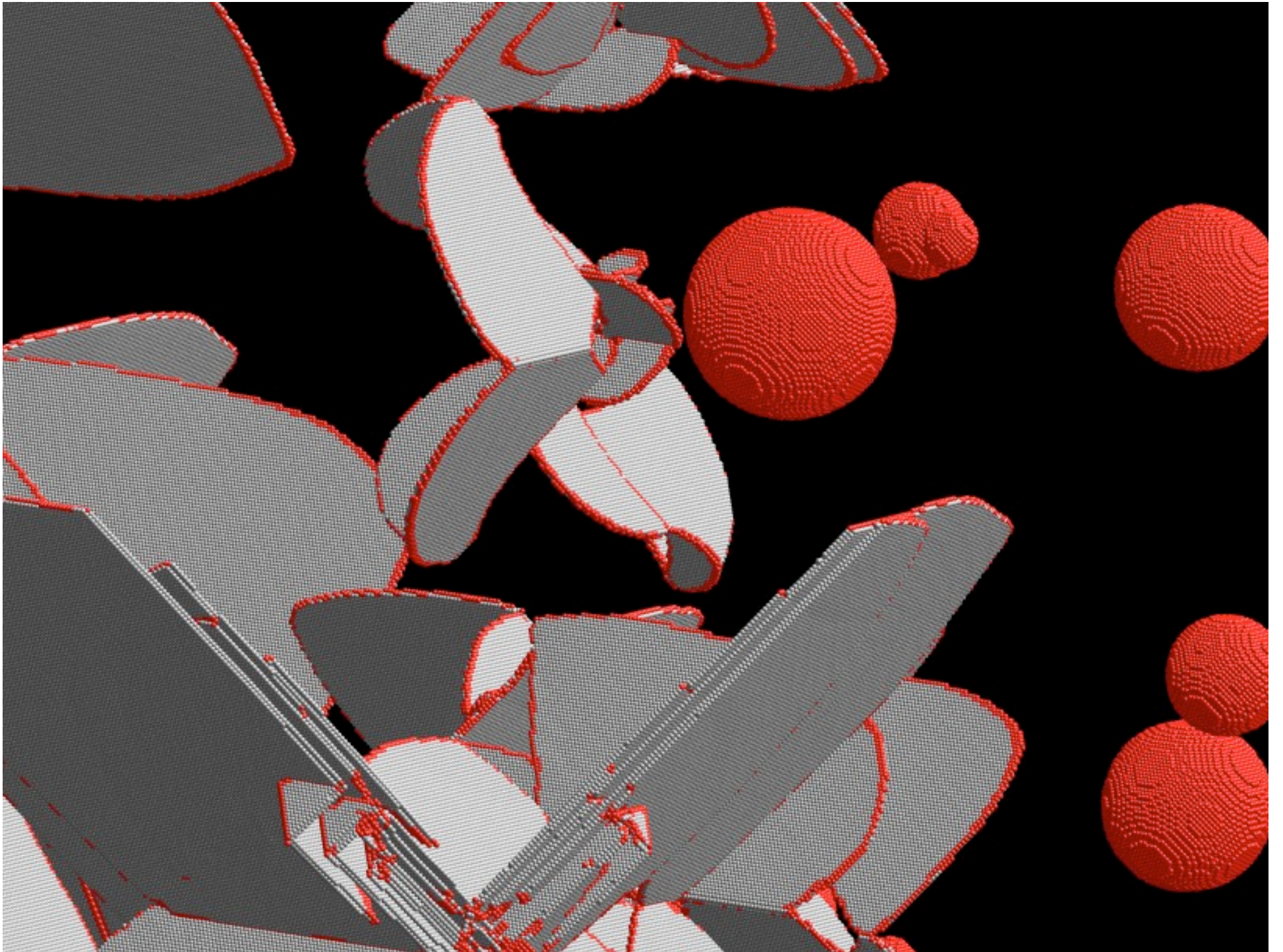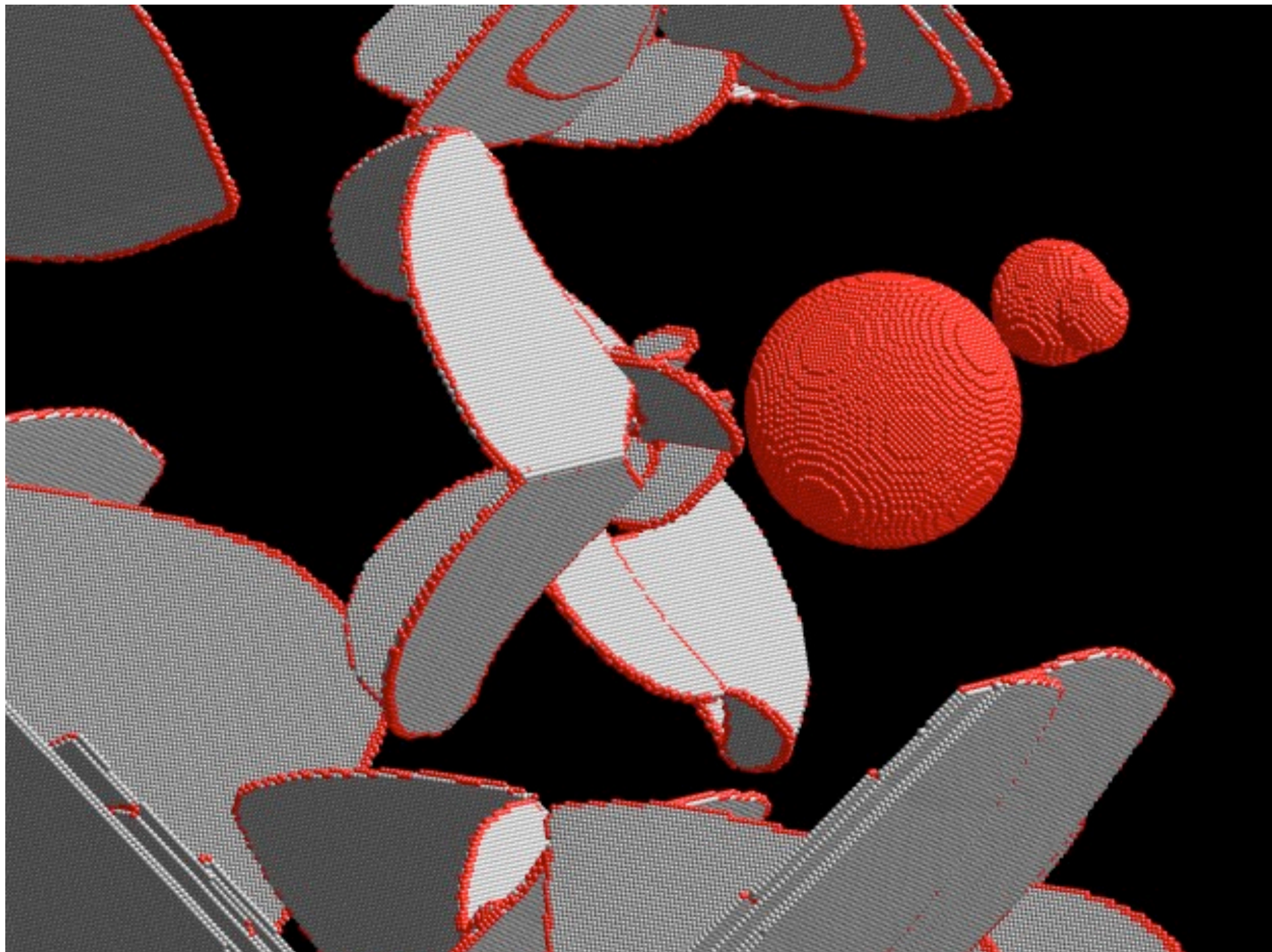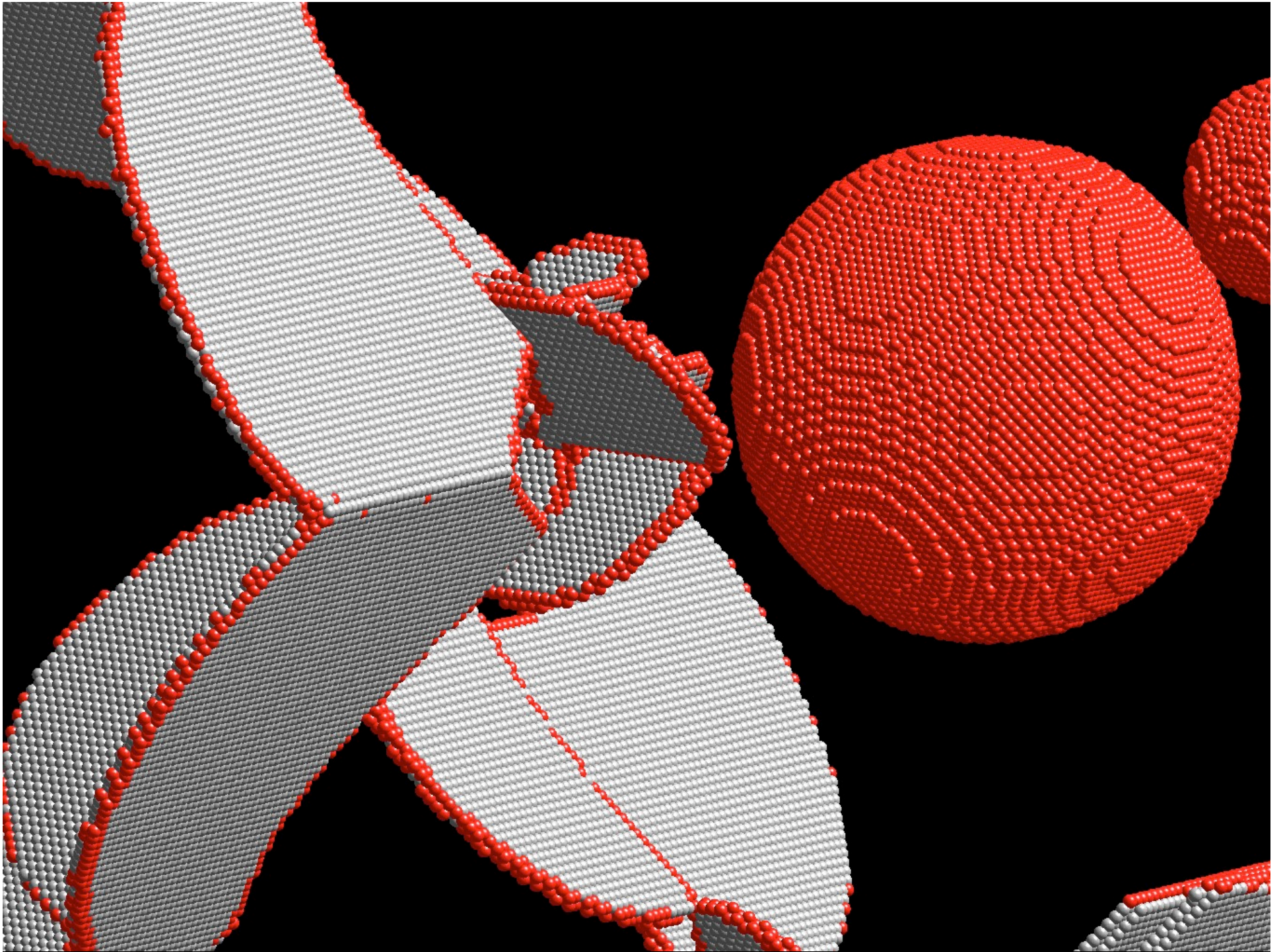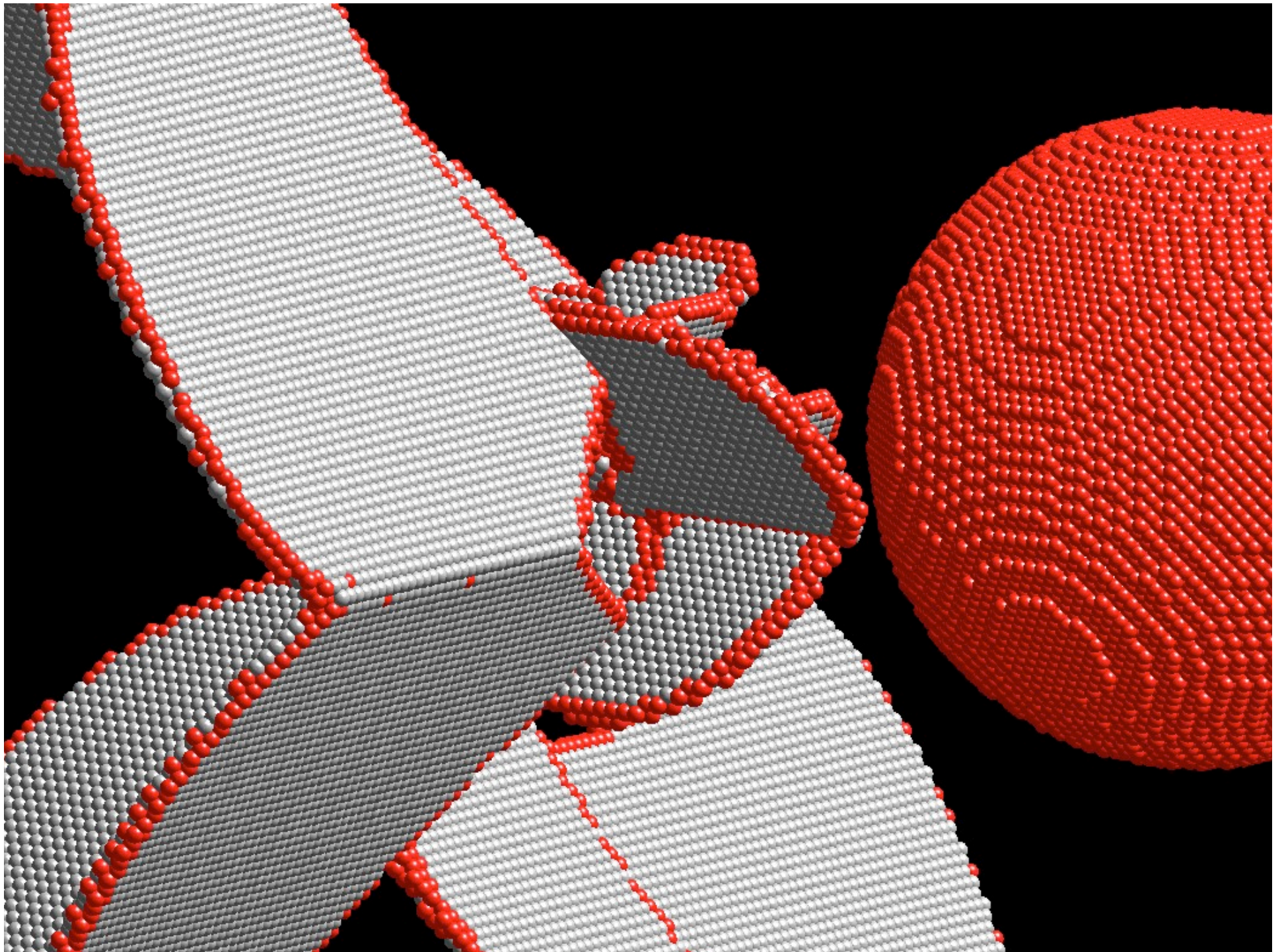
