## $\mathop{\mathrm{Exam}}_{\mathrm{Winter \ 2010}} \#1 - \mathop{\mathrm{EE}}_{482} 482$

The test is open book/open notes. Show all work. Be sure to state all assumptions made and **check** them when possible. The number of points per problem are indicated in parentheses (50 total).

1. The electron concentration in a region of silicon depends linearly on depth with concentration of  $5 \times 10^{15} \,\mathrm{cm}^{-3}$  at surface (x = 0) and  $10^{15} \,\mathrm{cm}^{-3}$  at depth of  $x = 500 \,\mathrm{nm}$ . If the vertical electron current density in this region is constant at  $J_n = 100 \,\mathrm{A/cm}^2$ , calculate the electric field near  $x = 500 \,\mathrm{nm}$ . You may assume that the mobility is constant at  $1250 \,\mathrm{cm}^2/\mathrm{Vs}$ . (12)

2. (a) Sketch the band diagram (*E* vs. *k* along main symmetry directions) for a semiconductor which has  $\mu_p > \mu_n$  and  $N_v < N_c$ . The qualitative relations should be clear from your sketch. Assume scattering lifetimes are equal for holes and electrons. Briefly note reasoning. (10)

(b) Calculate the intrinsic carrier concentration at 300 K in a semiconductor which has a single valence band maxima given by  $E = E_v - (\hbar^2 k^2/2m_0)$  and eight conduction band minima in the  $\langle 111 \rangle$  directions with  $E = E_c + 2\hbar^2(k - k_0)^2/m_0$  where  $k_0 =$  $(\pm a, \pm a, \pm a), E_c - E_v = 1 \text{ eV}$  and  $m_0$  is the free electron mass. (10)

- 3. A GaAs wafer is doped with  $10^{16}$  cm<sup>-3</sup> donors and  $2 \times 10^{15}$  cm<sup>-3</sup> acceptors. It is desired to make this material semi-insulating by doping with chromium, which has a deep acceptor level 0.7 eV above the valence band maximum.
  - (a) What is the minimum required chromium concentrations to drop the majority carrier concentration to  $10^9 \,\mathrm{cm}^{-3}$  at 300 K? (10)

(b) What would be the resulting resistivity of the material? What would be the sheet resistance of a  $200 \,\mu\text{m}$  thick wafer of this material? (8)