

Metal-Oxide-Si (MOS) Cap

HW#6 Soln

1. Metal $\Rightarrow$ PolySi doped so $(E_F - E_C)_{\text{bulk}} = 0.05 \text{ eV} \therefore n+$

$$t_{\text{ox}} = x_{\text{ox}} = 50 \text{ \AA} = 50 \times 10^{-8} \text{ cm}$$

No significant oxide charges / p-type Si w/ $N_A = 5 \times 10^{17}$

$$C_{\text{ox}}' = \frac{K_{\text{ox}} \epsilon_0}{t_{\text{ox}}} = \frac{(3.9)(8.854 \times 10^{-14})}{50 \times 10^{-8}} = 6.91 \times 10^{-7} \frac{\text{F}}{\text{cm}^2}$$

$$\bar{\phi}_m = \chi_s - 0.05 = 4.0 \text{ V}$$

$$\phi_s = \chi_s + E_g - (E_F - E_V)_{\text{bulk}}$$

$$E_F - E_V = kT \ln \left(\frac{N_V}{p_0} \right) = 0.026 \ln \left(\frac{1.04 \times 10^{19}}{5 \times 10^{17}} \right) = 0.079 \text{ eV}$$

$$\bar{\phi}_s = 4.05 + 1.12 - 0.08 = 5.09 \text{ V}$$

$$\bar{\phi}_{ms} = 4 - 5.09 = -1.09 = V_{\text{FB}} \quad (\text{no oxide charges})$$

$$V_T = \bar{\phi}_{ms} - 2\phi_F - \frac{Q_B'}{C_{\text{ox}}'} - \frac{Q_{\text{ss}}}{C_{\text{ox}}'}$$

$$\phi_F = -\frac{kT}{q} \ln \frac{N_A}{n_i} = -0.026 \ln \left(\frac{5 \times 10^{17}}{1.5 \times 10^{10}} \right) = -0.45 \text{ V}$$

$$Q_B' = Q_{\text{dmax}} = -\sqrt{2K_s \epsilon_0 q N_A |2\phi_F|} = -3.881 \times 10^{-7} \frac{\text{C}}{\text{cm}^2}$$

$$V_T = -1.09 - 2(-0.45) - \frac{(-3.88 \times 10^{-7})}{6.91 \times 10^{-7}} = 0.3716 \text{ V}$$

a) $V_{\text{gb}} = -1 \text{ V} \quad V_{\text{FB}} < V_{\text{gb}} < V_T \Rightarrow \text{depletion}$

$$V_{\text{gb}} - \bar{\phi}_{ms} = V_{\text{ox}} + V_s \quad V_{\text{ox}} = -\frac{Q_B'}{C_{\text{ox}}'} \quad \text{eq (11)}$$

$$-1 + 1.09 = \frac{\sqrt{2qK_s \epsilon_0 N_A V_s}}{C_{\text{ox}}'} + V_s \quad \leftarrow \text{+ since } \sqrt{V_s} > 0$$

$$0.09 = 0.59 \sqrt{V_s} + V_s \Rightarrow \sqrt{V_s} = \frac{-0.59 \pm \sqrt{(0.59)^2 + 4(0.09)}}{2} = 0.125$$

$$\phi_s = V_s = 0.016 \text{ V}$$

$$V_{\text{ox}} = 0.59 \sqrt{V_s} = 0.07 \text{ V}$$

$$x_d = \frac{-Q_s}{qN_A} = \frac{Q_g}{qN_A} = 5.8 \times 10^{-7} \text{ cm}$$

$$Q_g = C_{\text{ox}} V_{\text{ox}} = 4.64 \times 10^{-8} \frac{\text{C}}{\text{cm}^2}$$

$$C_d' = \frac{K_s \epsilon_0}{x_d} = 1.79 \times 10^{-6} \frac{\text{C}}{\text{cm}^2 \text{ V}}$$

$$C = \frac{C_{\text{ox}}' C_d'}{C_{\text{ox}}' + C_d'} = 5.0 \times 10^{-7} \frac{\text{C}}{\text{cm}^2 \text{ V}} \quad \text{at high } f \text{ low } f$$