⟨100⟩ loading, u_p = 1 km/s,   t = 0 ps
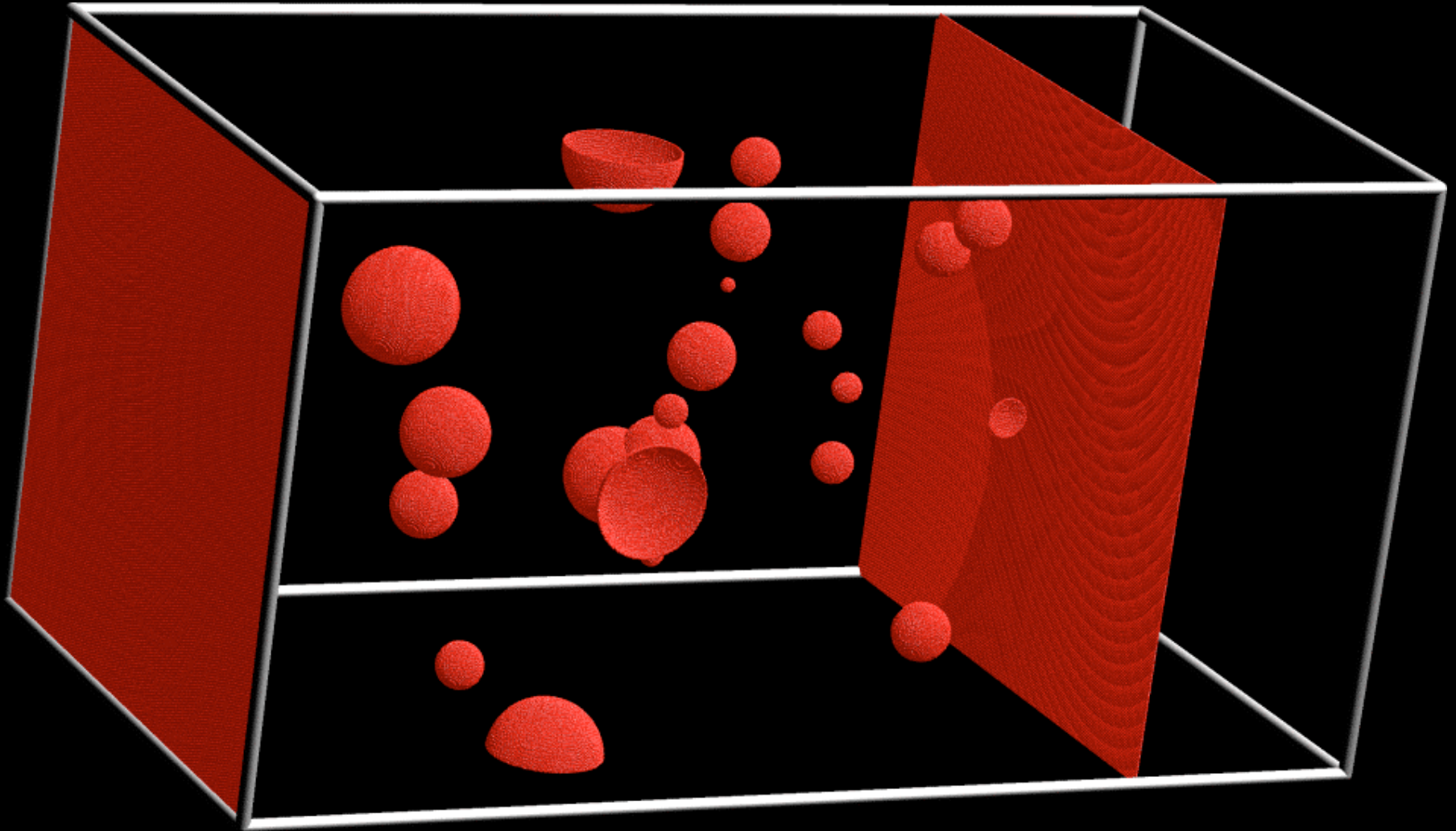
116 nm × 116 nm × 181 nm (1.41% porosity) ⇨ 202,872,066 atoms

