

Homework #6

1 a) $N_d = 10^{19} \text{ cm}^{-3}$ $W_n = 200 \mu\text{m}$

$N_a = 10^{17} \text{ cm}^{-3}$ $W_p = 0.2 \mu\text{m}$

(I) Zener $\rightarrow$ does not occur because both doping concentrations should be at least 10^{18} cm^{-3}

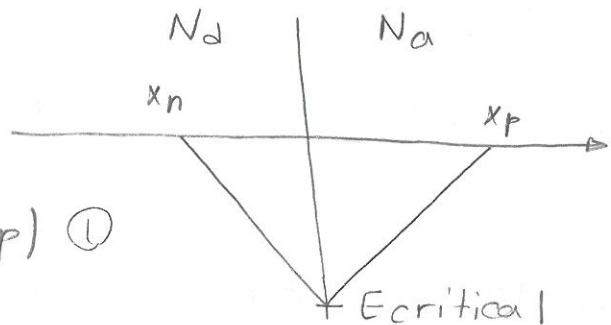
(II) Avalanche $\rightarrow$ From Fig. 3.12 (P. 13) we know that $E_{cr} = 6 \times 10^5 \text{ V cm}^{-1}$

We know that $\rightarrow$

$\phi_i - V_A = \frac{1}{2} E_{critical} (x_n + x_p)$ ①

$x_n = - \frac{E_{critical} \times K \epsilon_0}{q N_d} = -3.88 \times 10^{-7} \text{ cm}$

$x_p = \frac{E_{critical} \times K \epsilon_0}{q N_a} = 3.88 \times 10^{-5} \text{ cm}$



② $\phi_i = \frac{kT}{q} \ln \left(\frac{N_d N_a}{n_i^2} \right)$
 $= \underline{\underline{0.943 \text{ V}}}$

①, ② $\Rightarrow \phi_i - V_A = \frac{1}{2} \times 6 \times 10^5 \text{ V cm}^{-1} \times 3.88 \times 10^{-5} \text{ cm} = 11.64 \text{ V}$

$\Rightarrow \underline{\underline{V_A = -10.69 \text{ V}}}$

(III) Punch-through

This happens when $x_p = W_p = 0.2 \mu\text{m} = 2 \times 10^{-5} \text{ cm}$

$$x_p = \left(\frac{2K\epsilon_0}{q} (\phi_i - V_a) \frac{N_d}{N_a(N_d + N_a)} \right)^{\frac{1}{2}}$$

$$\Rightarrow \phi_i - V_a = 3.09 \Rightarrow V_a = -\underline{\underline{2.15V}} \Rightarrow$$

Punch-through happens

(I) 1b) Zener break down $\rightarrow$ For $N_a = 10^{18}$ $E_{critical} = 10^6 \text{ Vcm}^{-1}$

(II) Avalanche $\rightarrow$

$$x_n = \frac{E_{critical} \times K\epsilon_0}{q N_d} = 6.47 \text{ nm}$$

$$x_p = \frac{E_{critical} \times K\epsilon_0}{q N_a} = 64.7 \text{ nm}$$

$$\phi_i - V_a = \frac{1}{2} E_{critical} (x_n + x_p) = 3.56 \text{ V} \Rightarrow V_a = -\underline{\underline{2.58V}} \quad \textcircled{1}$$

Both Can Occur

(III) Punch-through $\rightarrow$ This happens when $x_p = w_p = 0.2 \mu\text{m}$

$$\Rightarrow \phi_i - V_a = 33.99 \Rightarrow V_a = -\underline{\underline{33.02V}} \quad \textcircled{2}$$

① & ② $\rightarrow$ Both Zener and avalanche occur.

$$1) c) N_d = N_a = 10^{19} \Rightarrow E_{\text{critical}} = 3 \times 10^6 \text{ V cm}^{-1}$$

Punch-through $\rightarrow$

$$x_p = w_p = 2 \times 10^{-5} \text{ cm} = \left(\frac{2k\epsilon_0}{q} (q_i - V_A) \frac{10^{19}}{10^{19} \times 2 \times 10^{19}} \right)^{\frac{1}{2}}$$

$$q_i = \frac{kT}{q} \ln \left(\frac{(10^{19})^2}{10^{20}} \right) = 1.06 \text{ V}$$

$$\Rightarrow V_A = \underline{-617.03 \text{ V}}$$

Zener $\rightarrow E_{\text{critical}} = 3 \times 10^6 \text{ V cm}^{-1}$

$$x_n = x_p = \frac{E_{\text{critical}} \times k\epsilon_0}{q N_a} = \frac{3 \times 10^6 \times 11.7 \times 8.85 \times 10^{-14}}{1.6 \times 10^{-19} \times 10^{19}} \text{ cm}$$

$$= 1.94 \times 10^{-6} \text{ cm}$$

$$q_i - V_A = \frac{1}{2} E_{\text{critical}} (x_n + x_p) = 5.82 \Rightarrow V_A = \underline{-4.76 \text{ V}}$$