1b) $V_{gb} = 0.0V$ $V_{FB} < V_{gb} < V_T \Rightarrow$ depletion

$$V_{gb} - \phi_{ms} = V_{ox} + V_s$$

$$1.09 = \frac{\sqrt{2K_s \epsilon_0 q N_a V_{ox}}}{C_{ox}'} + V_s = 0.59 \sqrt{V_s} + V_s$$

$$V_s + 0.59 \sqrt{V_s} - 1.09 = 0$$

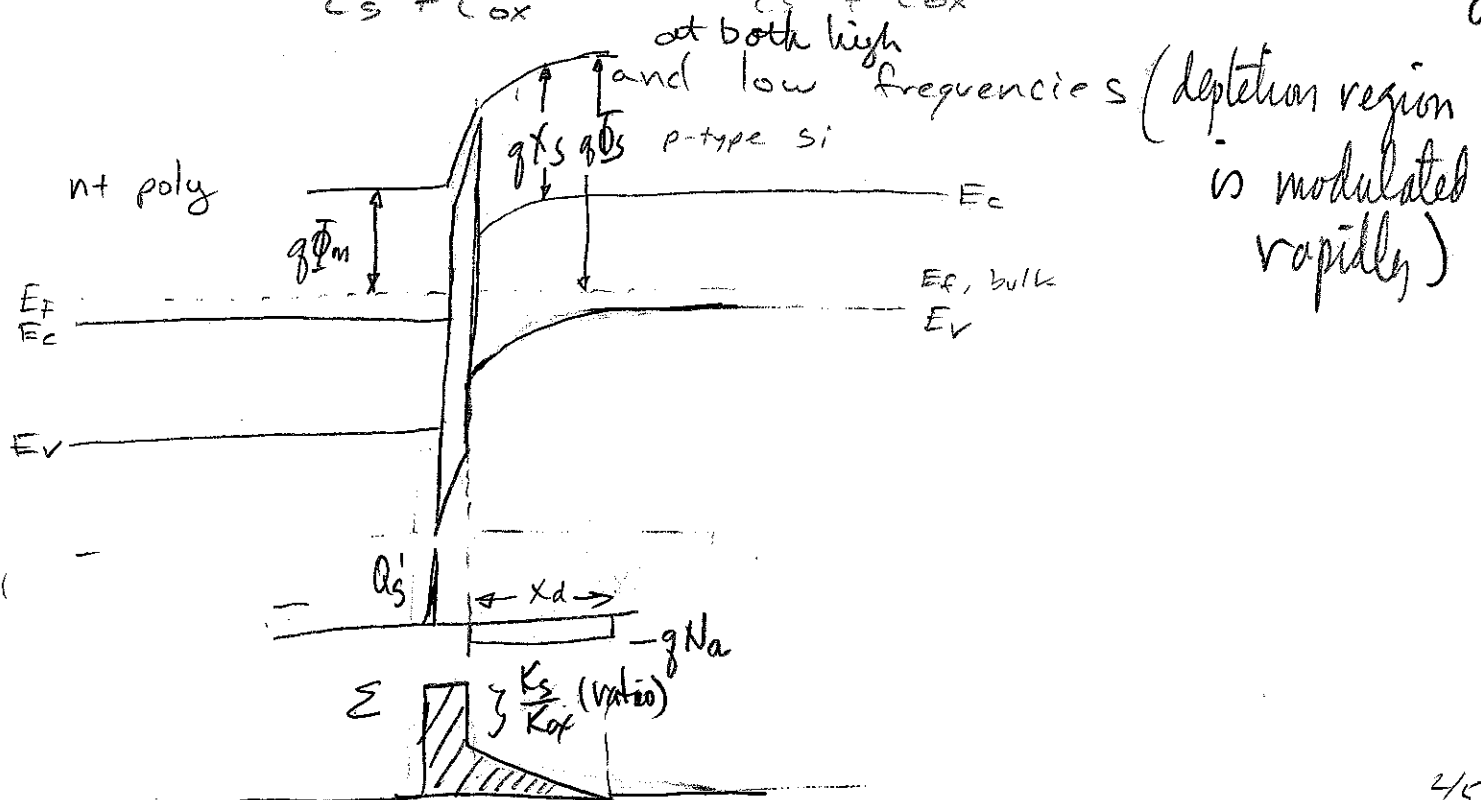
$$\sqrt{V_s} = 0.79 \Rightarrow \underline{V_s = 0.62 = \phi_s}$$