$\langle 100 \rangle$ loading, u_p = 1 km/s, t = 10 ps
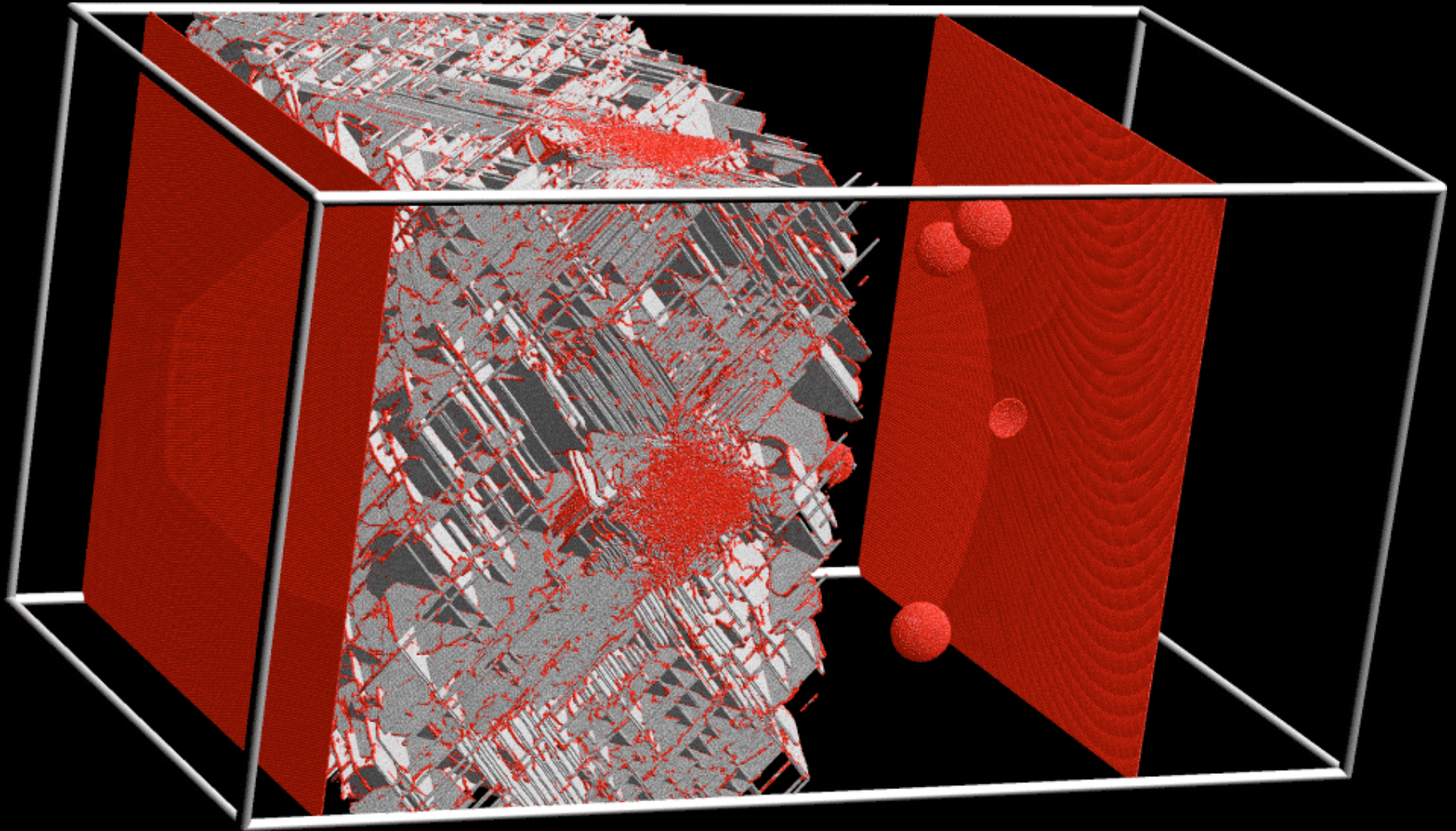
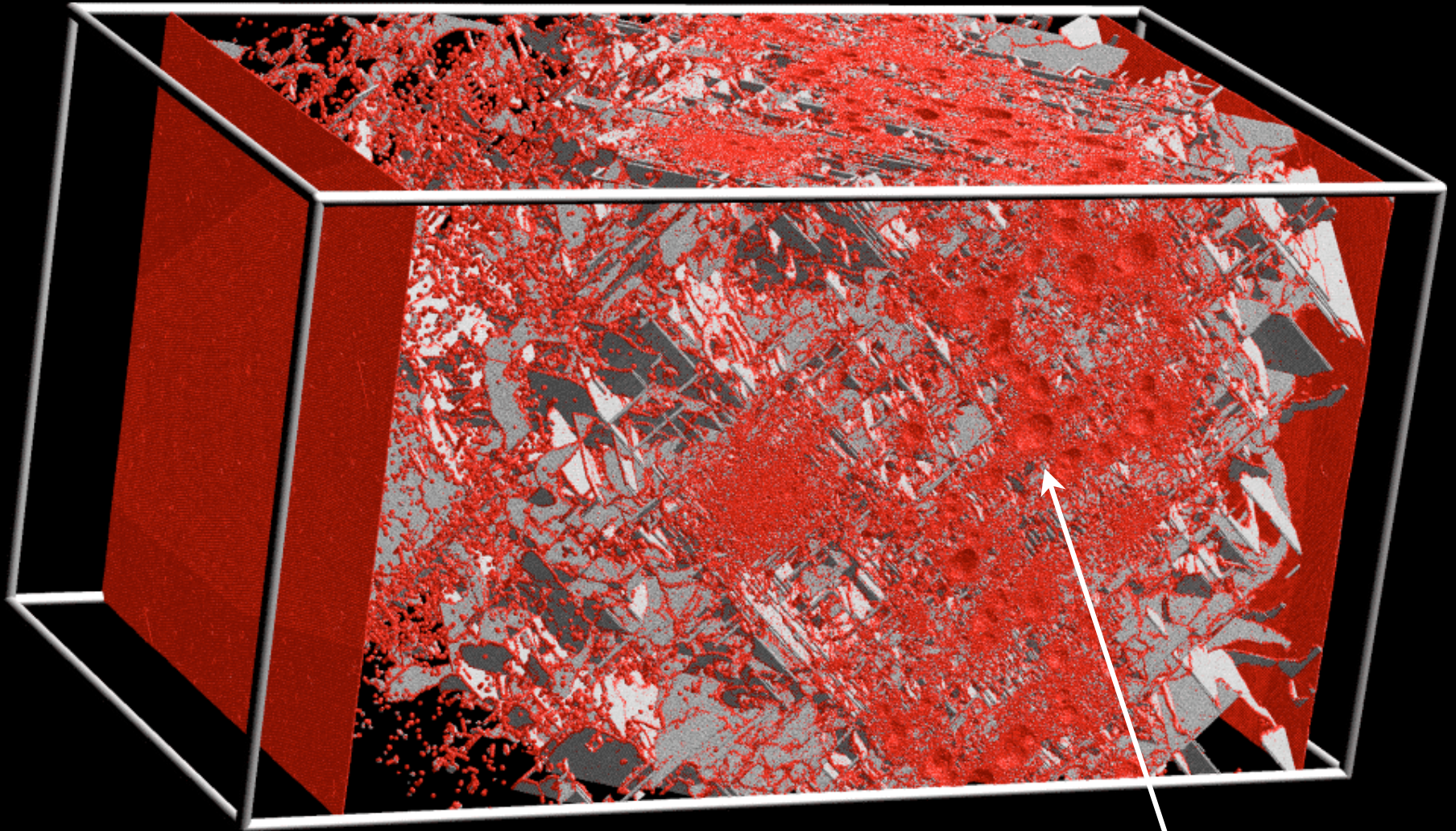$\langle 100 \rangle$ loading, $u_p = 1$ km/s,   t = 20 ps