$\Rightarrow$ Zener Occurs (Avalanche Can not occur

because the dopings are both greater than 10^{18} cm^{-3}

so ionized impurity scattering becomes dominant which makes carriers unable to gain as much energy before being scattered)

2a) $N_d \gg N_a$, $N_a = 5 \times 10^{16} \text{ cm}^{-3}$ $\tau_n = \tau_p = 1 \mu\text{s}$ $T = 300 \text{ K}$

One-Sided junction $\Rightarrow$ diode current is mainly electrons injected into the p-Side.

$$J = 50 \text{ A cm}^{-2} \approx J_{np} = \frac{Q_n}{\tau_n} \Rightarrow Q_n = (50 \text{ A cm}^{-2}) (10^{-6} \text{ s})$$

$\uparrow$ $\leftarrow$ P-Side
 $\bar{e}$ current

$$= 5 \times 10^{-5} \frac{\text{C}}{\text{cm}^2}$$

2b) $Q_d = \sqrt{2 K \epsilon_0 q N_a (\phi_i - V_a)} \rightarrow$ Need both of ϕ_i and V_a

For V_a , we can find it with the current density:

$$J_{np} = q \frac{n_i^2}{N_a} \left(\frac{D_n}{L_n} \right) \exp\left(\frac{q V_a}{k T}\right) \Rightarrow$$

$$V_a = \frac{k T}{q} \ln \left(\frac{J_{np} N_a L_n}{n_i^2 q D_n} \right)$$

@ $N_a = 5 \times 10^{16} \text{ cm}^{-3} \Rightarrow \mu_n = 975 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$

$$D_n = \frac{k T}{q} \mu_n = 24.96 \text{ cm}^2 \text{ s}^{-1} \Rightarrow L_n = \sqrt{D_n \tau_n} \approx 5 \times 10^{-3} \text{ cm}$$

$$\Rightarrow V_a = 0.0256 \ln \left(\frac{50 \text{ A cm}^{-2} \times 5 \times 10^{16} \text{ cm}^{-3} \times 5 \times 10^{-3} \text{ cm}}{10^{20} \text{ cm}^{-6} \times 1.6 \times 10^{-19} \text{ C} \times 24.96 \text{ cm}^2 \text{ s}^{-1}} \right)$$

$$= 0.795 \text{ V} / \text{and } \phi_i = \frac{k T}{q} \ln \left(\frac{N_d N_a}{n_i^2} \right) \rightarrow$$

Need N_d ! Since $N_d \gg N_A$ assume that $E_F = E_C$ and

full ionization $\Rightarrow n = N_d = N_C \exp\left(\frac{0}{kT}\right) = N_C = 2.8 \times 10^{19} \text{ cm}^{-3}$

$$\Rightarrow \phi_i = 0.0256 \ln\left(\frac{5 \times 10^{16} \times 2.8 \times 10^{19}}{10^{20}}\right) \text{ V} = 0.952 \text{ V}$$

$$\Rightarrow Q_d = [2(11.7)(8.85 \times 10^{-14} \text{ Fcm})(1.6 \times 10^{-19} \text{ C})(5 \times 10^{16} \text{ cm}^{-3})(0.952 - 0.795) \text{ V}]$$
$$= \underline{\underline{5.1 \times 10^{-8} \text{ Ccm}^{-2}}}$$

Charge stored @ equilibrium ($V_a = 0$) $\Rightarrow$

$$\underline{\underline{Q_d = 1.26 \times 10^{-7} \text{ Ccm}^{-2}}}$$

2c) There are two parts to the switching. We have to address the change in the depletion charge and the stored charge in the neutral region.

as V_{diode} rises, first only the depletion charge is changing significantly.

$$\Delta Q_d = Q_d @ 0 - Q_d @ 50 \text{ A} = 7.5 \times 10^{-8} \text{ Ccm}^{-2}$$

$$t_1 = \frac{\Delta Q_d}{50 \text{ Acm}^{-2}} = \frac{7.5 \times 10^{-8}}{50} \text{ S} = \underline{\underline{1.5 \text{ ns}}}$$

2C) after that, Q_n and $\frac{Q_n}{\tau_n}$ (recombination) become significant.

using the continuity equation:

$$I_f = \frac{Q_n}{\tau_n} + \frac{dQ_n}{dt} \leftarrow \text{not zero, not in equilibrium.}$$

$$Q_n = I_f \tau_n \left[1 - \exp\left(-\frac{t}{\tau_n}\right) \right] = 50 \times 10^{-6} \left[1 - \exp\left(-\frac{t}{\tau_n}\right) \right] \frac{C}{cm^2}$$

(i) Turn-on defined as Q_n reaches 63% of its final value.

$$\Rightarrow \left[1 - \exp\left(-\frac{t_2}{\tau_n}\right) \right] = 63\% \Rightarrow t_2 = 1.02 \times 10^{-6} s = \underline{1.02 \mu s}$$

