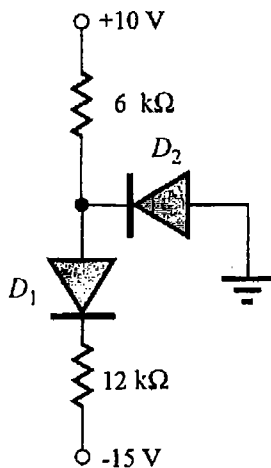
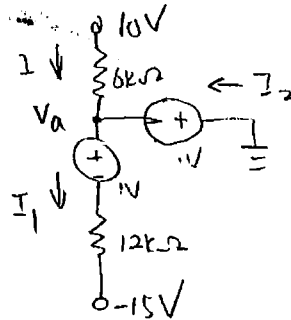


1. (12 pts) Find the Q-point for the diodes D_1 and D_2 shown in the figure below using the constant voltage drop (CVD) model with $V_{on} = 1$ V. Give answers for **BOTH** diodes.



Assume both diodes are ON.



$$V_a = -V_{on} = -1V$$

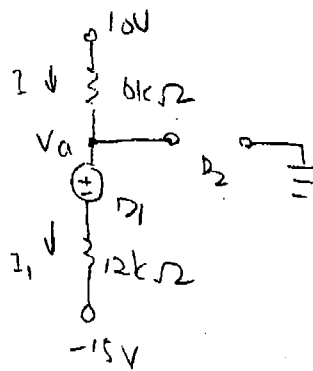
$$I = \frac{10V - (-1V)}{6k\Omega} = 1.83mA$$

$$I_1 = \frac{(-1V - (-15V))}{12k\Omega} = 1.08mA$$

$$I_2 = I - I_1 = -0.75mA \approx 0$$

Inconsistent with D_2 ON

Thus D_1 ON - D_2 OFF



$$I = I_1 = \frac{10V - (-1V)}{(6 + 12)k\Omega} = 1.33mA$$

$$V_a = 10V - IR = 10 - 1.33mA \cdot 6k\Omega = 2V$$

$$V_{D2} = -V_a = -2V$$

Q-pt for D_1 (1.33mA, 1V)

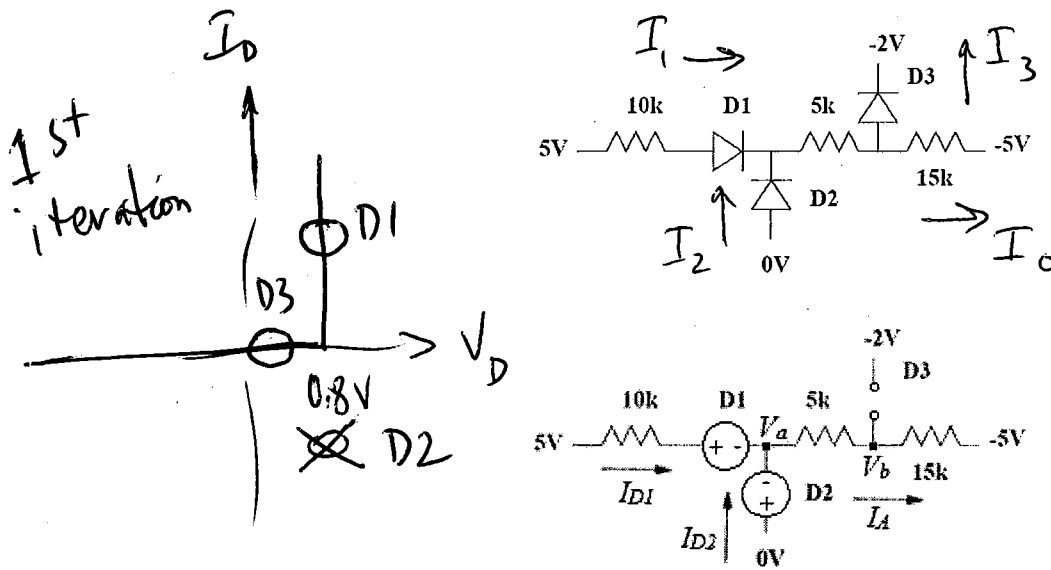
Q-pt for D_2 (0A, -2V)

Check $I_{D1} > 0$, $V_a = V_{on}$, consistent with D_1 ON

$I_{D2} = 0$, $V_{D2} = -2V < V_{on}$, consistent with D_2 OFF

3. (25 points) In the following circuit, use the constant voltage diode model with a threshold (turn-on) voltage of 0.8 V. Assume the diodes **D₁** and **D₂** are on and the diode **D₃** is off.