$$V_{ox} = 0.59 \sqrt{V_s} = 0.47$$

$$Q_G' = -Q_d' = C_{ox}' V_{ox} = 3.25 \times 10^{-7} \frac{C}{cm^2}$$

$$C_s' = \frac{K_s \epsilon_0}{x_d} = \frac{K_s \epsilon_0}{Q_d' / q N_a} = \frac{(11.8)(8.854 \times 10^{-14})}{\frac{3.25 \times 10^{-7}}{(1.6 \times 10^{-19})(5 \times 10^{17})}} = 2.57 \times 10^{-7} \frac{F}{cm^2}$$

$$C_{mos}' = C_{ox}' // C_s' = \frac{C_s' C_{ox}'}{C_s' + C_{ox}'} = \frac{(2.57 \times 10^{-8})(6.906 \times 10^{-7})}{C_s' + C_{ox}'} = 1.87 \times 10^{-7} \frac{F}{cm^2}$$



$$1c) \quad V_{gb} = 2V$$

$$V_{gb} > V_T \Rightarrow \text{Inversion}$$

$$V_s = \phi_s \approx 2|\phi_F| = 2(0.4504) = 0.9008 V$$

$$V_{gb} - \phi_{ms} = V_{ox} + V_s$$

$$2 + 1.0911 = V_{ox} + 0.9008 \Rightarrow V_{ox} = 2.1823 V$$

$$V_{ox} = -\frac{Q_s'}{C_{ox}'} \Rightarrow Q_s' = -2.1823 (6.906 \times 10^{-7}) = -1.507 \times 10^{-6} \frac{C}{cm^2}$$

$$Q_m' = -Q_s' \quad (\text{since no oxide charge}) \Rightarrow$$

$$Q_m' = Q_g' = 1.51 \times 10^{-6} \frac{C}{cm^2}$$

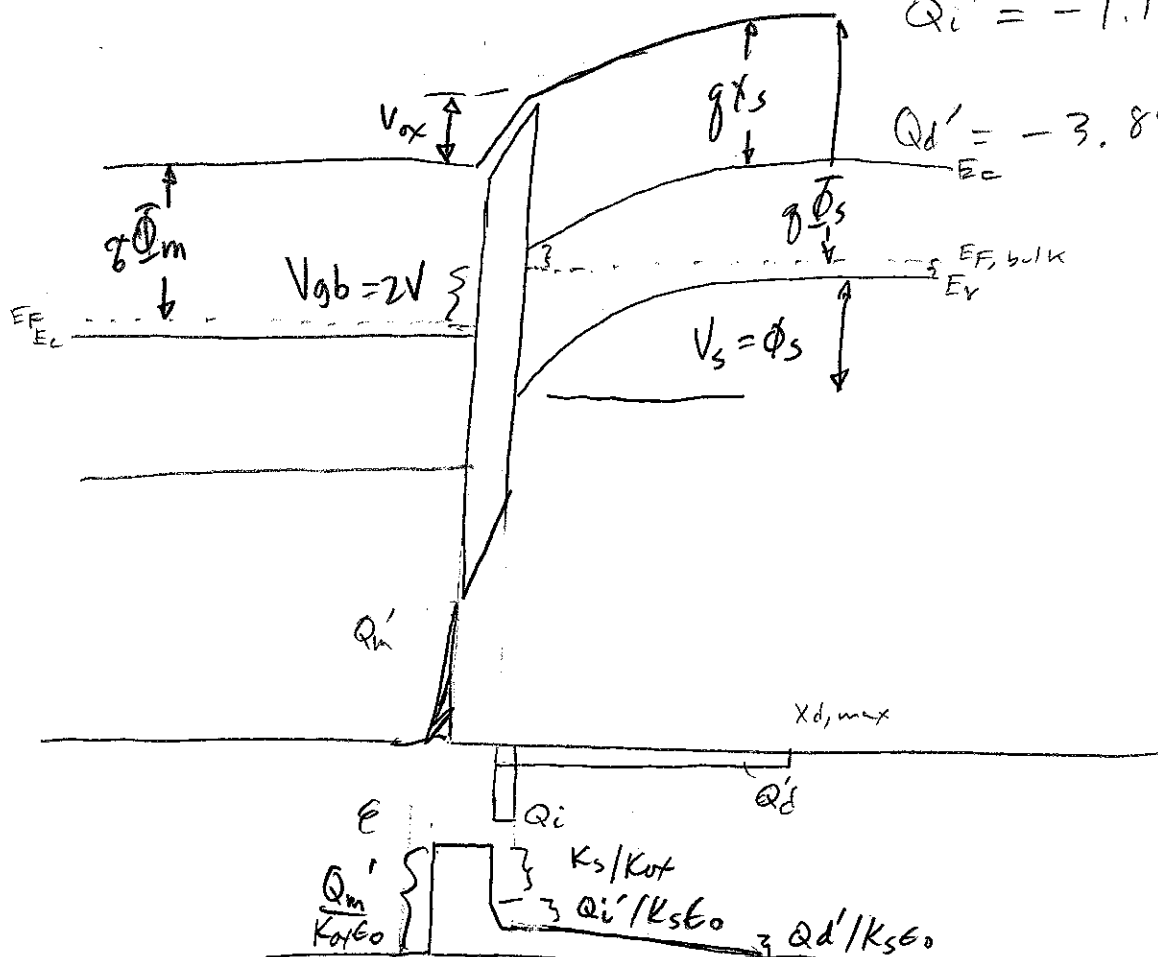
Inversion Charge:

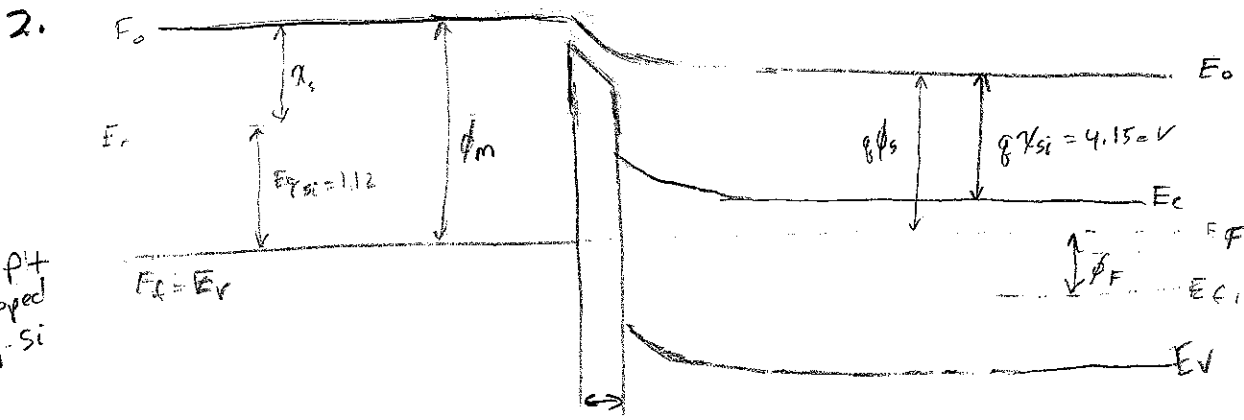
$$V_{gb} = \phi_{ms} + 2|\phi_F| - \frac{Q_d' + Q_i'}{C_{ox}'}$$

$$V_{gb} = \underbrace{\phi_{ms} + 2|\phi_F|}_{V_T} - \frac{Q_d'}{C_{ox}'} - \frac{Q_i'}{C_{ox}'}$$

$$Q_i' = -1.1246 \times 10^{-6} \frac{C}{cm^2}$$

$$Q_d' = -3.88 \times 10^{-7} \frac{C}{cm^2}$$





$$\frac{Q_{ss}'}{q} = 5 \times 10^{10} \text{ cm}^{-2}$$

$$\frac{P_{ox}}{q} = 2 \times 10^{16} \text{ cm}^{-3}$$

$$C_{ox}' = \frac{k_{ox} \epsilon_{ox}}{t_{ox}} = \frac{3.9 \times 8.854 \times 10^{-14} \frac{\text{F}}{\text{cm}}}{50 \times 10^{-8} \text{ cm}} = 6.9 \times 10^{-7} \frac{\text{F}}{\text{cm}^2}$$

$$\bar{\phi}_s = \chi_{si} + (E_c - E_F)$$

$$N_d = 10^{17} \text{ cm}^{-3} \Rightarrow (E_c - E_F) = .15 \text{ V}$$

$$\bar{\phi}_s = 4.05 + .15 = 4.2 \text{ V}$$

$$\bar{\phi}_m = \chi_s + E_g = 4.05 + 1.12$$

$$\bar{\phi}_{ms} = \bar{\phi}_m - \bar{\phi}_s = 1.12 - .15 = 0.97 \text{ V}$$

There exists Q_{ss} on SiO_2 , so $V_{FB} \neq \bar{\phi}_{ms}$

$$V_{FB} = \bar{\phi}_{ms} - \frac{Q_{ss}'}{C_{ox}'} - \frac{1}{C_{ox}'} \int_0^{t_{ox}} \frac{x}{t_{ox}} \rho(x) dx$$