Turn on time = $t_1 + t_2 \simeq 1.02 \mu s$ (Filling Q_d is really fast)

(ii) Turn-on defined as $V_d = 0.795 - 0.1 = 0.695 V$

$$Q_n = 50 \times 10^{-6} C cm^{-2} \exp\left(-\frac{0.1V}{25mV}\right) = 916 \times 10^{-9} C cm^{-2}$$

$$\Rightarrow 50 \times 10^{-6} \left[1 - \exp\left(-\frac{t_2}{\tau_n}\right) \right] = 916 \times 10^{-9} C cm^{-2}$$

$$\Rightarrow t_2 = 1.85 \times 10^{-8} s = \underline{18.5 ns}$$

and since V_d has changed, Q_d has changed too

$$@ 0.695 V, Q_d = 6.53 \times 10^{-8} C cm^{-2} \Rightarrow \Delta Q_d = 6.07 \times 10^{-8} C cm^{-2}$$

$$t_1 = \frac{\Delta Q_d}{50 A cm^{-2}} = \underline{1.21 ns} \Rightarrow t_{\text{turn-on}} = \underline{14.41 ns}$$

2d) With a -50 A cm^{-2} reverse current, we can again use the continuity equation to figure out the response.

$$I_R = \frac{Q_n}{\tau_n} + \frac{dQ_n}{dt} = -50 \text{ A cm}^{-2}$$

$$Q_n(t=0) = I_f \tau_n = 50 \times 10^{-6} \text{ A cm}^{-2} \text{ s}$$

$$Q_n = A + B \exp\left(-\frac{t}{\tau_n}\right)$$

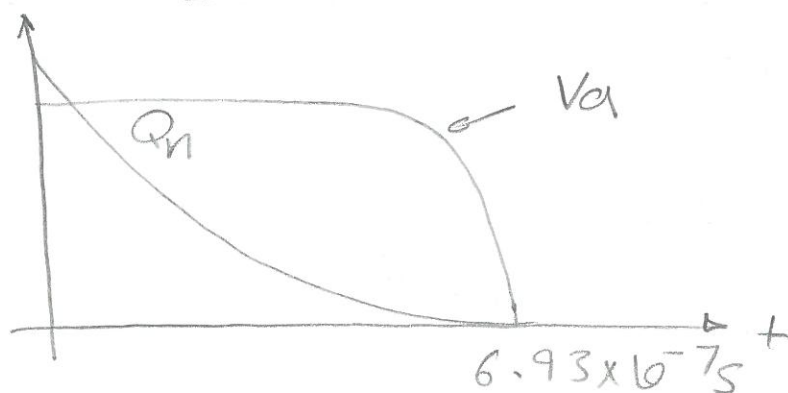
$$A + B = 50 \times 10^{-6} \text{ C cm}^{-2}$$

$$A = I_R \tau_n = -50 \times 10^{-6} \text{ C cm}^{-2} \Rightarrow B = 100 \times 10^{-6} \text{ C cm}^{-2}$$

$$Q_n = 50 \times 10^{-6} \text{ C cm}^{-2} \left(2 \exp\left(-\frac{t}{\tau_n}\right) - 1\right)$$

$$\text{Storage time } (t_s) \Rightarrow 2 \exp\left(-\frac{t}{\tau_n}\right) - 1 = 0$$

$$\Rightarrow t_s = \underline{\underline{6.93 \times 10^{-7} \text{ s}}}$$



2 e) For short-base:

$$J_{np} = q \frac{n_i^2}{N_a} \left(\frac{D_n}{W_p'} \right) \left[\exp\left(\frac{qV_a}{kT}\right) - 1 \right] \quad W_p' = |W_p - x_p|$$

$$Q_n = \frac{1}{2} W_p' q \frac{n_i^2}{N_a} \left[\exp\left(\frac{qV_a}{kT}\right) - 1 \right] = J_{np} \left(\frac{W_p'^2}{2D_n} \right)$$

$$= 50 \text{ A cm}^{-2} \left(\frac{(0.5 \times 10^{-4} \text{ cm})^2}{2 \times 24.96 \text{ cm}^2 \text{ s}^{-1}} \right) = 2.5 \times 10^{-9} \text{ C cm}^{-2}$$

$$\Rightarrow t_2 = 5.01 \times 10^{-11} \text{ s}$$

$$V_a = \frac{kT}{q} \ln \left[\frac{2 Q_n N_a}{q n_i^2 W_p'} + 1 \right] = \underline{\underline{0.678 \text{ V}}}$$

$$Q_d @ 0.678 \text{ V} = 6.74 \times 10^{-8} \text{ C cm}^{-2}$$

$$\Rightarrow t_1 = \frac{6.74 \times 10^{-8} \text{ C cm}^{-2}}{50 \text{ A cm}^{-2}} = 1.35 \text{ ns}$$

$$\Rightarrow \text{Total Switching time} \approx 1.35 \text{ ns}$$

A lot less stored charge in a short-base Junction.