- (5 pt) Calculate the voltage across each diode.
- (5 pt) Calculate the current through each diode.
- (5 pt) Check your assumptions for D₁ -- are they correct? Why or why not?
- (5 pt) Check your assumptions for D₂ -- are they correct? Why or why not?
- (5 pt) Check your assumptions for D₃ -- are they correct? Why or why not?



According to the assumption: $V_{D1} = 0.8\text{ V}$, $V_{D2} = 0.8\text{ V}$, $I_{D3} = 0$.

$$V_a = -0.8\text{ V}, I_{D1} = \frac{5\text{ V} - 0.8\text{ V} - (-0.8\text{ V})}{10\text{ k}\Omega} = 0.50\text{ mA}.$$

$$I_A = \frac{0\text{ V} - 0.8\text{ V} - (-5\text{ V})}{15\text{ k}\Omega + 5\text{ k}\Omega} = 0.21\text{ mA}.$$

$$I_{D2} = I_A - I_{D1} = -0.29\text{ mA}$$

$$V_b = V_a - 5\text{ k}\Omega \cdot 0.21\text{ mA} = -1.85\text{ V}$$

$$V_{D3} = V_b - (-2\text{ V}) = 0.15\text{ V}$$

D₁: $V_{D1} = 0.8\text{ V}$, $I_{D1} = 0.50\text{ mA}$. $I_{D1} > 0$, assumption for D₁ being on is correct.

D₂: $V_{D2} = 0.8\text{ V}$, $I_{D2} = -0.29\text{ mA}$. $I_{D2} < 0$, assumption for D₂ being on is NOT correct.

D₃: $I_{D3} = 0$, $V_{D3} = 0.15\text{ V} < 0.8\text{ V}$. $V_{D3} < V_{on}$, assumption for D₃ being off is correct. *if D₂ is ON as assumed.*

With D2 off, D3 on, D1 on:

$$V_b = -5V + I_o * 15k\Omega, \quad I_o = \frac{5V - V_{on} - (-5V)}{10k + 5k + 15k} = \frac{9.2V}{30k\Omega}$$

$$= -5V + \frac{9.2V}{30k\Omega} * 15k\Omega = 0.307mA$$

$$= -5V + 4.6V = -0.4V$$

$$V_{D3} = -0.4 - (-2V) = 1.6V > V_{on} \Rightarrow \text{not OFF} \quad D3$$

With D2 off and D3 on (and D1 still on)

$$V_b = -2V + V_{on} = -1.2V$$

$$V_a = 5V - V_{on} = I_1 (10k\Omega)$$

$$= 5V - 0.8V - \frac{5.4V}{15k\Omega} * 10k\Omega$$

$$= 5V - 0.8V - 3.6V = 0.6V$$

for

$$I_1 = \frac{5V - V_{on} - V_b}{15k\Omega} = \frac{5.4V}{15k\Omega}$$

$$= 0.36mA$$

$$V_{D2} = 0 - 0.6V = -0.6V \Rightarrow \text{OFF}$$

$$I_3 = I_1 - \frac{V_b - (-5V)}{15k\Omega} = 0.36mA - \frac{3.8V}{15k\Omega} = 0.36mA - 0.253mA$$