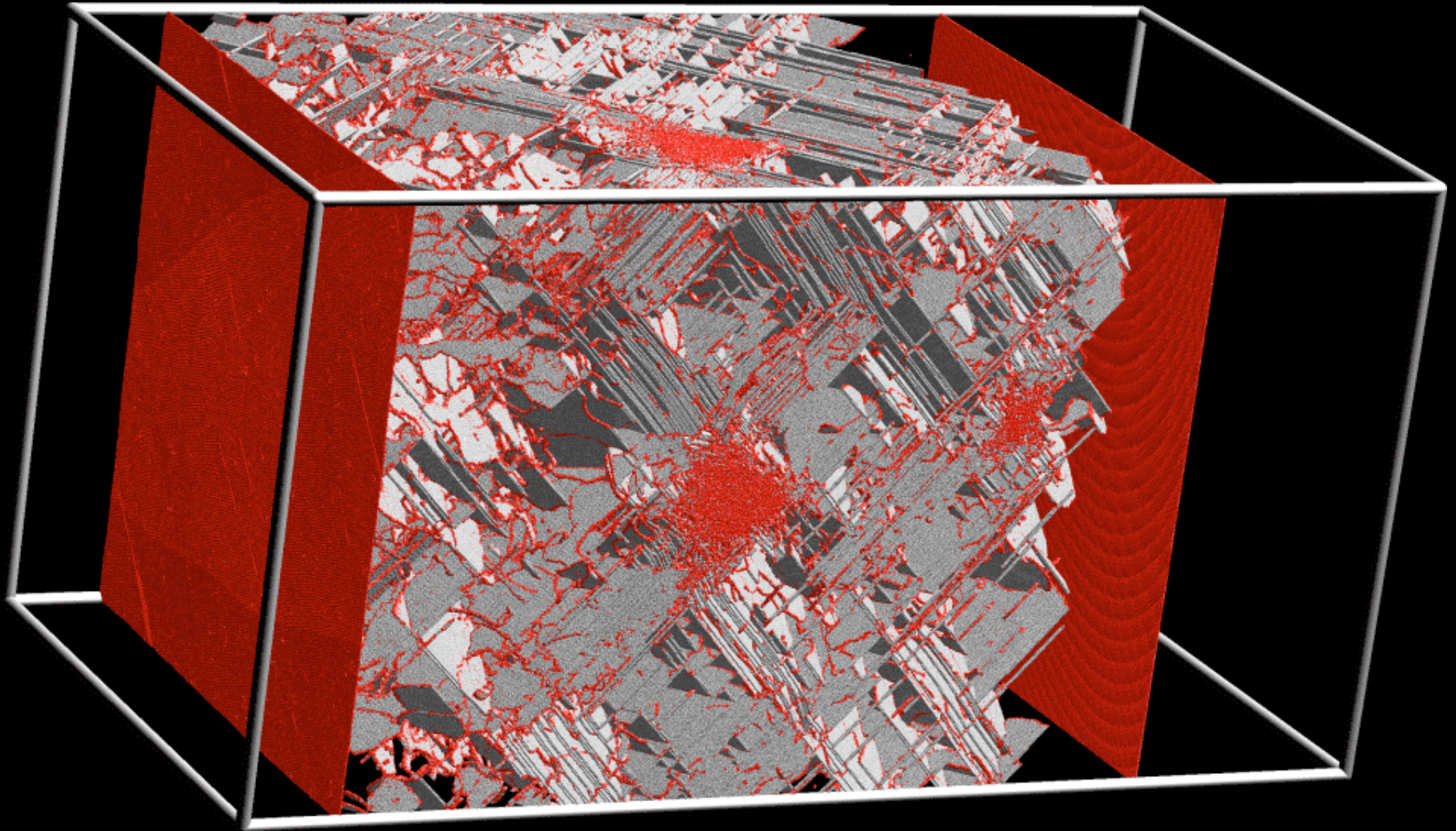
⟨100⟩ loading, u_p = 1 km/s,   t = 30 ps
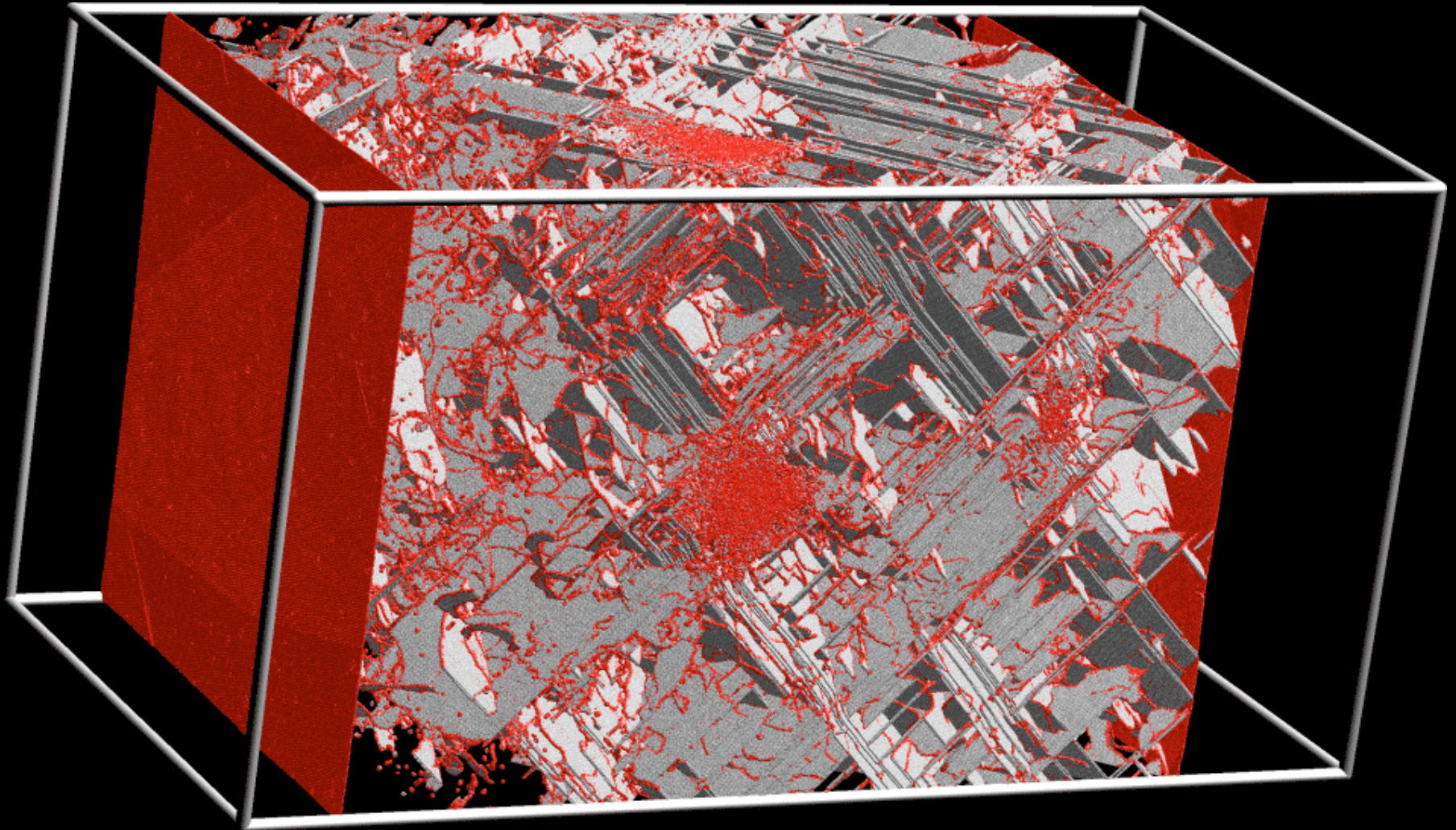
$\langle 100 \rangle$ loading, u_p = 1 km/s,   t = 40 ps