$$3. \text{GaAs} \quad N_a = 10^{18} \quad N_d = 10^{17} \quad W_p = 0.9 \mu\text{m} \quad W_n = 100 \mu\text{m}$$

$$\tau_n = \tau_p = 0.01 \mu\text{s} \quad A = 0.25 \text{cm}^2$$

$$N_a = 10^{18} \text{cm}^{-3} \Rightarrow \mu_n = 275 \text{cm}^2 \text{V}^{-1} \text{s}^{-1} \Rightarrow D_n = 0.0256 \text{V} \times 275 \text{cm}^2 \text{V}^{-1} \text{s}^{-1} \\ = 7.04 \text{cm}^2 \text{s}^{-1}$$

$$\Rightarrow L_n = \sqrt{D_n \tau_n} = 2.65 \times 10^{-4} \text{cm} = 2.65 \mu\text{m} > W_p \text{ (Short diode at P side)}$$

$$N_d = 10^{17} \text{cm}^{-3} \Rightarrow \mu_p = 250 \text{cm}^2 \text{V}^{-1} \text{s}^{-1} \Rightarrow D_p = 6.4 \text{cm}^2 \text{s}^{-1} \Rightarrow L_p = 2.53 \mu\text{m} \\ \text{(long diode at n side)}$$

a)

Need to know depletion region widths:

$$x_n = \left[\frac{2kT}{q} \ln \left(\frac{N_d N_a}{n_i^2} \right) \right]^{\frac{1}{2}}$$

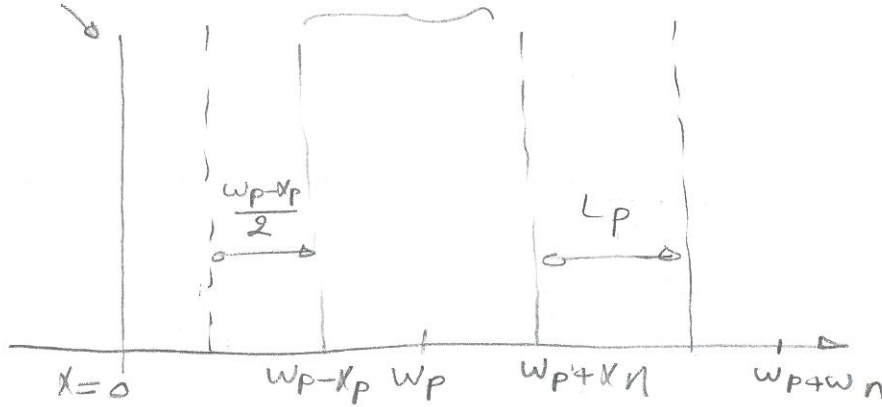
$$q_i = \frac{kT}{q} \ln \left(\frac{N_d N_a}{n_i^2} \right) = 1.31 \text{V}$$

$$\Rightarrow x_n = \left[\frac{2 \times 12.9 \times 8.85 \times 10^{-14}}{1.6 \times 10^{-19}} \times 1.31 \times \frac{10^{18}}{10^{18} \times (10^{17} + 10^{18})} \right]^{\frac{1}{2}} = 4.12 \times 10^{-6} \text{cm} \\ = 0.0412 \mu\text{m}$$

$$x_p = \left[\frac{2kT}{q} \ln \left(\frac{N_d N_a}{n_i^2} \right) \right]^{\frac{1}{2}} = 1.3 \times 10^{-6} \text{cm} = 0.013 \mu\text{m}$$

Surface of the p side

depletion region



all the carriers generated from $\frac{w_p - x_p}{2}$ to $w_p + x_n + L_p$ are captured by depletion region and end up as

Short circuit current $\Rightarrow$

$$I_{ph} = qA \int_{\frac{w_p - x_p}{2}}^{w_p + x_n + L_p} g(x) dx = qA \phi_0 \eta \left[\exp(-\alpha(\frac{w_p - x_p}{2})) - \exp(-\alpha(w_p + x_n + L_p)) \right]$$

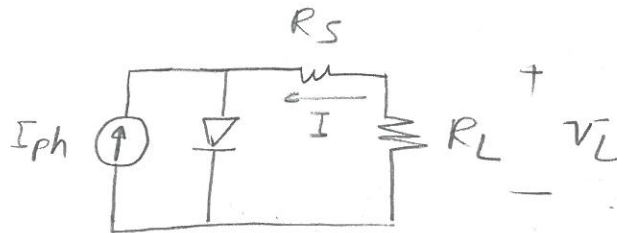
@ wavelength = $0.65 \mu m \Rightarrow \alpha = 2 \times 10^4 \text{ cm}^{-1}$

$$\phi_0 = \frac{P_g}{hc} = \frac{10 \text{ mW}}{\text{cm}^2} \times \frac{1}{\frac{1.24}{0.65} \times 1.6 \times 10^{-19} \text{ J}} = 3.28 \times 10^{16} \text{ cm}^{-2} \text{ s}^{-1}$$

