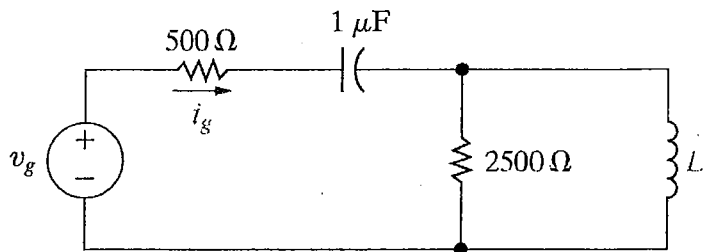


3. For the circuit to the right, $V_g = 20 \cos(2000t)$.

a) If $L = 1.25$ H, what is the complex power absorbed by the load (R and L in parallel)? (12)



$$Z_L = j\omega L = j(2000)(1.25) = j2500$$

$$Z_C = \frac{-j}{\omega C} = \frac{-j}{(2000)(10^{-6})} = -j500$$

$$Z_{R||L} = \frac{(2500)(j2500)}{2500 + j2500} = \frac{(2500)^2 \angle 90}{2500\sqrt{2} \angle 45} = \frac{2500}{\sqrt{2}} \angle 45 = 1250 + j1250$$

$$I_{LOAD} = \frac{V_g}{Z_{total}} = \frac{20}{(500 - j500) + (1250 + j1250)} = \frac{20}{1750 + j750}$$

$$= \frac{20 \angle 0}{1904 \angle 23.2} = 0.0105 \angle -23.2$$

$$S = \frac{|I|^2}{2} Z_{LOAD} = \frac{(0.0105)^2}{2} (1250 + j1250) = 0.0689 + j0.689 \text{ VA}$$

$$= 0.0974 \angle 45^\circ \text{ VA}$$

b) What value of L would maximize power transfer to the load? (8)

Norton transformation of source $I_N = (V_g) / (Z_{Th}) = \frac{20 \angle 0}{500\sqrt{2} \angle 45^\circ}$

$$Y_N = \frac{1}{Z_m} = \frac{1}{500 - j500} = \frac{1}{500\sqrt{2} \angle -45^\circ} = \frac{\sqrt{2}}{1000} \angle 45^\circ = 0.0283 \angle 45^\circ \text{ A}$$

$$= \frac{1}{1000} (1 + j) =$$

$$Y_{LOAD} = \frac{1}{R} + \frac{1}{j\omega L} = \frac{1}{R} - \frac{j}{\omega L}$$

$$P = \frac{|I|^2 R}{2} \quad |I_R| = \left| \frac{Y_R}{G + jB_L + Y_N} \right| \quad \text{max when } jB_L = -jB_N$$

$$\frac{1}{\omega L} = \frac{1}{1000} \Rightarrow \underline{\underline{L = 0.5}}$$

To maximize P, maximize $|I_R|$

End of Exam