$$= 0.107mA > 0$$

$$D1, \text{on} \quad V_{D1} = 0.8V \quad I_1 = 0.36mA$$

$$D2, \text{off} \quad V_{D2} = -0.6V \quad I_2 = 0$$

$$D3, \text{on} \quad V_{D3} = 0.8V \quad I_3 = 0.107mA$$

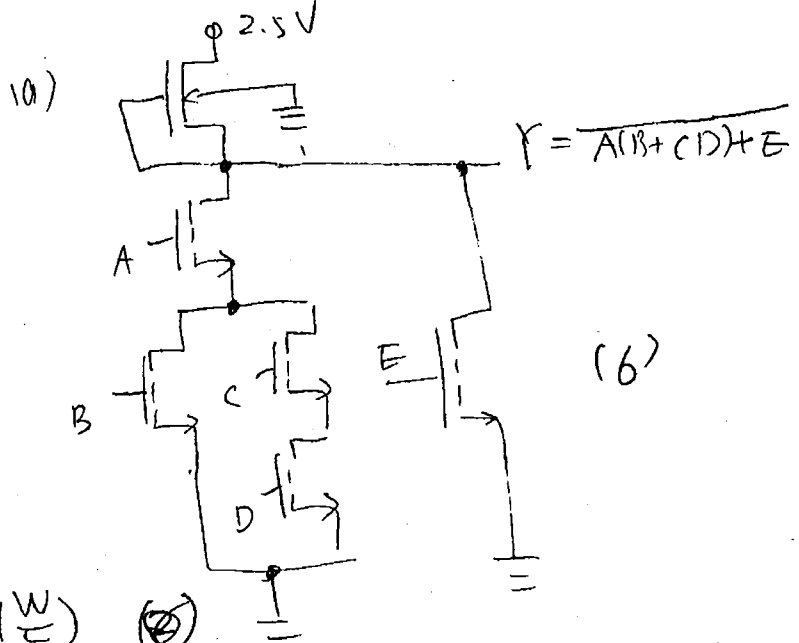
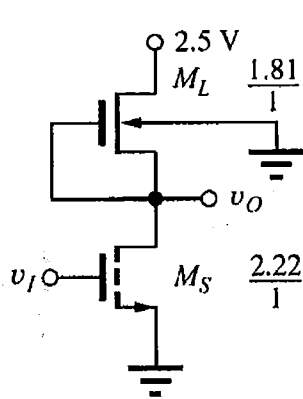
(16 pts) You are asked to design an NMOS logic gate that implements

$$Y = \overline{A(B + CD) + E}$$

based on the reference inverter shown below.

(a) (6 pts) Draw the circuit diagram.

(b) (10 pts) Find the W/L ratios of all transistors in the circuit such that the propagation delay (τ_p) is 1/2 the delay of the reference inverter below. (Hint: $\tau_p \propto R_{on}C$)



$$\tau \sim R_{on}C \propto \left(\frac{W}{L}\right)^{-1}$$

$$\tau \rightarrow \frac{1}{2}\tau \Rightarrow \left(\frac{W}{L}\right) \rightarrow 2\left(\frac{W}{L}\right) \quad (2)$$

(b) M_L should have $\left(\frac{W}{L}\right)$ doubled $\left(\frac{W}{L}\right)_L = \frac{3.62}{1}$

Let on-resistance of M_S to be R_{on}^S .

Pick worse case path ACD.

$$R_A + R_C + R_D = \frac{1}{2} R_{on}^S \quad \left(\frac{1}{2} \text{ delay}\right)$$

(i) $R_A = R_C = R_D = \frac{1}{6} R_{on}^S$, $R_B = \frac{1}{3} R_{on}^S$, $R_E = \frac{1}{2} R_{on}^S$.

$$\left(\frac{W}{L}\right)_{A,C,D} = 6 \left(\frac{2.22}{1}\right) = \frac{13.32}{1} \quad \left(\frac{W}{L}\right)_B = 3 \cdot \frac{2.22}{1} = \frac{6.66}{1}$$

$$\left(\frac{W}{L}\right)_E = \frac{4.44}{1} \quad 2'$$

(ii) $R_A = \frac{1}{4} R_{on}^S$, $R_C = R_D = \frac{1}{8} R_{on}^S$, $R_B = \frac{1}{4} R_{on}^S$, $R_E = \frac{1}{2} R_{on}^S$

$$\left(\frac{W}{L}\right)_{A,B} = 4 \left(\frac{2.22}{1}\right) = \frac{8.88}{1} \quad \left(\frac{W}{L}\right)_{C,D} = 8 \cdot \frac{2.22}{1} = \frac{17.76}{1}$$

$$\left(\frac{W}{L}\right)_E = \frac{4.44}{1}$$