$$\Rightarrow I_{ph} = (1.6 \times 10^{-19} \text{ C}) (0.25 \text{ cm}^2) (3.28 \times 10^{16} \text{ cm}^{-2} \text{ s}^{-1}) (0.9) \times \left[\exp(-10^4 \text{ cm}^{-1} \times 0.1935 \times 10^{-4}) - \exp(-2 \times 10^4 (2.97 \times 10^{-4})) \right] =$$

$$= 9.7 \times 10^{-4} \text{ A} = \underline{\underline{0.97 \text{ mA}}}$$

3 b)



$$P = - \frac{kT}{q} \frac{R_L I}{R_s + R_L} \ln \left(\frac{I_{ph} + I}{I_0} + 1 \right)$$

need to know I and R_s :

$$P = \frac{1}{q n \mu_n} = \frac{1}{1.6 \times 10^{-14} \times 10^{17} \times 800} = 0.0781 \Omega \text{ cm}$$

$$W_n = 100 \times 10^{-4} \text{ cm} \Rightarrow R_s = P \frac{L}{A} = 0.0781 \times \frac{10^{-2}}{0.25} = 3.125 \times 10^{-3} \Omega = \underline{\underline{3.125 \text{ m}\Omega}}$$

For I we need to solve this equation:

$$V_L = -I R_L \Rightarrow \frac{kT}{q} \frac{R_L}{R_s + R_L} \ln \left(\frac{I_{ph} + I}{I_0} + 1 \right) = -I R_L$$

$$I_0 = q A n_i^2 \left[\frac{D_p}{N_d L_p} + \frac{D_n}{N_a W_p} \right] = (1.6 \times 10^{-19} \text{ C}) (0.25 \text{ cm}^2) (2.4 \times 10^6 \text{ cm}^{-3})^2$$

$$\times \left[\frac{6.4 \text{ cm}^2 \text{ s}^{-1}}{10^{17} \text{ cm}^{-3} \times 2.53 \times 10^{-4} \text{ cm}} + \frac{7.04 \text{ cm}^2 \text{ s}^{-1}}{10^{18} \text{ cm}^{-3} \times 0.4 \times 10^{-4} \text{ cm}} \right] = 9.82 \times 10^{-20} \text{ A} \Rightarrow I \approx -I_{ph}$$

$$\Rightarrow P = R_L I^2 = (0.97 \times 10^{-3} \text{ A})^2 \times 100 \Omega = \underline{\underline{0.094 \text{ mW}}}$$

to find P_{max} we need to solve (94 P.38)

$$\Rightarrow \begin{cases} P_{\max} = 0.811 \text{ mW} \\ I_m = 9.42 \times 10^{-4} \text{ A} \end{cases} \Rightarrow R_L = \frac{0.811 \text{ mW}}{(9.42 \times 10^{-4})^2} = 913.95 \Omega$$

$\Rightarrow$ If we increase R_L to 913.95Ω we get better Power and after that less power.

3C) E_g for GaAs = 1.424 eV (300 K)

$$E_g = h \frac{c}{\lambda} = \frac{1.24}{\lambda(\mu\text{m})} \text{ eV} \Rightarrow \lambda = \frac{1.24}{1.424} \mu\text{m} \approx \underline{\underline{871 \text{ nm}}}$$

3d)

$$q_{\text{out}} = \int U dx = \int_{n\text{-Side}} U dx + \int_{p\text{-Side}} U dx \quad (\text{Short diode})$$

$$= \frac{n p_0 \left(e^{\frac{qVA}{kT}} - 1 \right) W_p}{2 \tau_n} + \frac{A_p p_0 \left(e^{\frac{qVA}{kT}} - 1 \right)}{\tau_p}$$

$$= \frac{5.76 \times 10^{-6} \times 3.73 \times 10^{13} \times 0.4 \times 10^{-4} \text{ cm}^{-2} \text{ s}^{-1}}{2 \times 0.01 \times 10^{-6}} + \frac{2.53 \times 10^{-4} \times 5.76 \times 10^{-5} \times 3.73 \times 10^{13} \text{ cm}^{-2} \text{ s}^{-1}}{0.01 \times 10^{-6} \text{ cm s}} \\ \approx \underline{\underline{5.44 \times 10^{13} \text{ cm}^{-2} \text{ s}^{-1}}}$$

The recombination takes place in two quasi-neutral n and p regions (Ignoring the recombination in the depletion region).