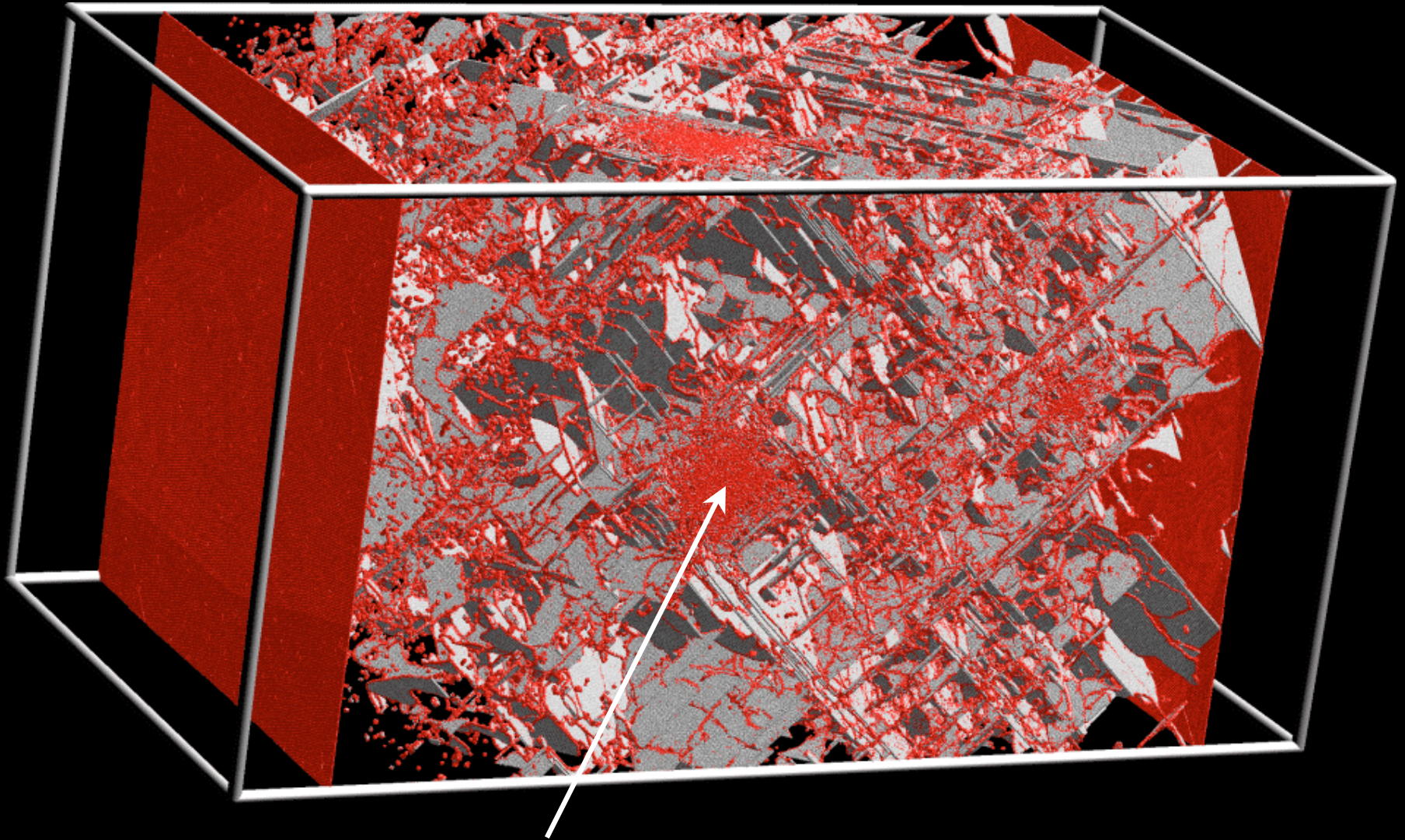
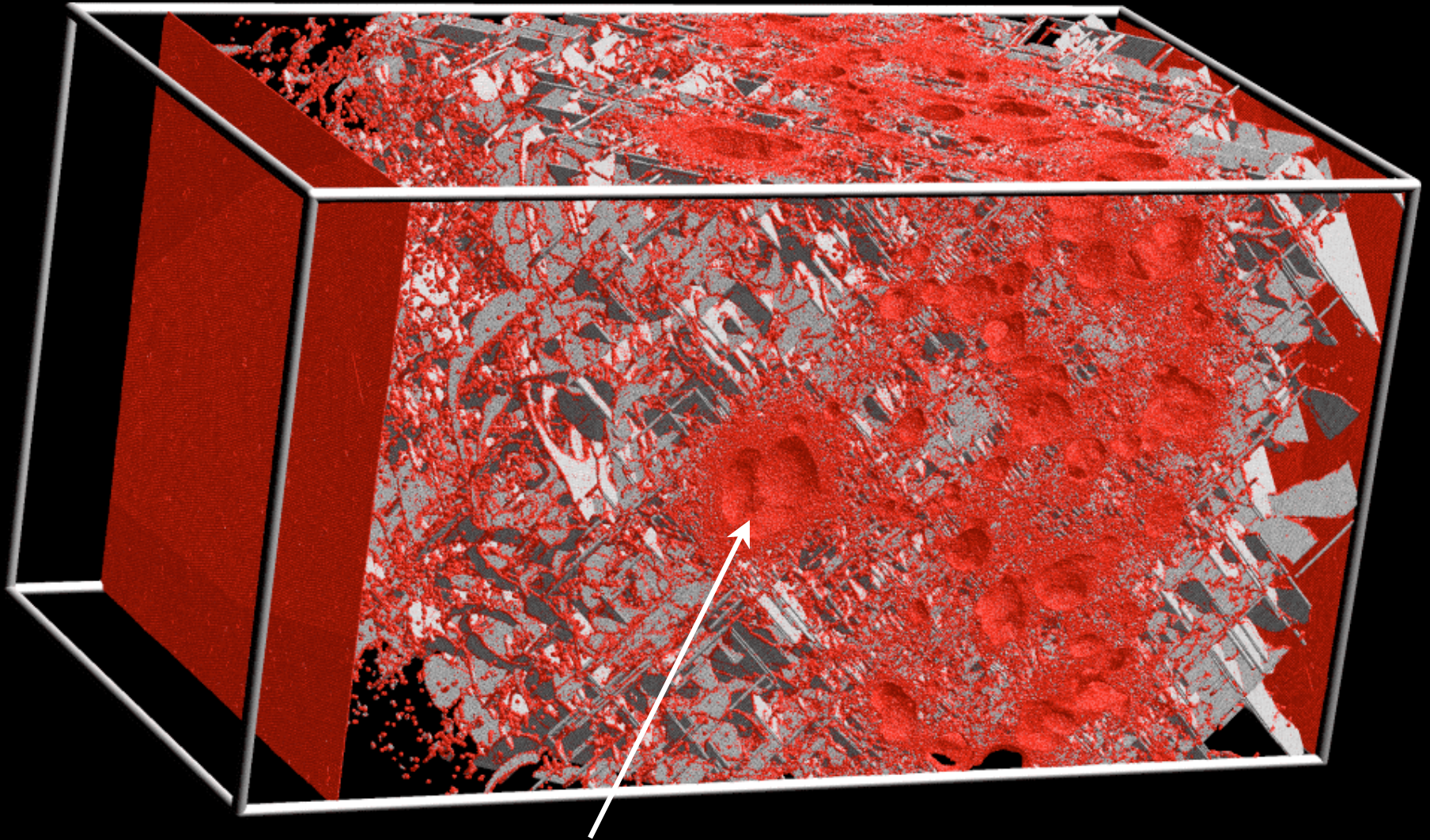Increased local dislocation density provides "memory" of void locations