$$V_{FB} = \bar{\phi}_{ms} - \left(\begin{array}{c} \Delta V_{\text{interface}} \\ \text{due to} \\ \text{charge} \end{array} \right) - \left(\begin{array}{c} \Delta V_{\text{oxide}} \\ \text{due to} \\ \text{charge} \end{array} \right)$$

$$= \bar{\phi}_{ms} - \frac{q}{C_{ox}'} \left[Q_{ss}' + P_{ox} \frac{t_{ox}^2}{2 \cdot t_{ox}} \right]$$

$$= 0.97 \text{ V} - \frac{1.6 \times 10^{-19}}{6.9 \times 10^{-7}} \left[5 \times 10^{10} + 2 \times 10^{16} \frac{(50 \times 10^{-8})^2}{2(50 \times 10^{-8})} \right]$$

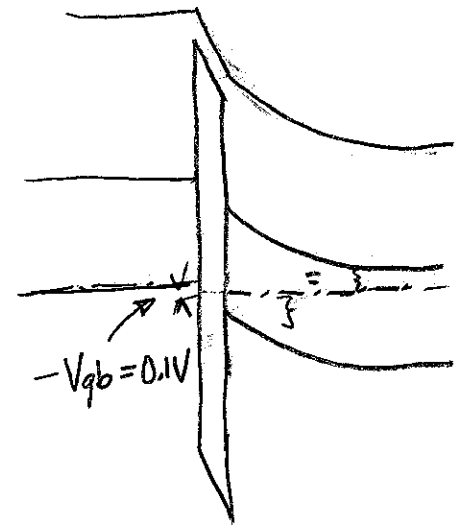
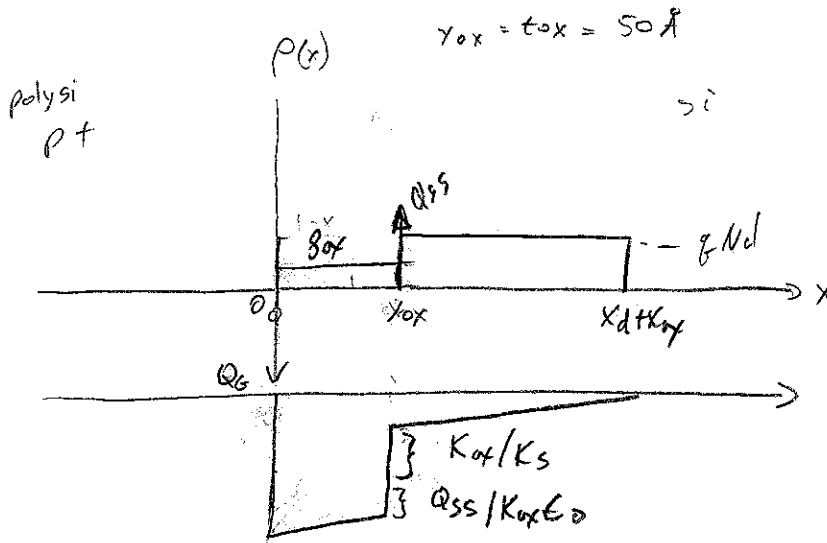
5.5×10^{10}

$$V_{FB} = 0.97 - .0128$$

$$\underline{V_{FB} = 0.957 \text{ V}}$$

2.

EOST
Edge-of-Strong
Inversion



$$Q_B' = q N_d x_{dmax}$$

$$x_{dmax} = \sqrt{\frac{2K_s\epsilon_0}{qN_d} |2\phi_F|}$$

$$\phi_F = \frac{kT}{q} \ln\left(\frac{N_d}{n_i}\right)$$

$$= 0.407 V$$

$$Q_B' = \sqrt{2K_s\epsilon_0 q N_d |2\phi_F|}$$

$$V_T = V_{FB} - 2\phi_F - \frac{Q_B'}{C_{ox}} = 0.957 - 0.814 - 0.238 = -0.1V$$

FB
Flat-Band