4. Using a polysilicon gate that acts as a metal.

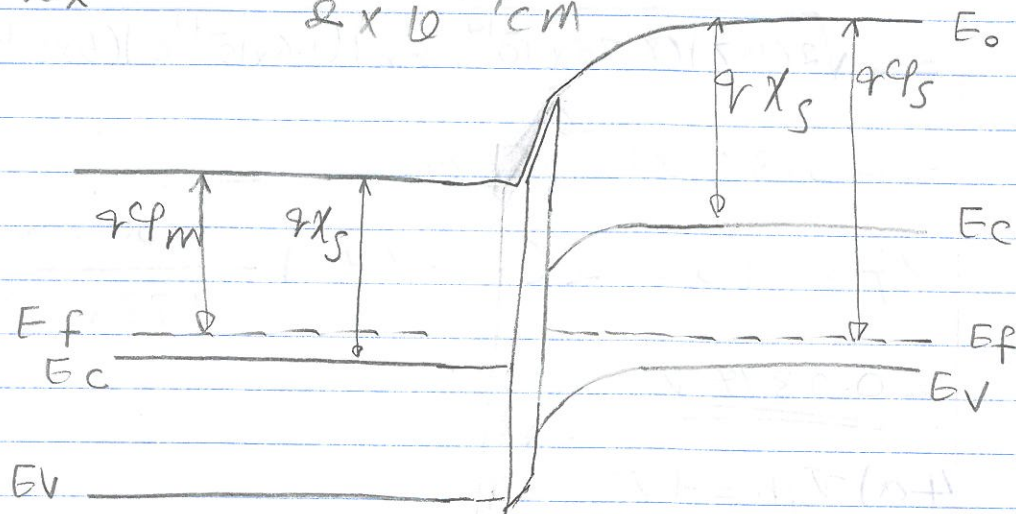
$$E_f = E_c + 0.05 \text{ eV} \Rightarrow n^+ \text{ degenerate}$$

$$t_{ox} = 2 \times 10^{-7} \text{ cm} ; N_A = 5 \times 10^{17} \text{ cm}^{-3}$$

In order to determine the mode of operation

we need to find V_T first.

$$C_{ox} = \frac{\kappa_{ox} \epsilon_0}{t_{ox}} = \frac{(3.9)(8.85 \times 10^{-14} \text{ F cm}^{-1})}{2 \times 10^{-7} \text{ cm}} = 1.73 \times 10^{-6} \text{ F cm}^{-2}$$



$$\chi_s = 4.05 \text{ V}$$

$$\phi_m = \chi_s - (E_f - E_c) = 4 \text{ V}$$

$$\phi_s = \chi_s + E_g - (E_f - E_v)$$

$$E_f - E_v = \frac{kT}{q} \ln\left(\frac{N_v}{N_A}\right) = 25 \text{ mV} \ln\left(\frac{2.5 \times 10^{19}}{5 \times 10^{17}}\right) = 0.0978 \text{ V}$$

$$\phi_s = (4.05 + 1.12 - 0.0978) \text{ V} = 5.07 \text{ V}$$

$$\phi_{ms} = \phi_m - \phi_s = 4.0 - 5.07 \text{ V} = -1.07 \text{ V}$$

Since there are no oxide charges, $V_{FB} = \phi_{ms} = \underline{\underline{-1.07V}}$

Threshold voltage V_T :

$$V_T = \phi_{ms} - 2\phi_F - \frac{Q_B'}{C_{ox}} \quad (\text{need to find all the terms!})$$

$$\phi_F = \frac{-kT}{q} \ln\left(\frac{N_A}{n_i}\right) = -25\text{mV} \ln\left(\frac{5 \times 10^{17}}{10^{10}}\right) = \underline{\underline{-0.443V}}$$

$$Q_B' = Q_{dmax}' = -\sqrt{2K\epsilon_0 q N_A |2\phi_F|}$$

$$= -\sqrt{2(11.7)(8.85 \times 10^{-14} \text{F/cm})(1.6 \times 10^{-19} \text{C})(5 \times 10^{17} \text{cm}^{-3})2(0.443)}$$

$$= -0.383 \times 10^{-6} \text{Ccm}^{-2}$$

$$V_T = -1.07 - 2(-0.443) - \frac{(-0.383 \times 10^{-6} \text{Ccm}^{-2})}{1.73 \times 10^{-6} \text{Fcm}^{-2}}$$

$$= \underline{\underline{0.0374V}}$$

4a) $V_{gb} = -1V$

$$V_{FB} < V_{gb} < V_T \Rightarrow \text{depletion.}$$

$$V_{gb} - \phi_{ms} = V_{ox} + V_S \quad (1)$$

$$V_{ox} = \frac{-Q_d'}{C_{ox}} \quad (2)$$

Putting (2) into (1)

$$-1V - (-1.07V) = \frac{\sqrt{2K\epsilon_0 q N_A V_S}}{C_{ox}} + V_S$$

$$0.07V = 0.235\sqrt{V_S} + V_S \Rightarrow V_S = \underline{\underline{0.0296V}}$$