⟨100⟩ loading, u_p = 1 km/s,   t = 50 ps

Nucleation of numerous small voids

$\langle 100 \rangle$ loading, u_p = 1 km/s, t = 60 ps

Re-opening of preexisting void

⟨100⟩ loading, u_p = 1 km/s,   t = 70 ps
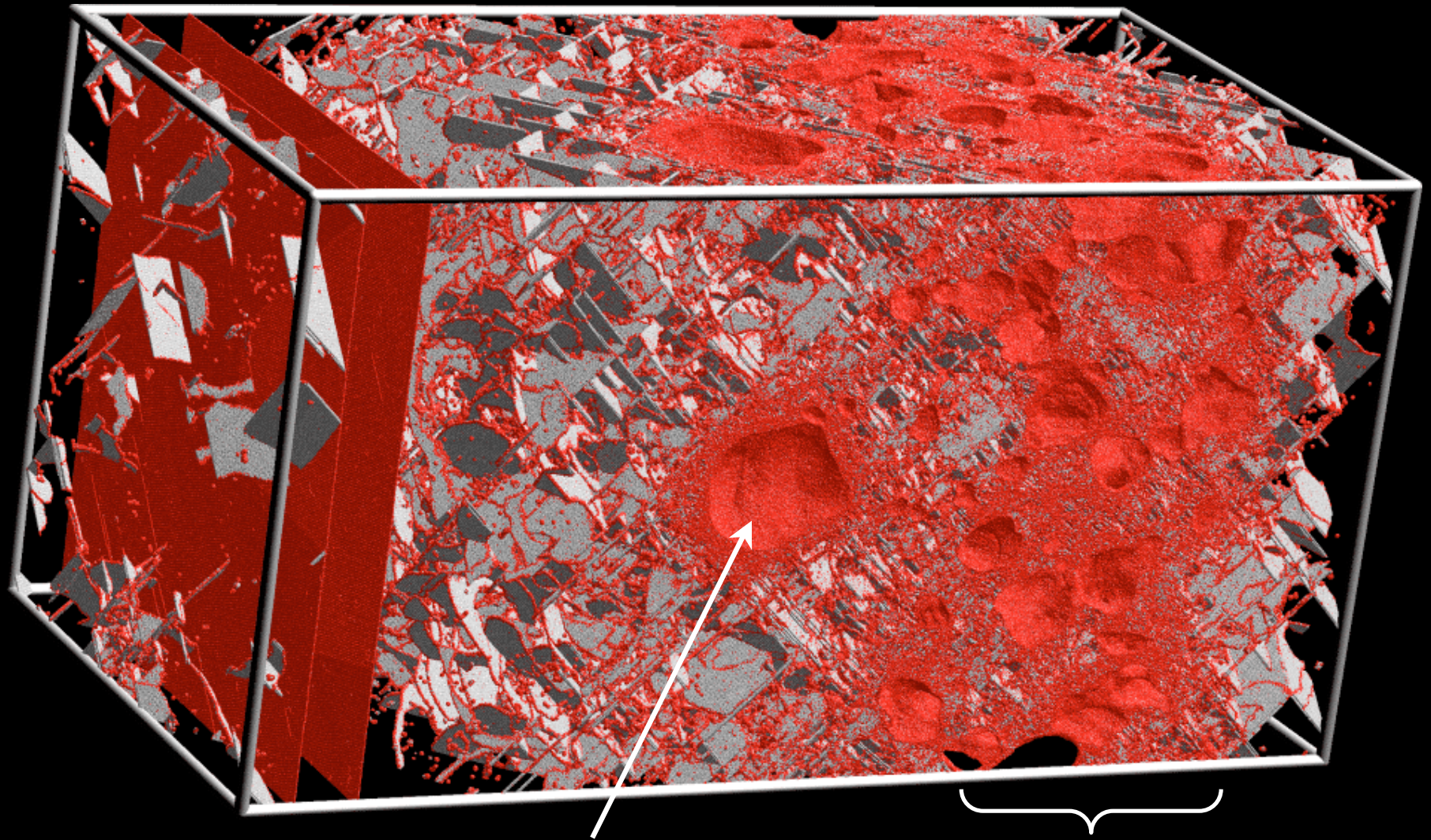
Re-opening of preexisting void