$$4a) V_0 x = 0.235 \sqrt{V_s} = \underline{\underline{0.0404 \text{ V}}}$$

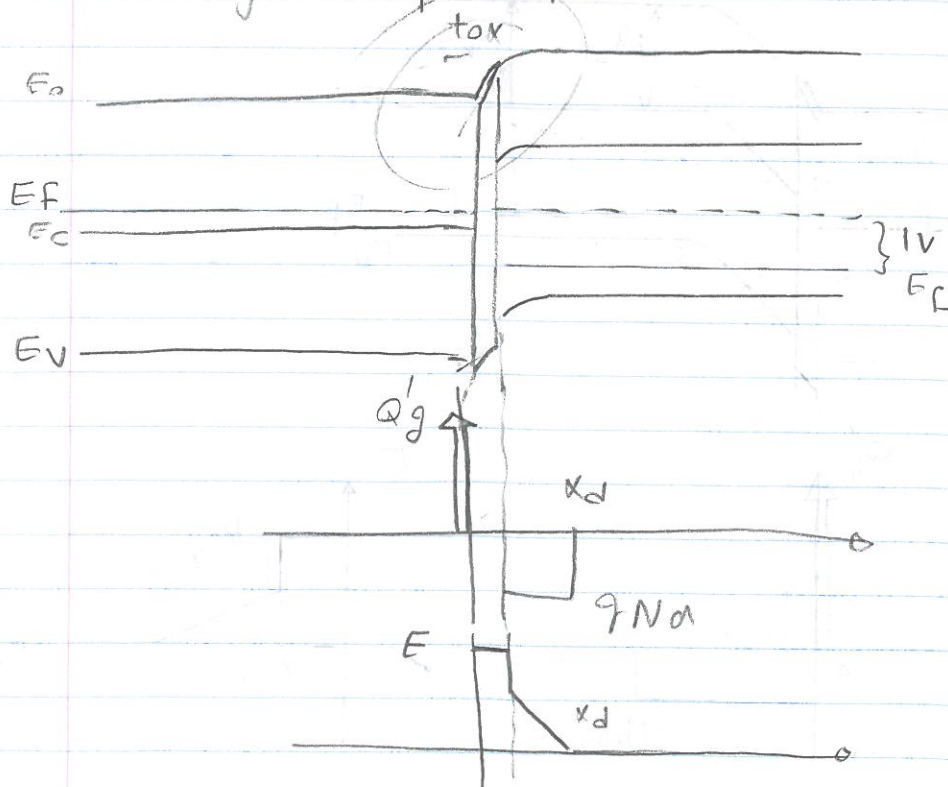
$$Q_g' = C_{ox}' V_0 x = \underline{\underline{0.694 \times 10^{-7} \text{ C cm}^{-2}}}$$

$$x_d = \frac{-Q_s}{qNa} = \frac{Q_g}{qNa} = \frac{0.694 \times 10^{-7} \text{ C cm}^{-2}}{(1.6 \times 10^{-19} \text{ C})(5 \times 10^{17} \text{ cm}^{-3})} = 8.74 \times 10^{-7} \text{ cm} = \underline{\underline{8.74 \text{ nm}}}$$

$$C_s' = C_d' = \frac{k_s \epsilon_0}{x_d} = \frac{(11.7)(8.85 \times 10^{-14} \text{ F cm}^{-1})}{8.74 \times 10^{-7} \text{ cm}} = \underline{\underline{1.18 \times 10^{-6} \text{ F cm}^{-2}}}$$

$$C'_{total} = \frac{C'_{ox} C_d'}{C'_{ox} + C_d'} = \underline{\underline{0.703 \times 10^{-6} \text{ F cm}^{-2}}}$$

Since depletion region width can be modulated rapidly, the capacitance is the same for low and high frequency.



$$4b) V_{gb} = 0V$$

$$V_{FB} < V_{gb} < V_T \Rightarrow \text{depletion}$$

$$\text{Similar to (a)}: V_{gb} - \phi_{ms} = V_{ox} + V_S$$

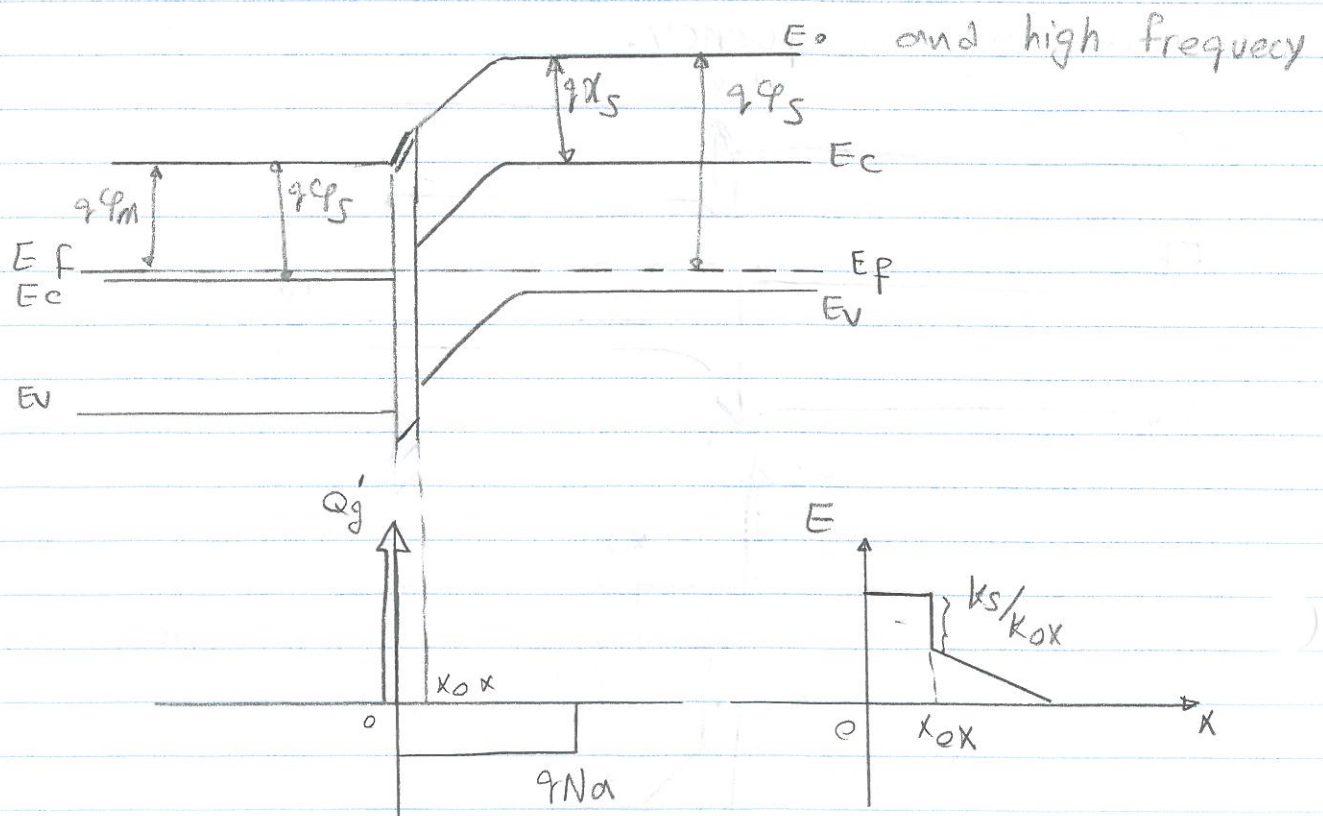
$$0 - (-1.07) = 0.235\sqrt{V_S} + V_S \Rightarrow \underline{V_S = 0.853V}$$

$$V_{ox} = 0.235\sqrt{0.853} \text{ V} = \underline{0.217V}$$

$$Q_g' = C_{ox}' V_{ox} = 3.75 \times 10^{-7} \text{ C cm}^{-2} \quad x_d = \frac{Q_g}{qN_A} = 46.9 \times 10^{-7} \text{ cm} = \underline{46.9 \text{ nm}}$$

$$C_s' = C_d' = \frac{K\epsilon_0}{x_d} = 2.21 \times 10^{-7} \text{ F cm}^{-2}$$

$$C'_{\text{total}} = C_d' \parallel C_{ox}' = \underline{1.96 \times 10^{-7} \text{ F cm}^{-2}} \text{ for both low}$$



4c) $V_{gb} = 1V$ $V_{gb} > V_T \Rightarrow$ inversion

$$V_S \approx \phi_{\text{surface}} = |2\phi_F| = 2|0.433| = 0.866V$$

$$V_{gb} - \phi_{ms} = V_{ox} + V_S \Rightarrow 1 - (-1.07)V = V_{ox} + 0.866V$$

$$\Rightarrow V_{ox} = 1.204V$$

$$V_{ox} = -\frac{Q'_S}{C_{ox}} \Rightarrow Q'_S = -(1.204V)(1.73 \times 10^{-6} \text{ F cm}^{-2})$$

$$= -2.08 \times 10^{-6} \text{ C cm}^{-2} = -Q'_m = -Q'_g$$

$$Q'_i = Q'_m - Q'_{d\max} = 2.08 \times 10^{-6} - (+0.383 \times 10^{-6}) \text{ C cm}^{-2}$$

$$= 1.68 \times 10^{-6} \text{ C cm}^{-2} \text{ or } (Q'_i = C'_{ox}(V_{gb} - V_T) = 1.66 \times 10^{-6} \text{ C cm}^{-2})$$

@ low freq. $C_{\text{total}} = C_{ox} = 1.73 \times 10^{-6} \text{ F cm}^{-2}$

@ high freq. $C_{\text{total}} = C_{ox} || C_{s,\min}$

$$C_{s,\min} = \frac{K_s \epsilon_0}{x_d} \text{ and } x_d = \frac{Q'_i}{qN_a}$$

$$\Rightarrow C_{s,\min} = 3.37 \times 10^{-8} \text{ C cm}^{-2}$$

$$C_{s,\min} = 3.31 \times 10^{-8} \text{ C cm}^{-2} \text{ for HF.}$$