Linkup of voids in main spall zone
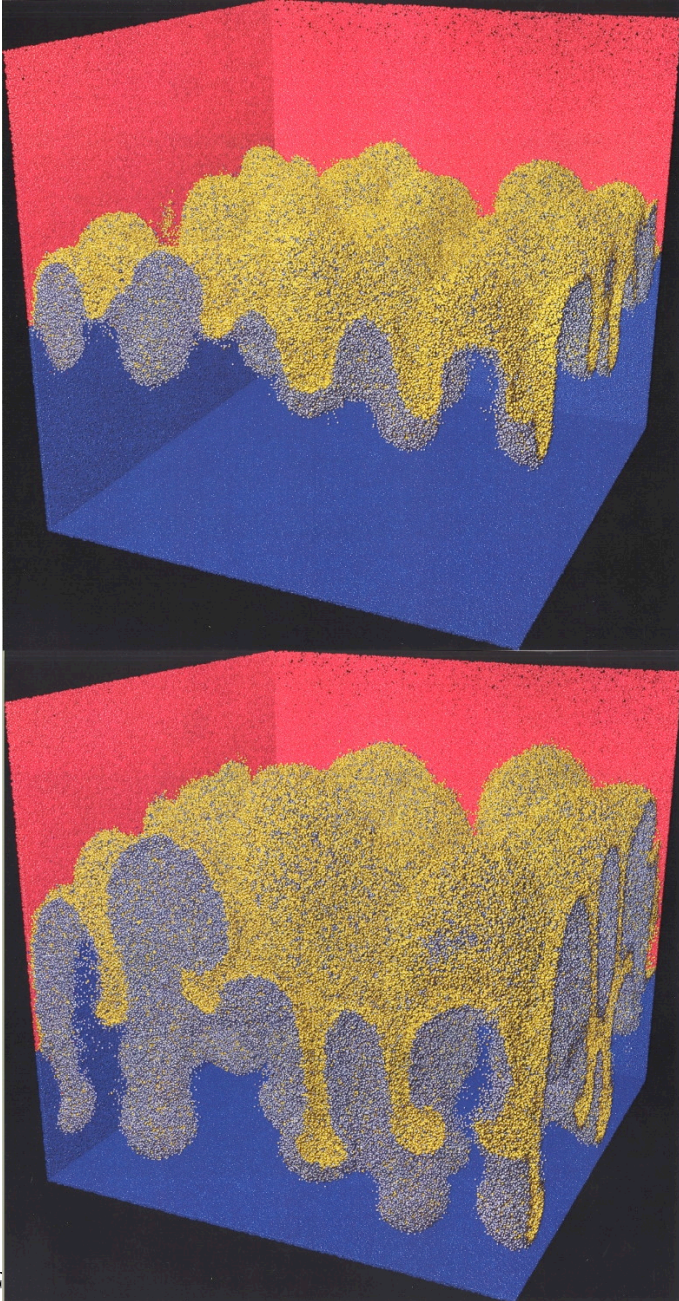
⟨100⟩ loading, u_p = 1 km/s, t = 80 ps
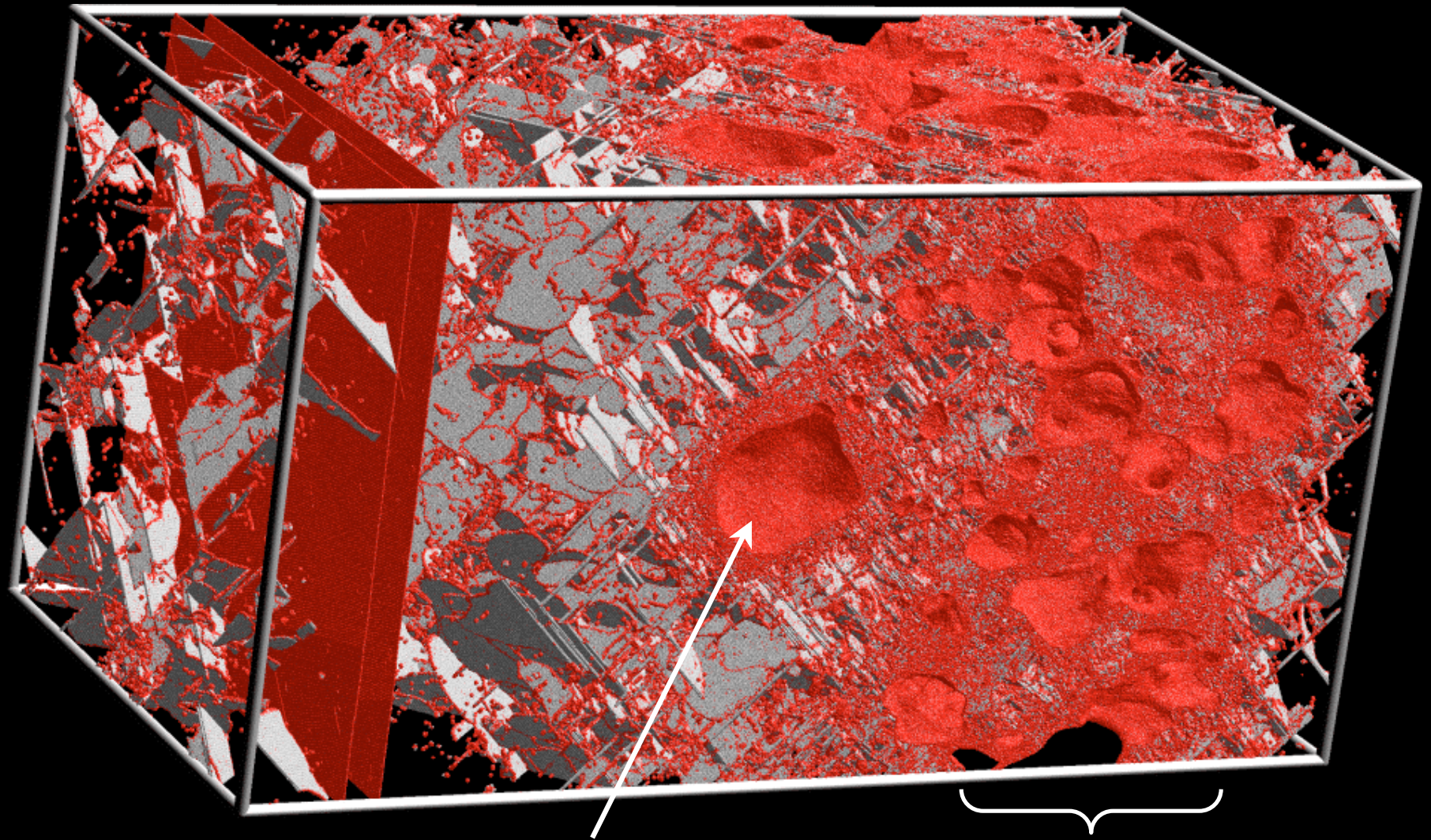
Re-opening of preexisting void
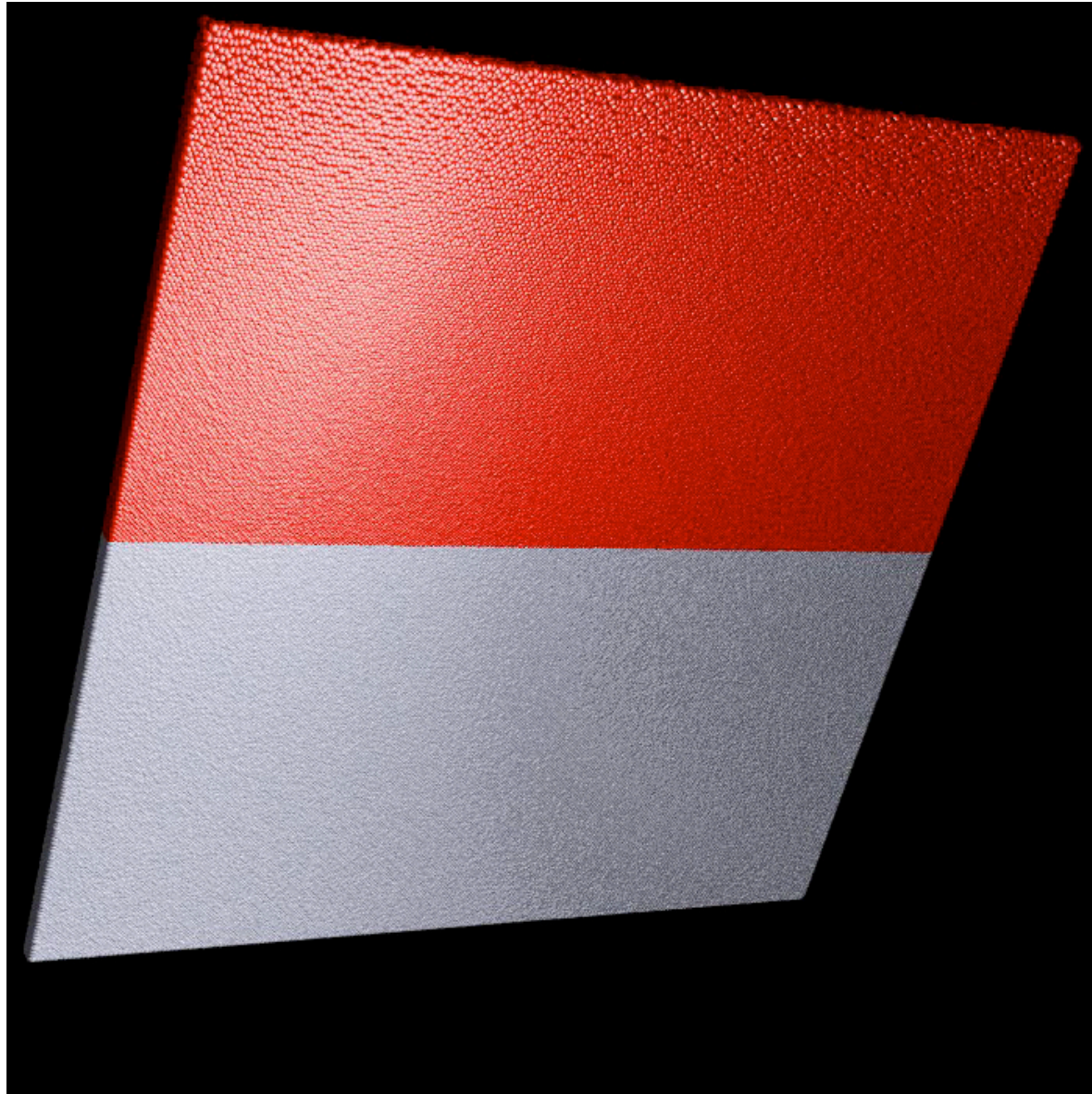
Linkup of voids in main spall zone

Raleigh-Taylor instability

Kadau et al, PNAS **101**, 5851 (2004)

100 million LJ atoms

A.F

Raleigh-Taylor instability

Kadau et al, PNAS **101**, 5851 (2004).

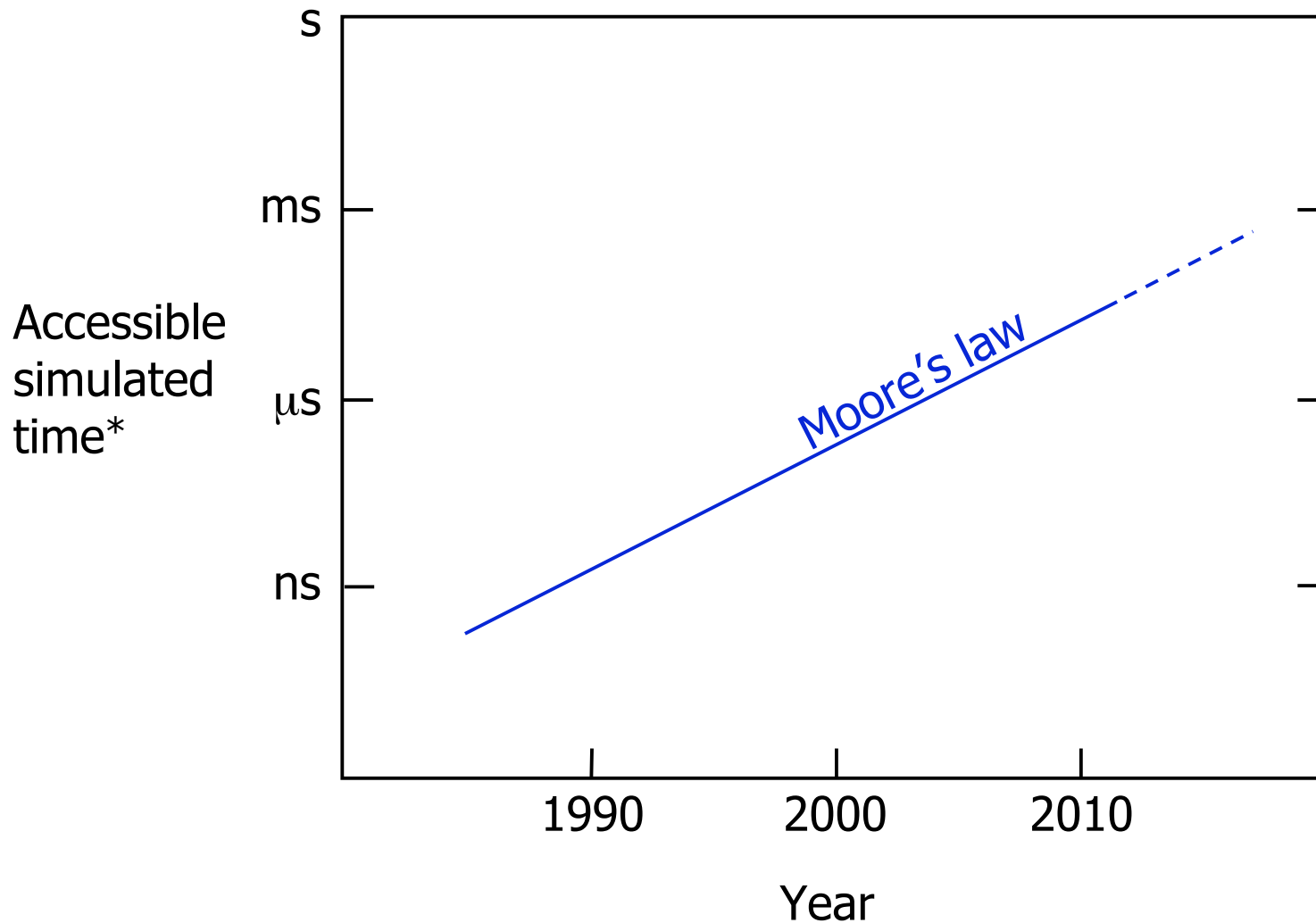*Los Alamos*

MD - achievable time scales

With fast empirical potential

nanoseconds

With first-principles forces (e.g., density functional theory)

few ps

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MD may never reach even one millisecond

* 1-week simulation of 1000-atom metal system, EAM potential

A.F. Voter, September, 2005 LAUR-05-8125

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